

# Principles for software composition 2024/25

## 06 - Erlang and CCS

[Ex. 1] Write a server in erlang to convert temperatures from Celsius degrees to Fahrenheit degrees and vice versa, using the formula  $F = 1.8C + 32$ . The server receives requests of the form  $(Pid, \text{cs}, C)$  or  $(Pid, \text{ft}, F)$  and replies to  $Pid$  by sending messages in analogous format. The server can be stopped by sending the message **stop**. All the other messages are ignored. Spawn a copy of the server, send it some temperatures to convert, check out the results and stop the server.

[Ex. 2] Write an erlang function **copy** that receives an integer  $n$  and if  $n$  is positive it prints  $n$  copies of  $n$  (one per line). Write an erlang function that receives a list of integers and spawn an instance of **copy** for each integer in the list.

[Ex. 3] Write an erlang function **view** that displays the content of the mailbox but makes all messages remain available in the mailbox afterwards.

[Ex. 4] Define a CCS process  $B_k^n$  that represents an in/out buffer with capacity  $n$  of which  $k$  positions are taken. Show that  $B_0^n$  is strongly bisimilar to  $n$  copies of  $B_0^1$  that run in parallel.

[Ex. 5] Write a guarded CCS process whose LTS has infinitely many states without using parallel composition.

[Ex. 6] Prove that CCS strong bisimilarity is a congruence w.r.t. restriction, i.e., that for all  $p, q, \alpha$ :

$$p \simeq q \Rightarrow p \backslash \alpha \simeq q \backslash \alpha$$

[Ex. 7] Prove that the CCS agents

$$p \stackrel{\text{def}}{=} \alpha.(\alpha.\beta.\text{nil} + \alpha.(\beta.\text{nil} + \gamma.\text{nil})) \quad \text{and} \quad q \stackrel{\text{def}}{=} \alpha.(\alpha.\beta.\text{nil} + \alpha.\gamma.\text{nil})$$

are not strong bisimilar.

[Ex. 8] Let us consider the guarded CCS processes

$$p \stackrel{\text{def}}{=} \mathbf{rec} \ x.(\alpha.x + \beta.x) \quad q \stackrel{\text{def}}{=} \mathbf{rec} \ y.(\bar{\alpha}.\text{nil} + \gamma.y) \quad r \stackrel{\text{def}}{=} \mathbf{rec} \ z.(\bar{\beta}.\text{nil} + \bar{\gamma}.z)$$

1. Draw the LTSs of the processes  $p, q, r$  and  $s \stackrel{\text{def}}{=} (p|q|r) \backslash \alpha \backslash \beta \backslash \gamma$ .
2. Show that  $s$  is strong bisimilar to the process  $t \stackrel{\text{def}}{=} \mathbf{rec} \ w.(\tau.w + \tau.\tau.\text{nil})$ .

[Ex. 9] Prove that the following property is valid for any agent  $p$ , where  $\approx$  is the weak bisimilarity:

$$p + \tau.p \approx \tau.p$$