

# Models of computation (MOD) 2013/14

## Exam – July 17, 2014

[Ex. 1] Consider the IMP program

$$w \stackrel{\text{def}}{=} \mathbf{while} \neg(x = 0) \vee \neg(y = 0) \mathbf{do} (x := x - 1; y := y - 1)$$

Define the set of stores  $T = \{\sigma \mid \dots\}$  for which the program  $w$  terminates and:

1. prove formally that for any store  $\sigma \in T$  we have  $\langle w, \sigma \rangle \rightarrow \sigma[0/x, 0/y]$ .  
(Hint: use well-founded induction on  $T$ )
2. prove formally (by using the rule for divergence seen during the course) that  $\langle w, \sigma \rangle \not\rightarrow$  for any store  $\sigma \notin T$ .

[Ex. 2] Consider the HOFL term:

$$t \stackrel{\text{def}}{=} \mathbf{rec} f. \lambda x. \lambda y. \mathbf{if} x \times y \mathbf{then} x \mathbf{else} (fx)((fx)y)$$

Derive the type, the canonical form and the denotational semantics of  $t$ .

[Ex. 3] Consider the CCS agents:

$$p \stackrel{\text{def}}{=} (\mathbf{rec} x. a.x) | \mathbf{rec} x. b.x \quad q \stackrel{\text{def}}{=} \mathbf{rec} x. a.a.x + a.b.x + b.a.x + b.b.x$$

Prove that  $p$  and  $q$  are strongly bisimilar or exhibit an HM-logic formula  $F$  that can be used to distinguish them.

[Ex. 4] Given the  $\mu$ -calculus formula:

$$\phi \stackrel{\text{def}}{=} \nu x. (p \vee \Diamond x) \wedge (q \vee \Box x)$$

compute its denotational semantics and evaluate it on the LTS below:

