Social Network Analysis

A crash course @ UPF

Dino Pedreschi



ISTI-CNR & Università di Pisa



http://kdd.isti.cnr.it





Complex (Social) Networks

- Big graph data and social, information, biological and technological networks
- The architecture of complexity and how real networks differ from random networks:
 - node degree and long tails,
 - social distance and small worlds,
 - clustering and triadic closure.
- Comparing real networks and random graphs.
- The main models of network science: small world and preferential attachment.



Complex (Social) Networks

- Strong and weak ties, community structure and longrange bridges.
- Robustness of networks to failures and attacks.
- Cascades and spreading. Network models for diffusion and epidemics. The strength of weak ties for the diffusion of information. The strength of strong ties for the diffusion of innovation.
- Practical network analytics with Cytoscape and Gephi.
- Simulation of network processes with NetLogo.



Complex (Social) Networks

- Textbooks
 - Albert-Laszlo Barabasi. Network Science (2016)
 - http://barabasi.com/book/network-science
 - David Easley, Jon Kleinberg: Networks, Crowds, and Markets
 (2010)
 - http://www.cs.cornell.edu/home/kleinber/networks-book/
- Network Analytics Software (open):
 - Cytoscape: http://www.cytoscape.org/
 - Gephi: http://gephi.github.io/
- Network Data Repository
 - http://networkrepository.com/
- Simulation of network models: NetLogo

Part 3

- Robustness
- Cascades
- Models of diffusion and spreading
- Empirical studies
- Research highlights at KDD LAB Pisa

Network robustness

A SIMPLE STORY (3):



ROBUSTNESS IN COMPLEX SYSTEMS

Complex systems maintain their basic functions even under errors and failures

$cell \rightarrow mutations$

There are uncountable number of mutations and other errors in our cells, yet, we do not notice their consequences.

Internet → router breakdowns

At any moment hundreds of routers on the internet are broken, yet, the internet as a whole does not loose its functionality.

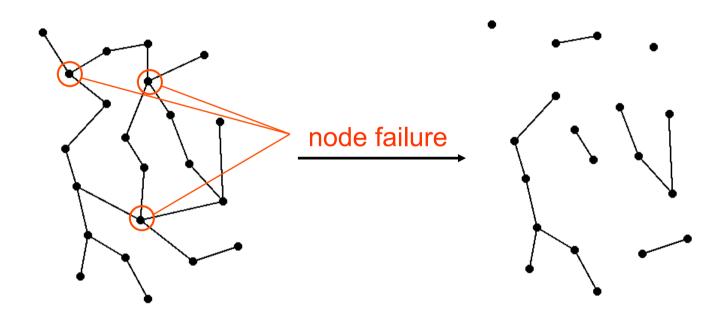
Where does robustness come from?

There are feedback loops in most complex systems that keep tab on the component's and the system's 'health'.

Could the network structure affect a system's robustness?

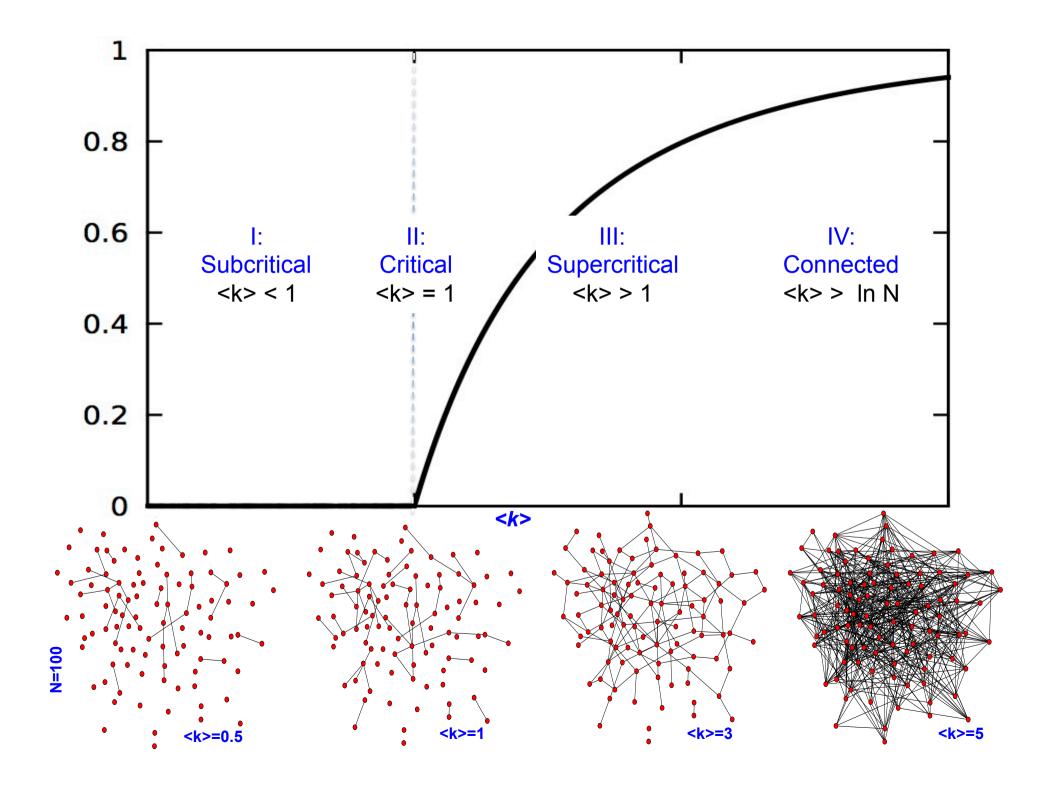
ROBUSTNESS

Could the network structure affect a system's robustness?



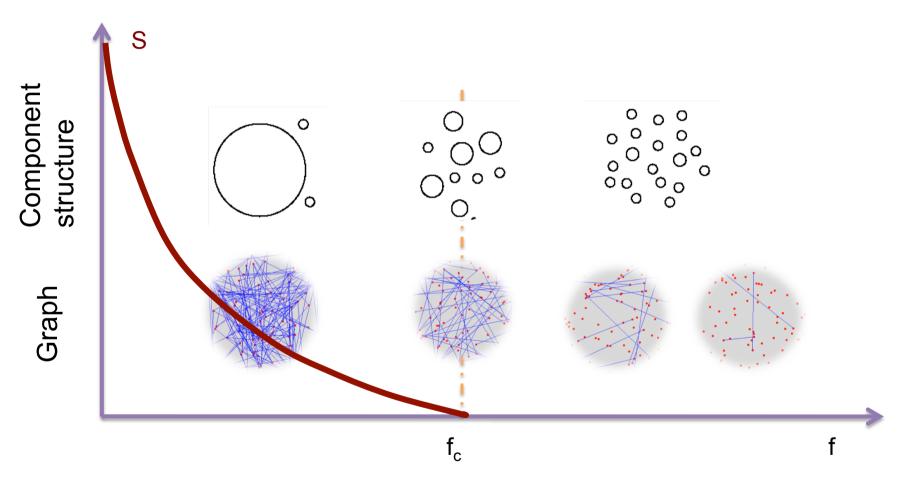
How do we describe in quantitave terms the breakdown of a network under node or link removal?

~percolation theory~



Damage is modeled as an inverse percolation process

f= fraction of removed nodes



(Inverse Percolation phase transition)

ROBUSTNESS: OF SCALE-FREE NETWORKS

The interest in the robustness problem has three origins:

- →Robustness of complex systems is an important problem in many areas
- → Many real networks are not regular, but have a scale-free topology
- → In scale-free networks the scenario described above is not valid

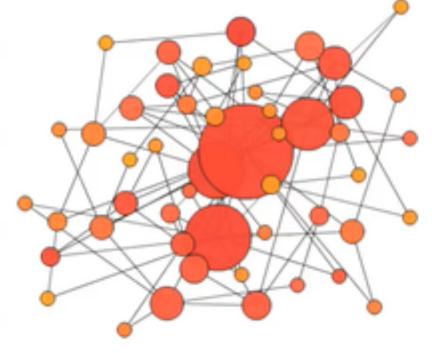
Albert, Jeong, Barabási, Nature 406 378 (2000)

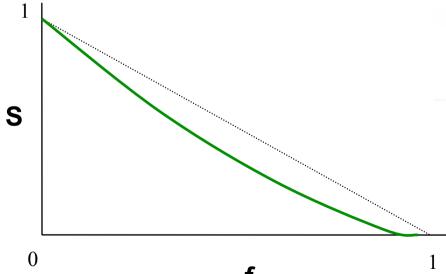
ROBUSTNESS OF SCALE-FREE NETWORKS

Scale-free networks do not appear to break apart under random failures.

Reason: the hubs.

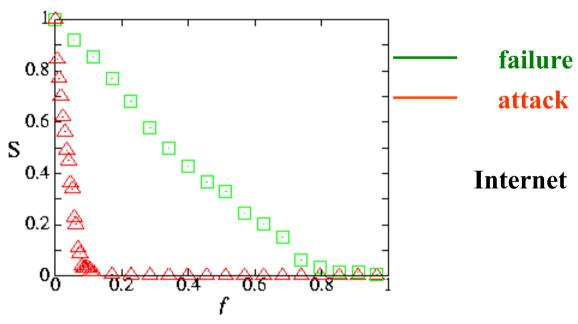
The likelihood of removing a hub is small.





Albert, Jeong, Barabási, *Nature* **406** 378 (2000)

INTERNET'S ROBUSTNESS TO RANDOM FAILURES



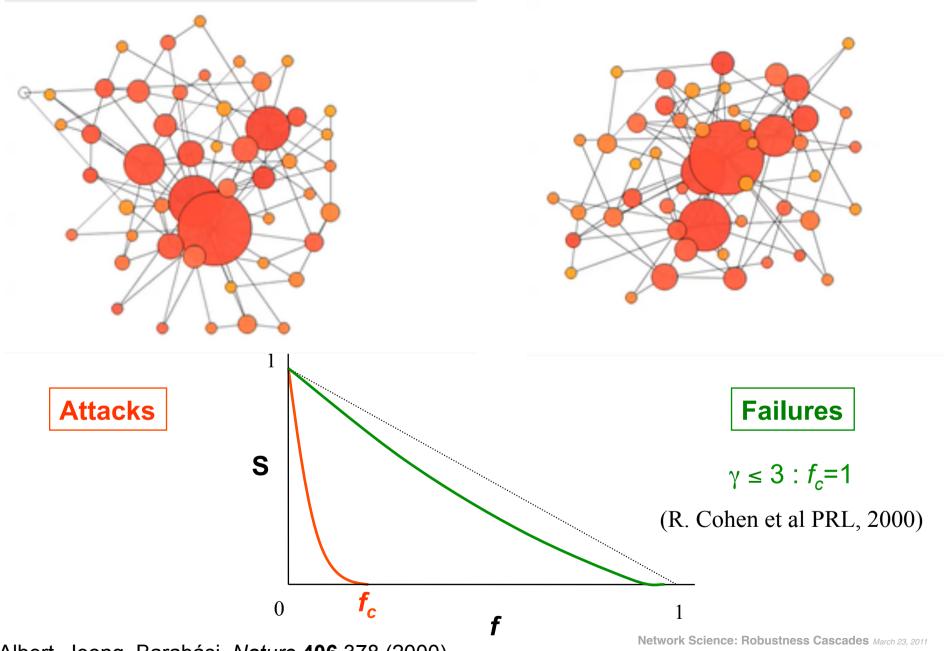
$$f_c = 1 - \frac{1}{\kappa - 1}$$

R. Albert, H. Jeong, A.L. Barabasi, *Nature* **406** 378 (2000)

Internet: Router level map, N=228,263; γ =2.1±0.1; κ =28 \rightarrow f_c =0.962

AS level map, N= 11,164; γ =2.1±0.1; κ =264 \rightarrow f_c =0.996

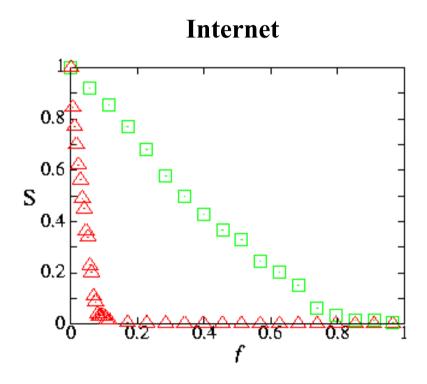
Achilles' Heel of scale-free networks



Albert, Jeong, Barabási, Nature 406 378 (2000)

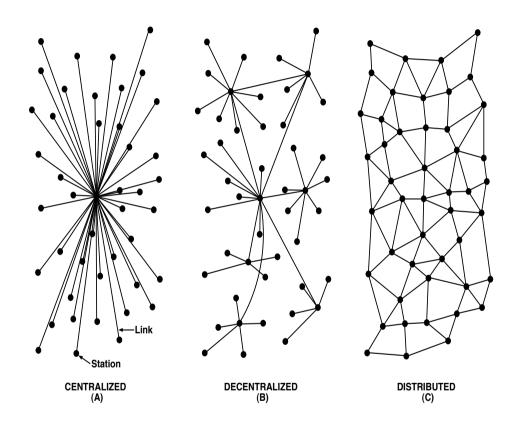
Achilles' Heel of complex networks

failure attack

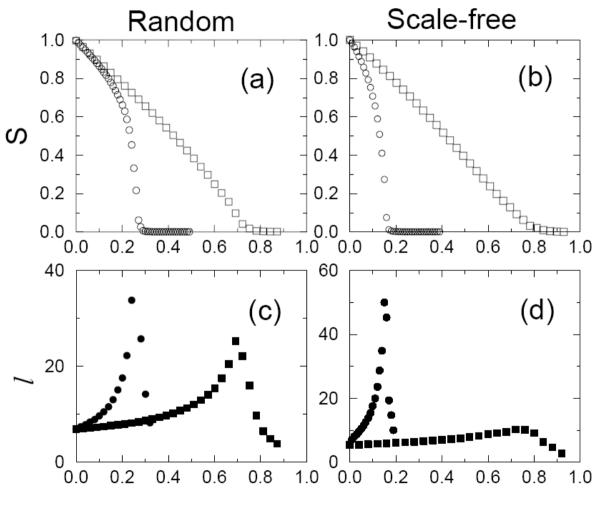


R. Albert, H. Jeong, A.L. Barabasi, *Nature* **406** 378 (2000)

Historical Detour: Paul Baran and Internet



Scale-free networks are more error tolerant, but also more vulnerable to attacks



- squares: random failure
- circles: targeted attack

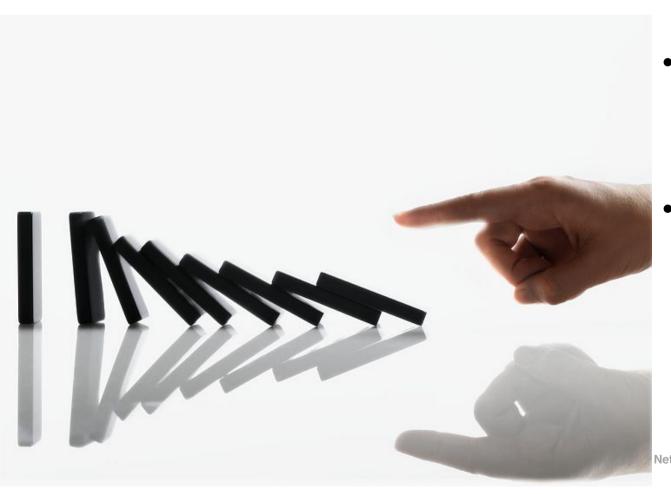
Failures: little effect on the integrity of the network.

Attacks: fast breakdown

Cascades

Cascades

Potentially large events triggered by small initial shocks



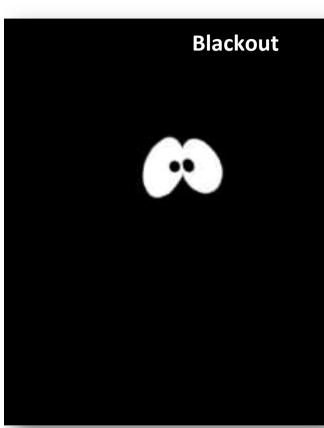
- Information cascades

 social and economic
 systems
 diffusion of innovations
- Cascading failures

 infrastructural networks
 complex organizations

Network Science: Robustness Cascades March 23, 2011

Cascading Failures in Nature and Technology







Flows of physical quantities

- congestions
- instabilities
- Overloads

Cascades depend on

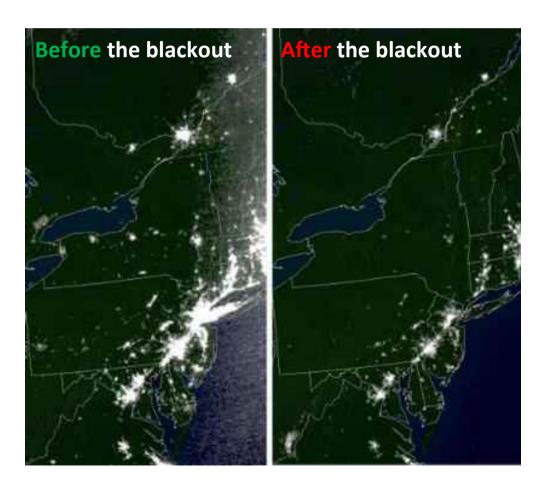
- Structure of the network
- Properties of the flow
- Properties of the net elements
- Breakdown mechanism

Network Science: Robustness Cascades March 23, 2011

Northeast Blackout of 2005

Origin

A 3,500 MW power surge (towards Ontario) affected the transmission grid at 4:10:39 p.m. EDT. (Aug-14-2003)

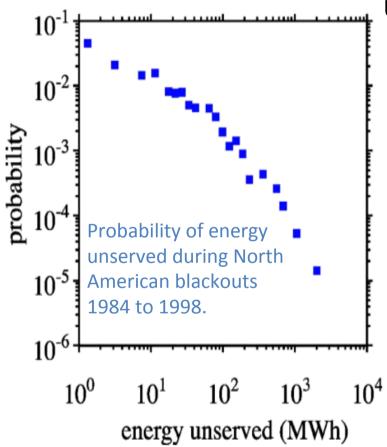




Consequences

More than 508 generating units at 265 power plants shut down during the outage. In the minutes before the event, the NYISO-managed power system was carrying 28,700 MW of load. At the height of the outage, the load had dropped to 5,716 MW, a loss of 80%.

Cascades Size Distribution of Blackouts



Unserved energy/power magnitude (S) distribution

$$P(S) \sim S^{-\alpha}, 1 < \alpha < 2$$

Source	Exponent	Quantity
North America	2.0	Power
Sweden	1.6	Energy
Norway	1.7	Power
New Zealand	1.6	Energy
China	1.8	Energy

I. Dobson, B. A. Carreras, V. E. Lynch, D. E. Newman, CHAOS 17, 026103 (2007)

Cascades Size Distribution of Earthquakes Determination of Epicenters

358,214 Events, 1963 - 1998 10⁴ Shallow (0 70 km) earthquakes 10³ Earthquake Cumulative Number 10² Intermediate (70 300 km) Earthquake size S distribution 10 Earthquakes during 1977–2000. $P(S) \sim S^{-\alpha}, \alpha \approx 1.67$ 5.5 6.5 7.5 8 Moment Magnitude

Y. Y. Kagan, Phys. Earth Planet. Inter. 135 (2-3), 173-209 (200%) work Science: Robustness Cascades March 23, 2011

Short Summary of Models: Universality

Models	Networks	Exponents
Failure Prorogation Model	ER	1.5
Overload Model	Complete Graph	1.5
BTW Sandpile Model	ER/SF	1.5 (ER) $\gamma/(\gamma - 1)$ (SF)
Branching Process Model	ER/SF	1.5 (ER) $\gamma/(\gamma - 1)$ (SF)

Universal for homogenous networks

$$P(S) \sim S^{-3/2}$$

Same exponent for percolation too (random failure, attacking, etc.)

Epidemics and spreading

Epidemic spreading – Why?

Why is the spreading process important?







"Epidemic"

upon

people



Biological:

Airborne diseases (flu, SARS, ...)

- Venereal diseases (HIV, ...)
- Other infectious diseases including some cancers (HPV, ...)
- Parasites (bedbugs, malaria, ...)

Digital:

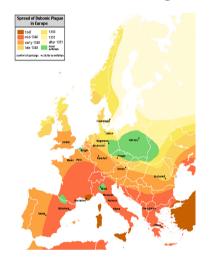
- Computer viruses, worms
- Mobile phone viruses

Conceptual/Intellectual:

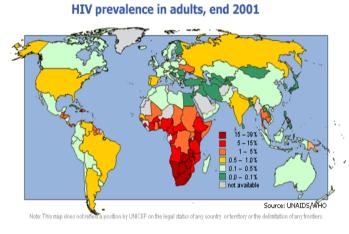
- Diffusion of innovations
- Rumors
- Memes
- Business practices

Biological: Notable Epidemic Outbreaks

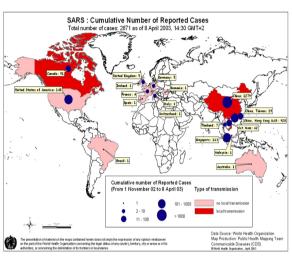
The Great Plague



HIV



SARS



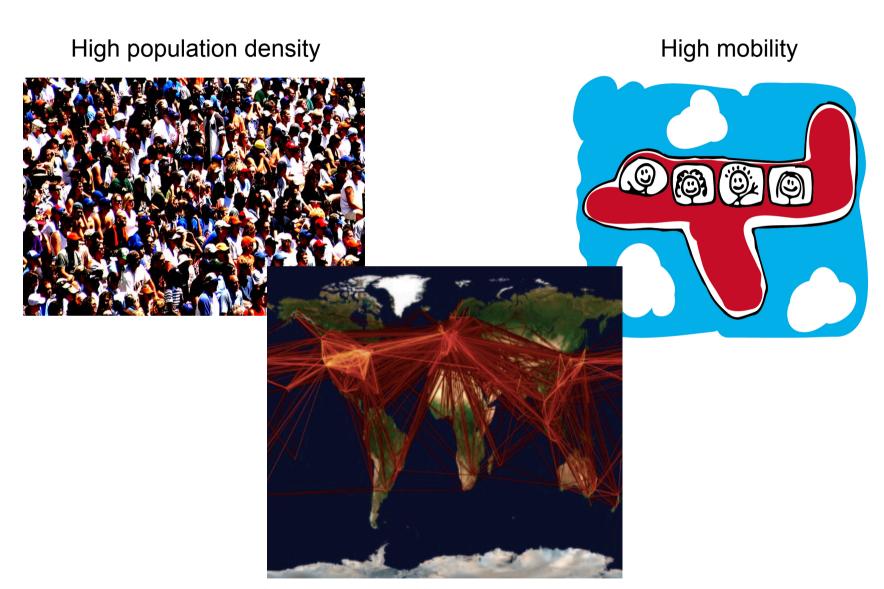


1918 Spanish flu



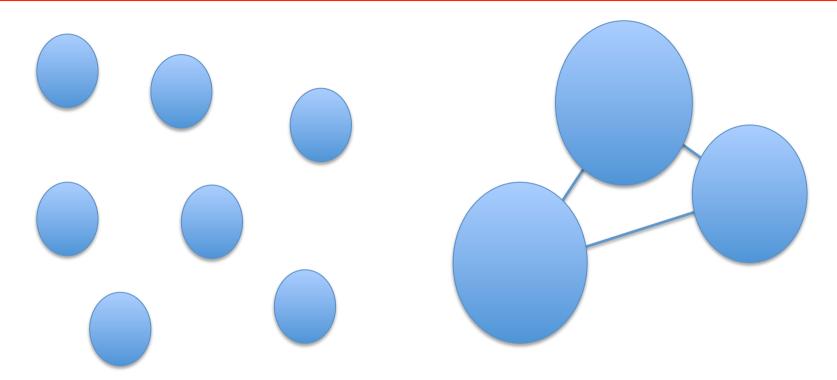
H1N1 flu

Epidemic spreading – Why does it matter now?



→ perfect conditions for epidemic spreading.

Large population can provide the "fuel"

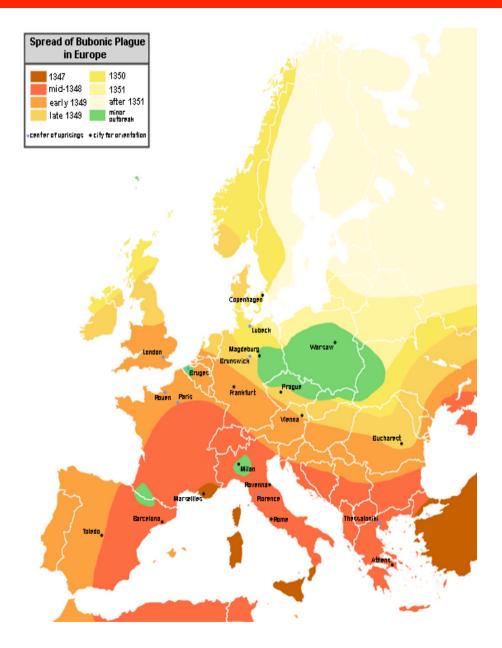


Separate, small population (hunter-gatherer society, wild animals)

Connected, highly populated areas (cities)

Human societies have "**crowd diseases**", which are the consequences of large, interconnected populations (Measles, tuberculosis, smallpox, influenza, common cold, ...)

14th Century – The Great Plague

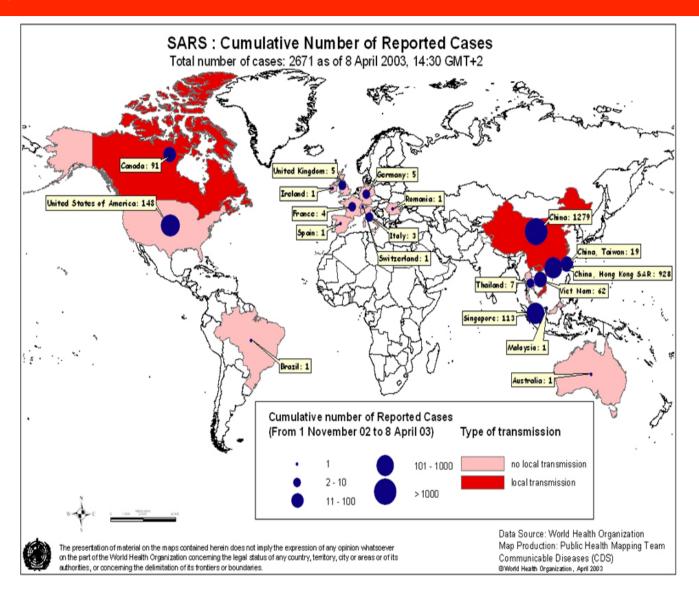


4 years from France to Sweden

Limited by the speed of human travel

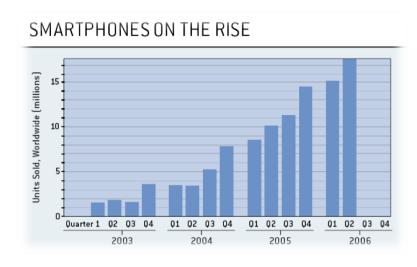
http://en.wikipedia.org/wiki/Black_Death http://de.wikipedia.org/wiki/Schwarzer_Tod

21st Century – SARS

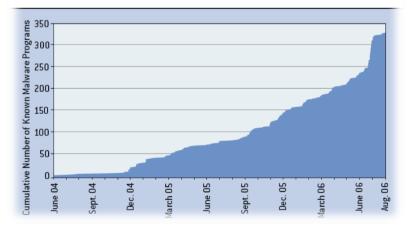


Source: World Health Organization

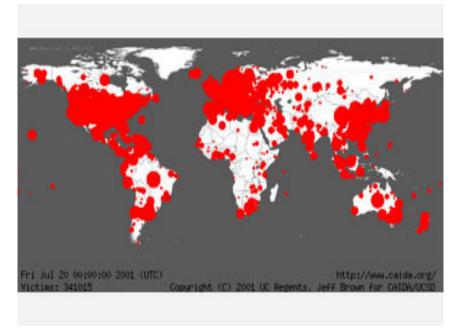
Computer Viruses, Worms, Mobile Phone Viruses



GROWTH IN MOBILE MALWARE



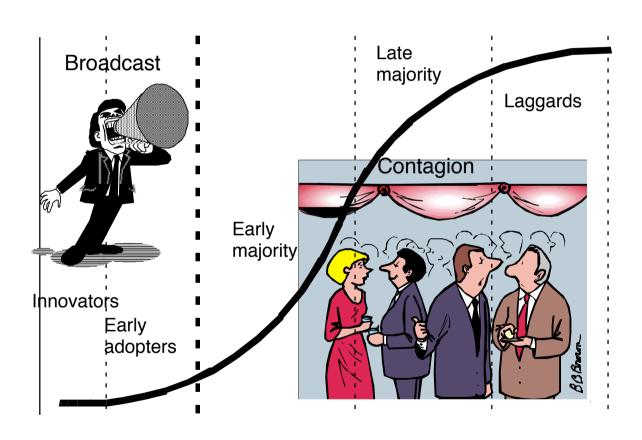
Code Red Worm paralyzed many countries' Internet



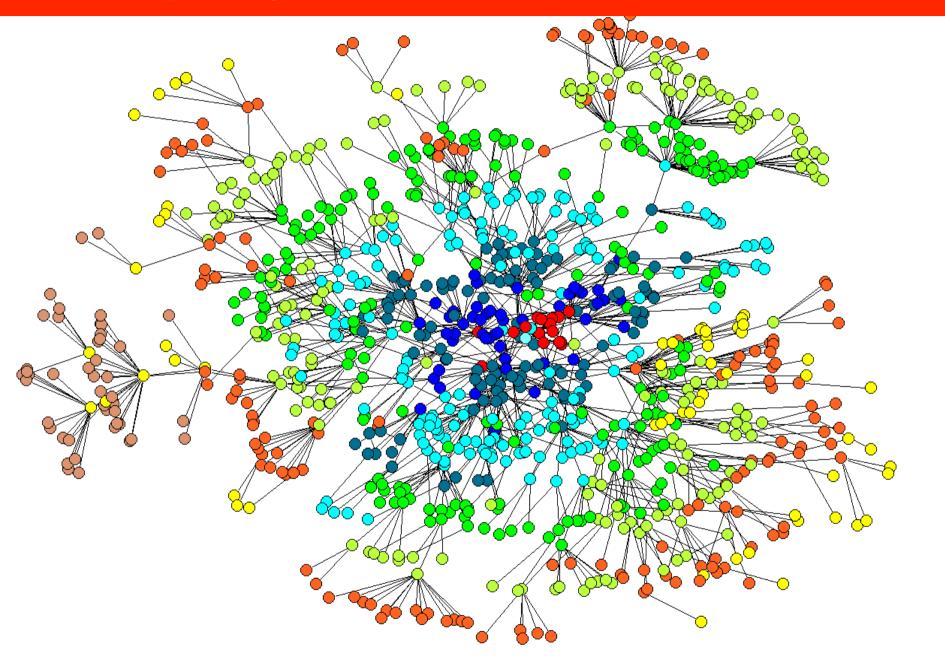
http://www.caida.org/publications/visualizations/

Hypponen M. Scientific American Nov. 70-77 (2006).

Diffusion of Innovation – The Adoption Curve



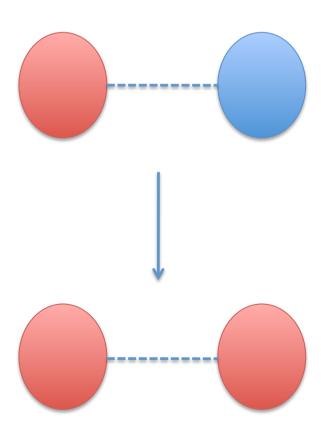
Information Spreading



Epidemic Spreading – Network

 Epidemic spreading always implies network structure!

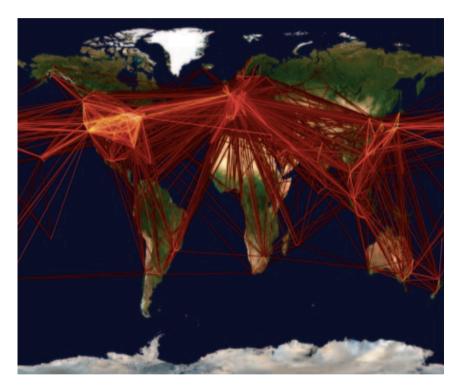
Spreading happens only when the carries of the diseases/virus/idea are connected to each other.

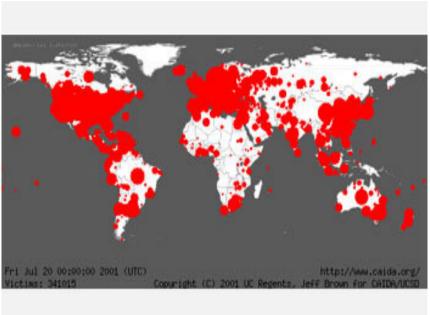


Epidemic Spreading – Network



Epidemic Spreading – Network





The transportation network

Internet

L. Hufnagel et al. *PNAS* **101**, 15124 (2004)

http://www.caida.org/publications/visualizations/

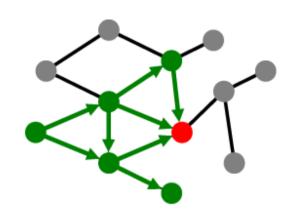
How to model diffusion?

Probabilistic models:

- Models of influence or disease spreading
 - An infected node tries to "push" the contagion to an uninfected node

Example:

You "catch" a disease with some prob.
 from each active neighbor in the network



Decision based models:

- Models of product adoption, decision making
 - A node observes decisions of its neighbors and makes its own decision

Example:

You join demonstrations if k of your friends do so too

Decision-based diffusion models

Collective action

[Granovetter 1978]

Collective Action [Granovetter, '78]

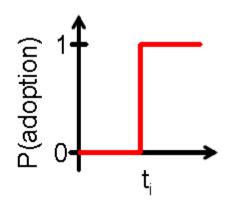
 Model where everyone sees everyone else's behavior

Examples:

- Clapping or getting up and leaving in a theater
- Keeping your money or not in a stock market
- Neighborhoods in cities changing ethnic composition
- Riots, protests, strikes

The model of collective action

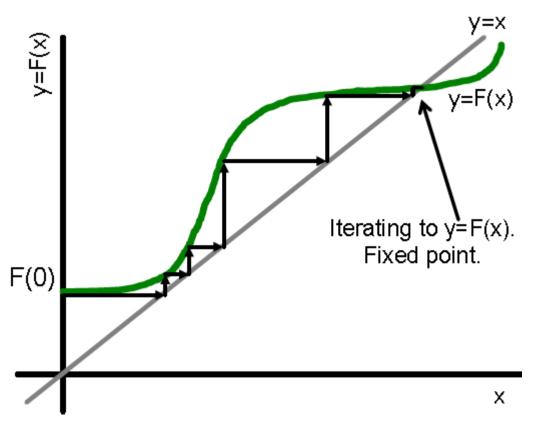
- n people everyone observes all actions
- Each person i has a threshold t_i
 - Node i will adopt the behavior iff at least t_i other people are adopters:
 - Small t_i: early adopter
 - Large t_i: late adopter



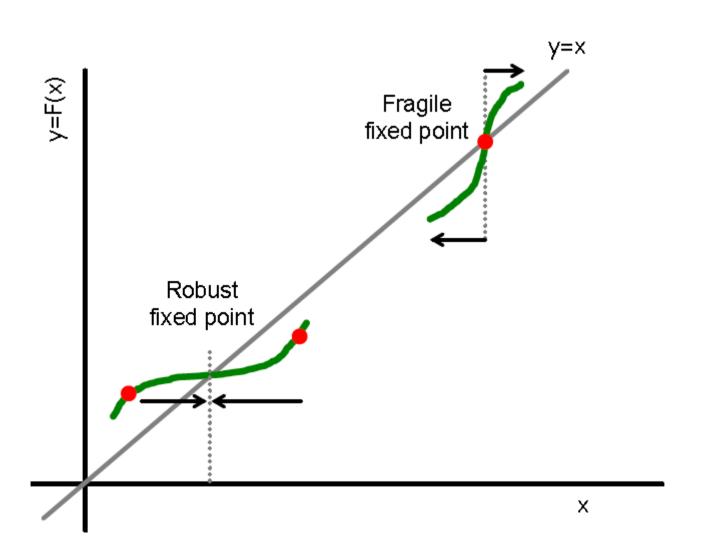
- The population is described by {t₁,...,t_n}
 - F(x) ... fraction of people with threshold $t_i \le x$

Dynamics of collective action

- Think of the step-by-step change in number of people adopting the behavior:
 - F(x) ... fraction of people with threshold $\leq x$
 - s(t) ... number of participants at time t
- Easy to simulate:
 - s(0) = 0
 - s(1) = F(0)
 - s(2) = F(s(1)) = F(F(0))
 - $s(t+1) = F(s(t)) = F^{t+1}(0)$
- Fixed point: F(x)=x
 - There could be other fixed points but starting from 0 we never reach them



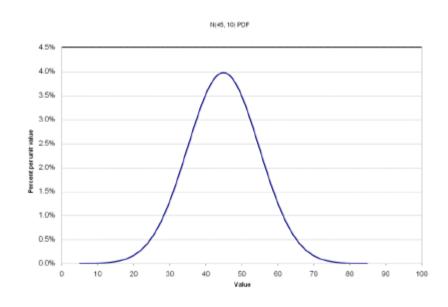
Fragile vs. robust fixed points

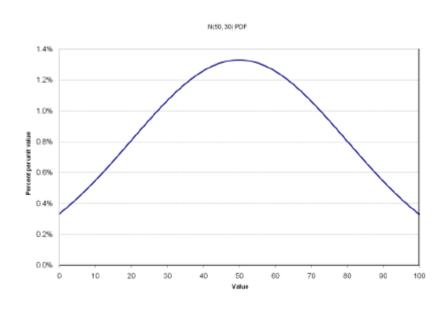


Distribution of thresholds (trust)

- Each threshold t_i is drawn independently from some distribution $F(x) = Pr[thresh \le x]$
 - Suppose: Normal with $\mu=n/2$, variance σ

Small σ: Large σ:



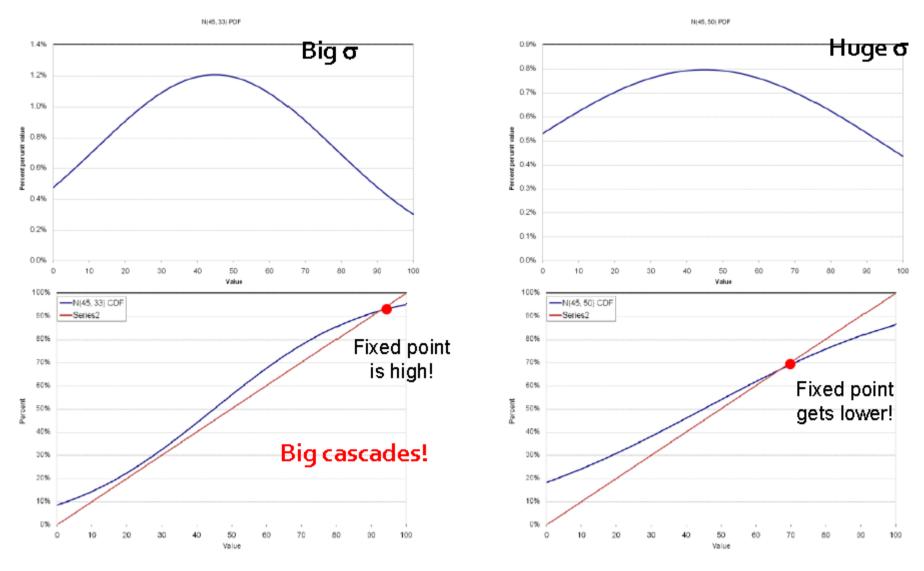


Simulation

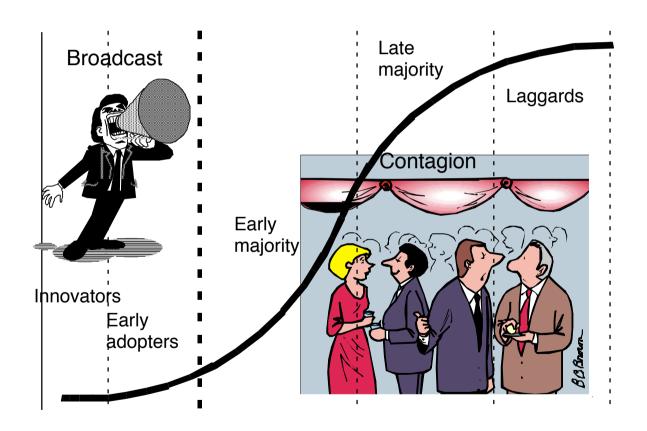


Bigger variance let's you build a bridge from early adopters to mainstream

Simulation



But if we increase the variance even more we move the higher fixed point lover



Weaknesses of the CA model

It does not take into account:

- No notion of social network more influential users
- It matters who the early adopters are, not just how many
- Models people's awareness of size of participation not just actual number of people participating

Modeling thresholds

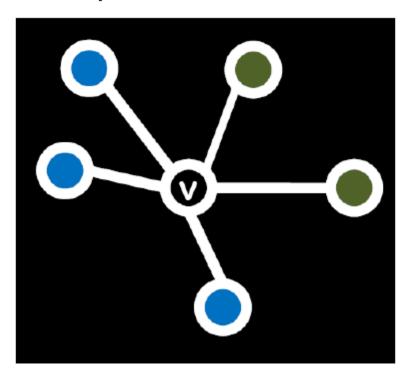
- Richer distributions
- Deriving thresholds from more basic assumptions
 - game theoretic models

Decision-based diffusion models

Game-theoretic models of cascades [Moore 2000]

Game theoretic models of cascades

- Based on 2 player coordination game
 - 2 players each chooses technology A or B
 - Each person can only adopt one "behavior", A or B
 - You gain more payoff if your friend has adopted the same behavior as you



Local view of the network of node v

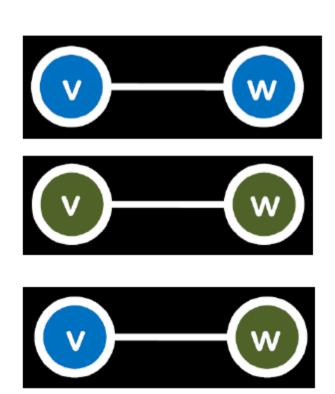
Rules of the game

Payoff matrix:

- If both v and w adopt behavior A, they each get payoff a>0
- If v and w adopt behavior B, they reach get payoff b>0
- If v and w adopt the opposite behaviors, they each get O

In some large network:

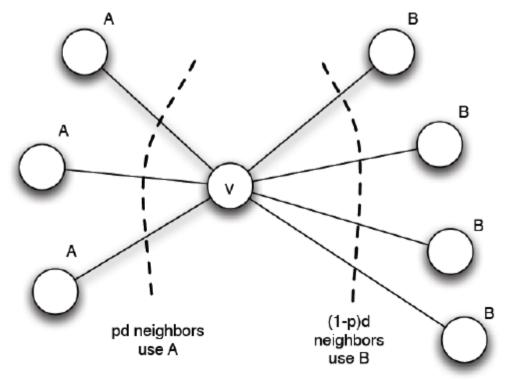
- Each node ν is playing a copy of the game with each of its neighbors
- Payoff: sum of node payoffs per game



A	B
a, a	0,0
0,0	b, b

w

Decision rule for node v



Threshold:

v choses A if p>q

$$q = \frac{b}{a+b}$$

- Let v have d neighbors
- Assume fraction p of v's neighbors adopt A

■
$$Payoff_v = a \cdot p \cdot d$$
 if v chooses A
= $b \cdot (1-p) \cdot d$ if v chooses B

■ Thus: v chooses A if: $a \cdot p \cdot d > b \cdot (1-p) \cdot d$

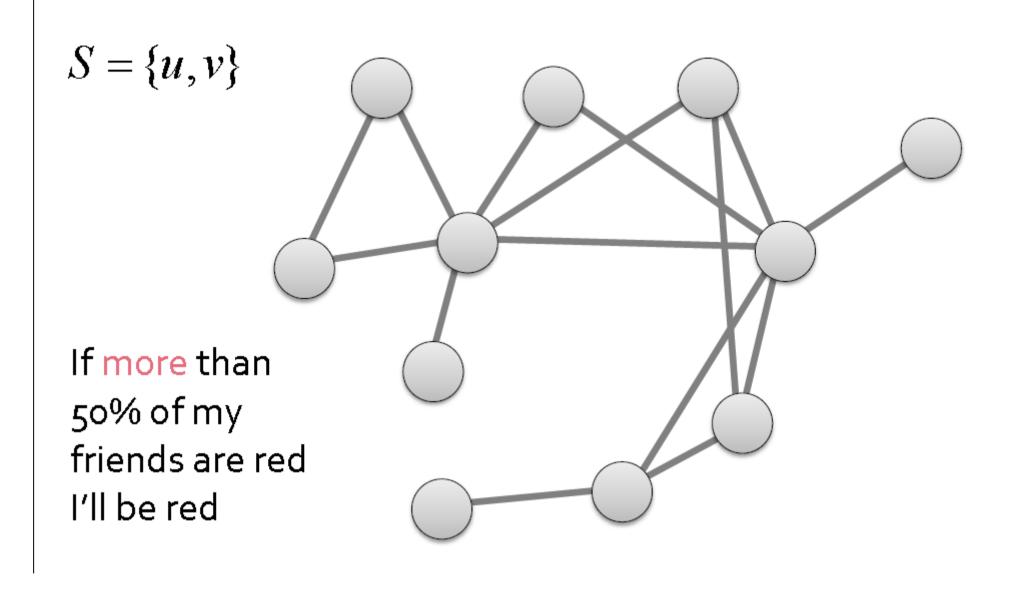
Example

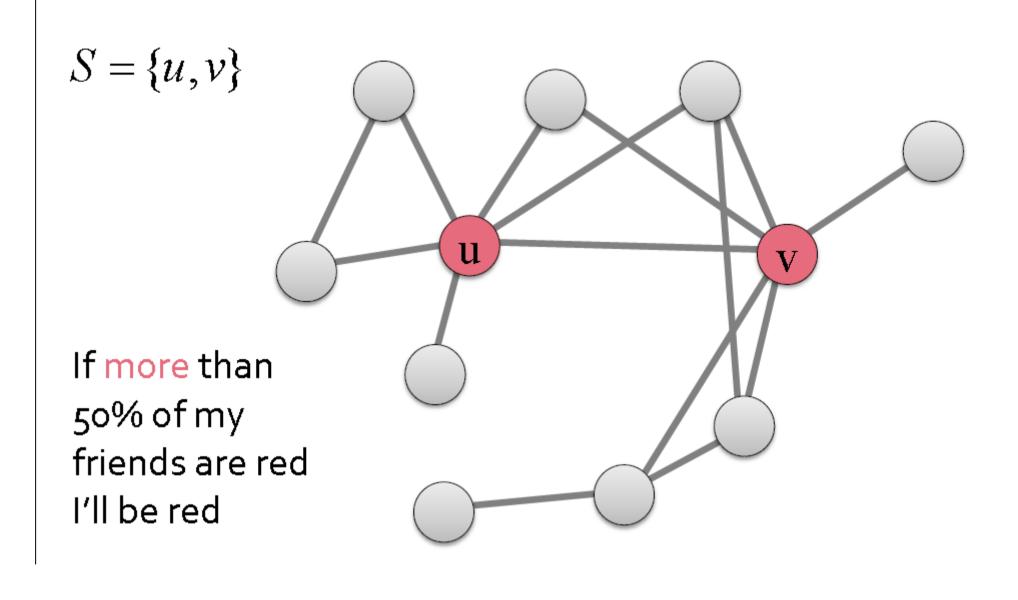
Scenario:

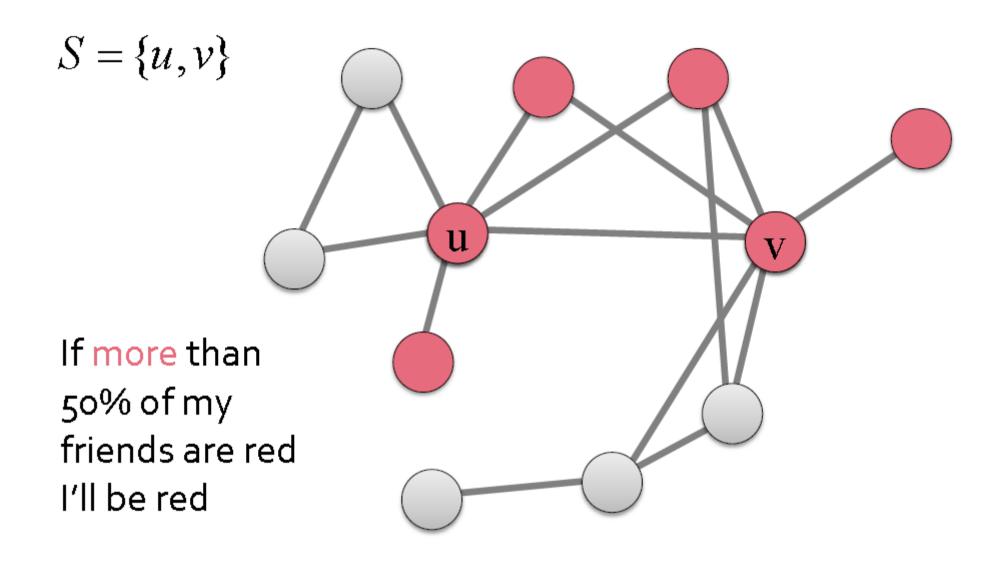
Graph where everyone starts with B. Small set S of early adopters of A

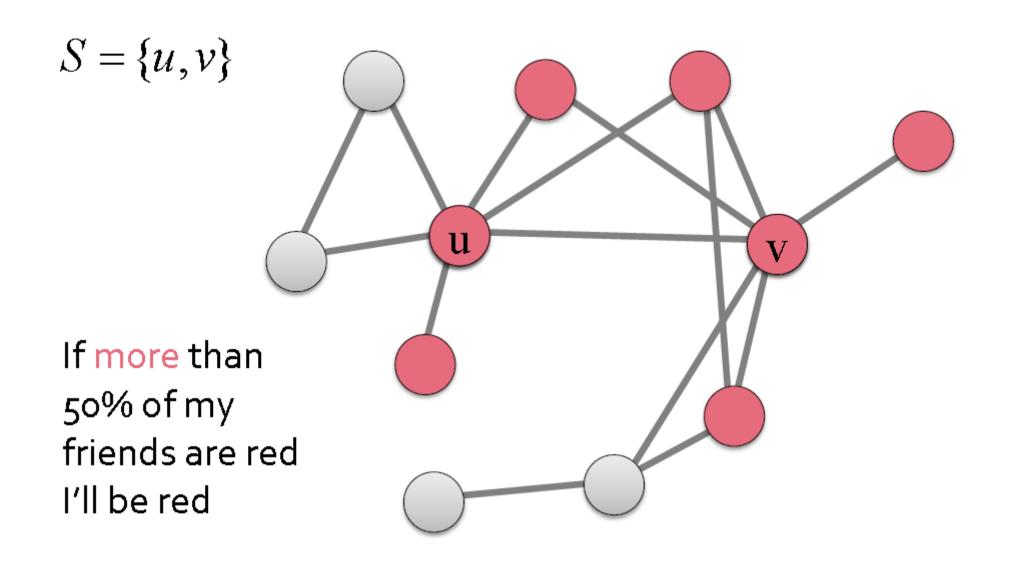
- Hard wire S they keep using A no matter what payoffs tell them to do
- Payoffs are set in such a way that nodes say:
 If at least 50% of my friends are red I'll be red

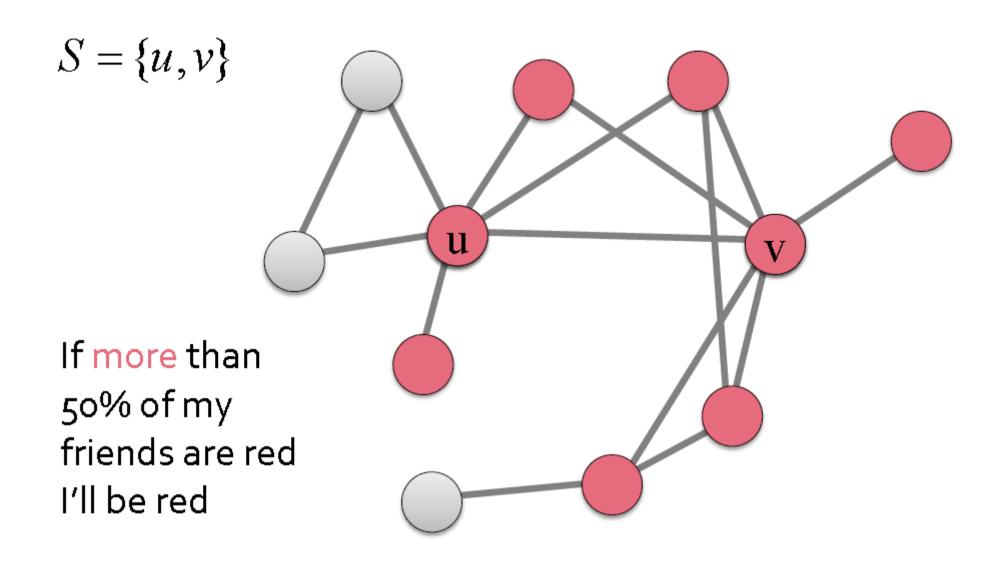
(this means: $a = b + \varepsilon$)

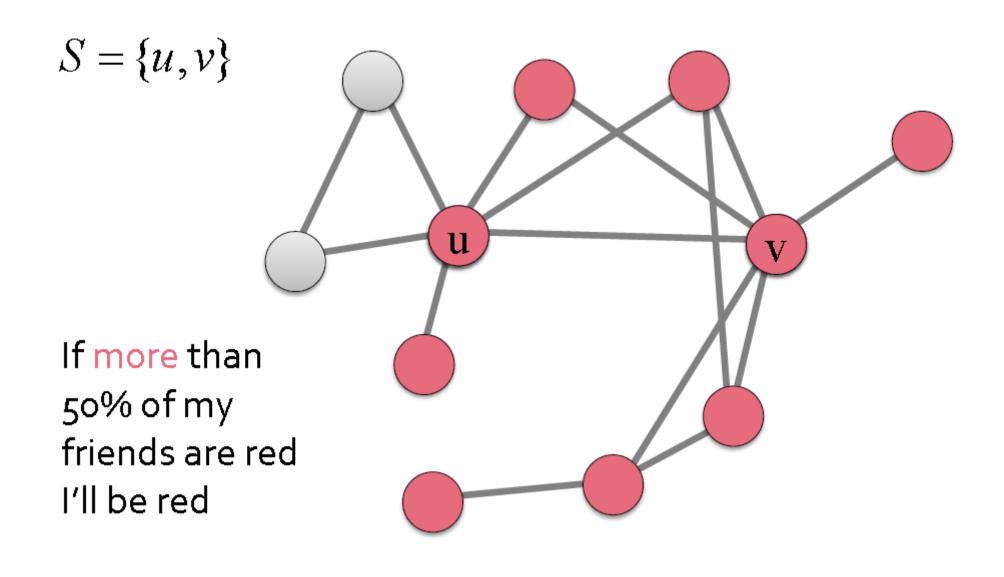






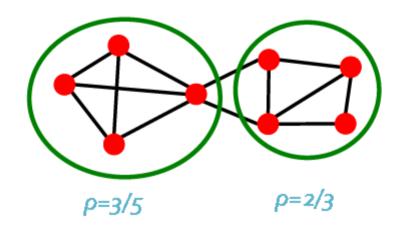






Stopping cascades

- What prevents cascades from spreading?
- Def: Cluster of density ρ is a set of nodes C where each node in the set has at least ρ fraction of edges in C.



Stopping cascades

- Let S be an initial set of adopters of A
- All nodes apply threshold q to decide whether to switch to A

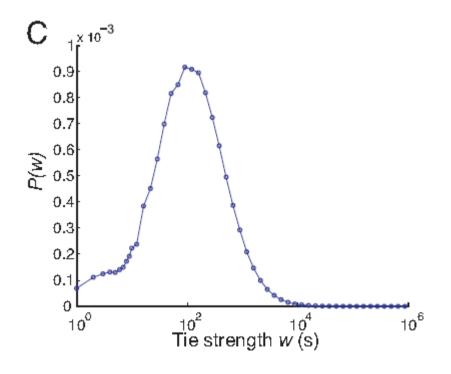
Two facts:

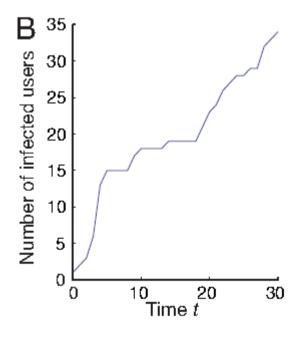
- 1) If G\S contains a cluster of density >(1-q)
 then S can not cause a cascade
- 2) If S fails to create a cascade, then there is a cluster of density >(1-q) in G\S

Empirical studies of cascading behavior

The strength of weak ties ...

 For information diffusion (spreading of news and rumors on a social network)





The weakness of weak ties

Diffusion of innovation / adoption

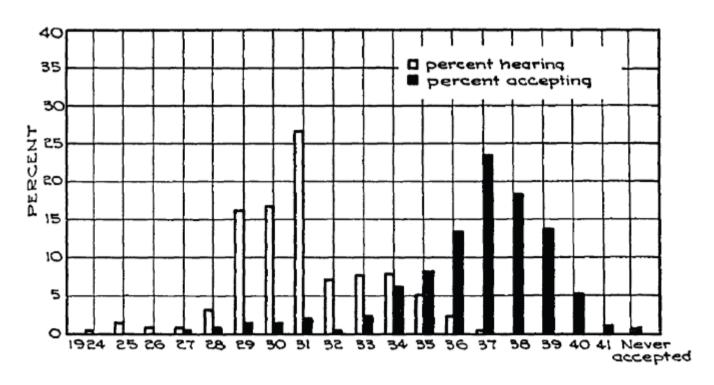
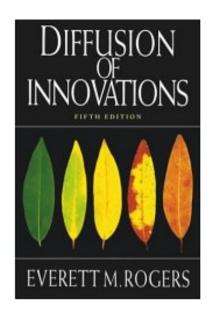
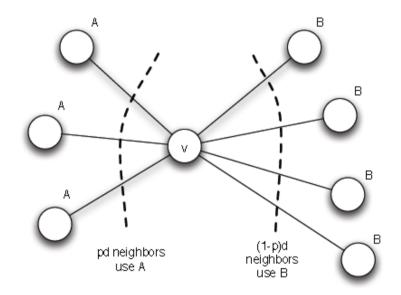
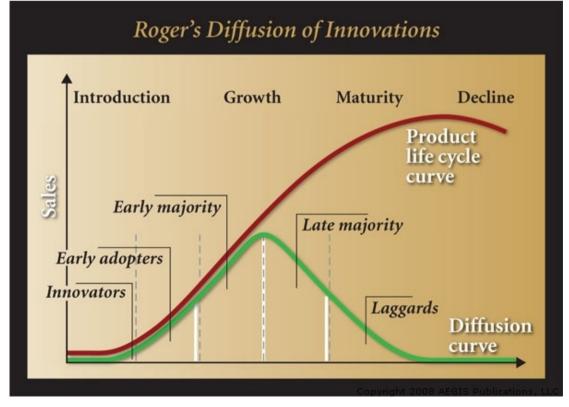


Figure 19.10: The years of first awareness and first adoption for hybrid seed corn in the Ryan-Gross study. (Image from [358].)

The strength of the strong ties for the







Adoption Curve: LiveJournal

Group memberships spread over the

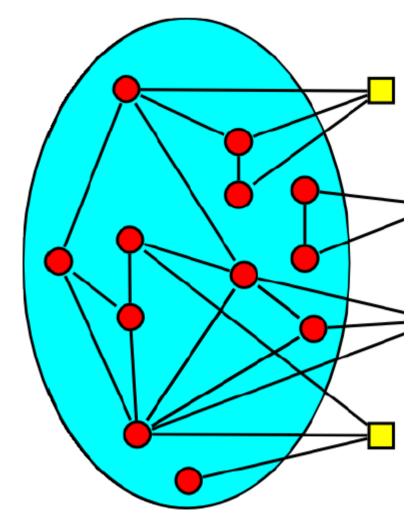
network:

 Red circles represent existing group members

Yellow squares may join

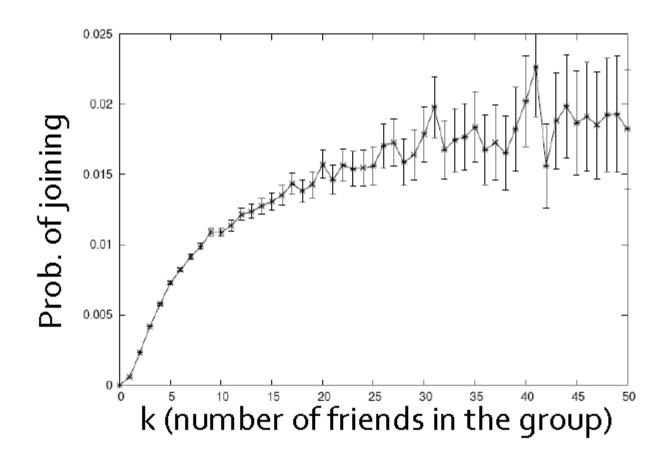
• Question:

How does prob. of joining a group depend on the number of friends already in the group?



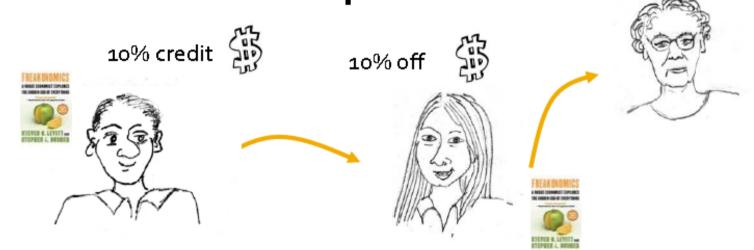
Adoption Curve: LiveJournal

LiveJournal group membership



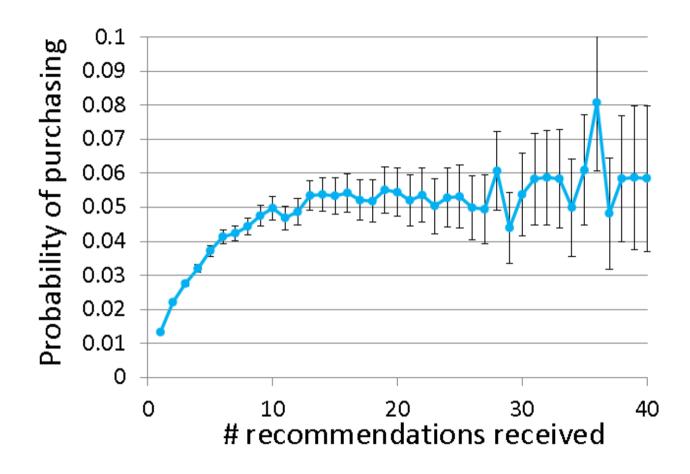
Diffusion in Viral Marketing

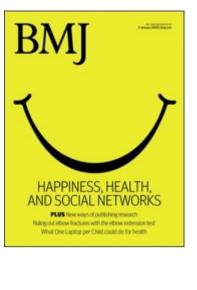
 Senders and followers of recommendations receive discounts on products

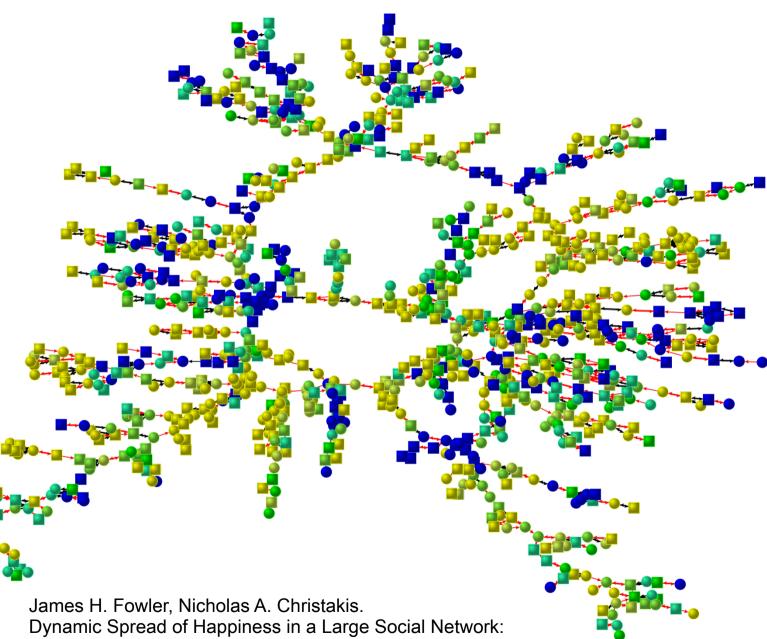


- Data: Incentivized Viral Marketing program
 - 16 million recommendations
 - 4 million people, 500k products

Adoption Curve: Validation







James H. Fowler, Nicholas A. Christakis.

Dynamic Spread of Happiness in a Large Social Network:

Longitudinal Analysis Over 20 Years in the Framingham Heart Study

British Medical Journal 337 (4 December 2008)

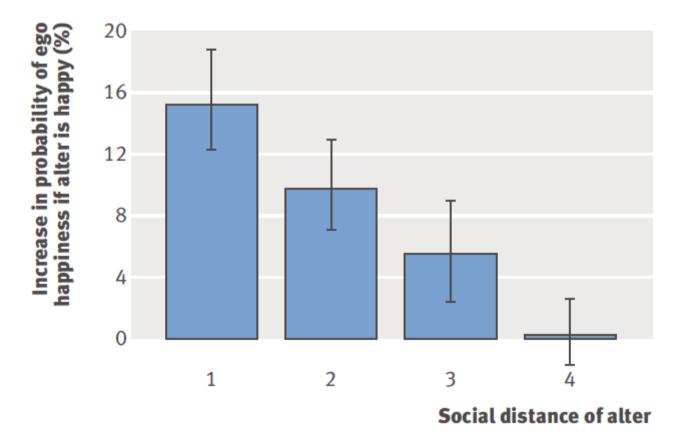


Fig 2 | Social distance and happiness in the Framingham social network. Percentage increase in likelihood an ego is happy if friend or family member at certain social distance is happy (instead of unhappy). The relationship is strongest between individuals who are directly connected but remains significantly >0 at social distances up to three degrees of separation, meaning that a person's happiness is associated with happiness of people up to three degrees removed from



Social influence or homophily?



Research highlights

The Three Dimensions of Social Prominence

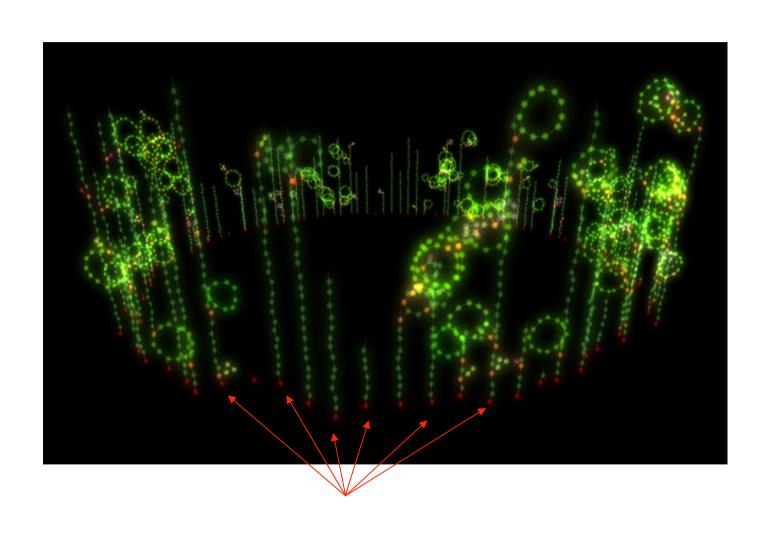
Diego Pennacchioli^{2,3}, Giulio Rossetti^{1,2}, Luca Pappalardo^{1,2}, Fosca Giannotti², Dino Pedreschi^{1,2}

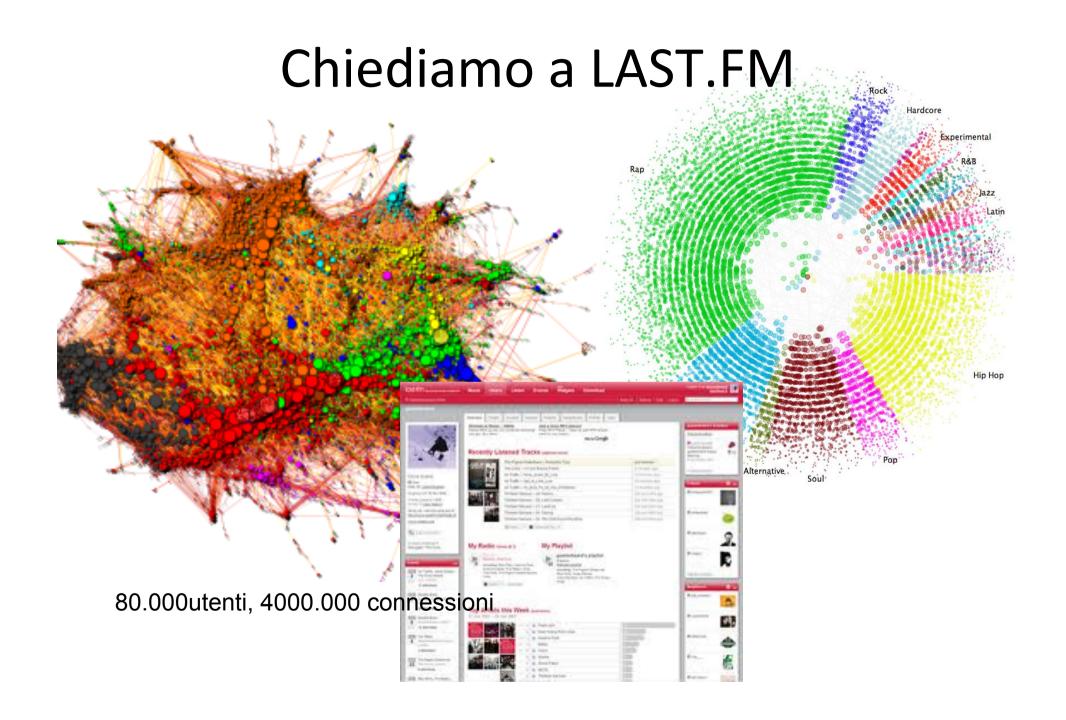
¹ Computer Science Dep., University of Pisa, Italy {rossetti,pedre}@di.unipi.it ² ISTI - CNR KDDLab, Pisa, Italy {fosca.giannotti, giulio.rossetti}@isti.cnr.it ³IMT Lucca, Italy



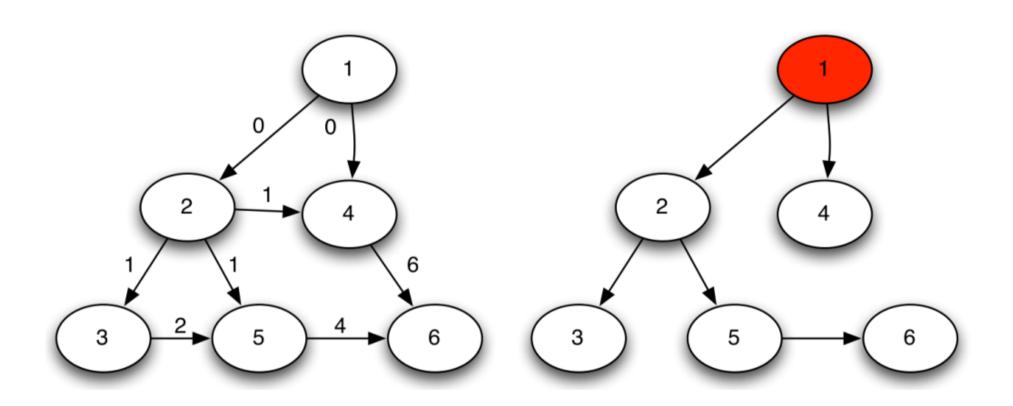


Social Influence: Leaders

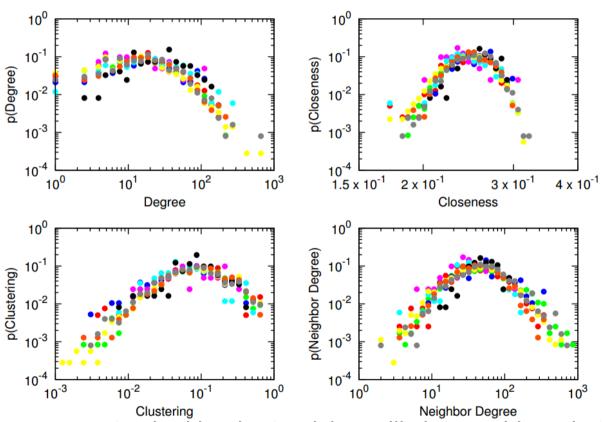




Leader finding



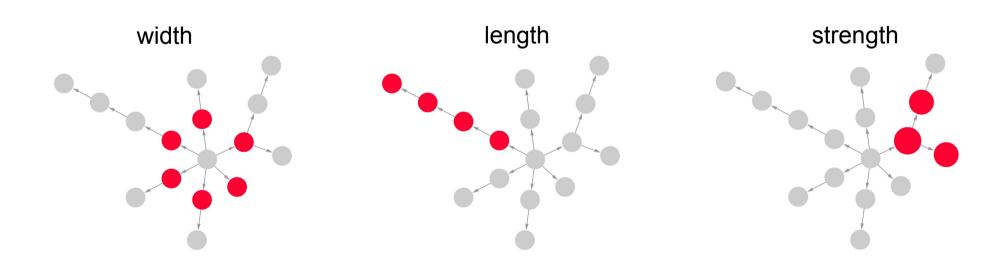
dai BigData...i veri influenzer non sono i leaders



... abbiamo scoperto che i leader teorici, quelli che avrebbero in teoria il potere di influenzare la rete sociale, non hanno una grande influenza pratica sulla rete.

What is Social Prominence?

- It has been observed that a small set of users in a Social Network is able to anticipate (or influence) the behavior of the entire network
- We detected 3 possible scenarios:

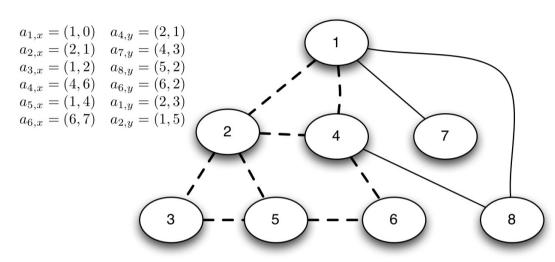


The Idea

- Define what a "leader" is
- Identify three measures of social prominence (width, depth and strength)
- Analyze their relationship with the topological characteristic of prominent actors in a network
- Look for patterns distinguishing different objects spreading in a social network

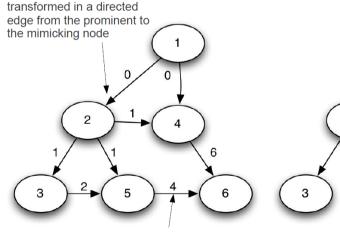
Leaders and structure

Each social connection is



For each Artist we extract the induced temporal subgraph of its Listeners

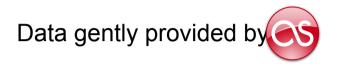
We define Leader all those nodes that are the first, in their neighborhood to adopt the given artist



The label on the edge represents the timestep in which the prominent node performed the action

The Minimum
Diffusion Tree (MDT)
is then the minimum
spanning tree

Data, experiments and results

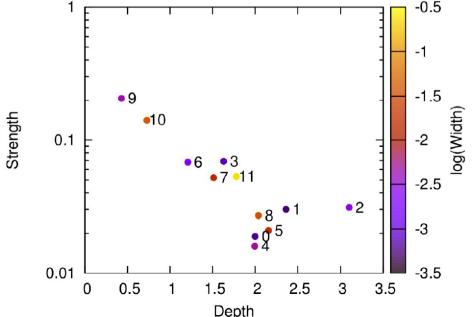


	Width	${\bf Strength}$	Degree	${\bf Clustering}$	Neigh Deg	${\bf Bet}\ {\bf Centr}$	Clo Centr
AVG Depth	-0.03	-0.23	-0.08	0.05	-0.08	-0.02	-0.13
Width	-	0.01	-0.31	0.13	0.05	-0.07	-0.59
Strength	-	-	0.02	-0.02	0.03	0.00	0.04
Degree	-	-	-	-0.16	-0.02	0.77	0.56
Clustering	-	-	-	-	-0.05	-0.06	-0.32
Neigh Deg	-	-	-	-	-	-0.00	0.39
Bet Centr	-	-	-	-	-	-	0.22

Central nodes are characterized by low Depth & Width High Width are usually reached only by nodes in tightly knit communities There is a trade-off between Depth and Strength (not between D and W nor between S a

Data, experiments and results

Cluster	size	dance	ele	folk	$_{ m jazz}$	met	pop	punk	rap	rock
0	1822	1.25	1.13	1.54	1.37	1.50	0.76	1.31	1.13	1.10
1	136	1.28	1.55	1.28	2.35	0.78	0.73	0.64	1.35	0.70
2	664	0.59	0.87	0.98	0.48	0.95	0.97	1.50	1.20	1.19
3	482	1.26	1.16	1.09	1.12	0.91	0.80	2.48	1.24	0.89
4	973	1.14	1.20	1.15	1.41	0.80	0.91	0.66	0.97	0.97
5	512	1.29	0.96	0.95	1.09	1.10	0.97	0.33	1.06	1.01
6	682	0.89	0.79	0.61	0.64	1.13	1.08	1.07	1.08	1.01
7	124	0.75	1.45	0.35	0.64	0	1.09	0	1.02	0.62
8	524	0.93	1.01	1.12	0.91	1.15	1.07	0.43	0.95	0.87
9	937	0.40	0.46	0.19	0.23	0.45	1.56	0.13	0.37	1.06
10	232	0.72	0.57	0.27	0.99	0.38	1.44	0.38	0.46	1.00
11	612	0.74	0.94	0.71	0.40	0.70	1.27	0.07	0.68	0.83
	٠ .	•						0.5		



Jazz:

1 lowest width4 lowest strengthNot easy to be prominent

Pop:

9, 10, 11 Lowest depth, highest strength

Leaders for pop artists are embedded in groups of users very engaged with the new artist, but not prominent among their friends

Punk:

2 high depth, low width and strength Long cascades, exactly the opposite of the pop genre, similar to folk!

Dance:

5 high depth, high width, low strength Dance successes are studied to reach everyone, but in two days nobody remembers anything about them...



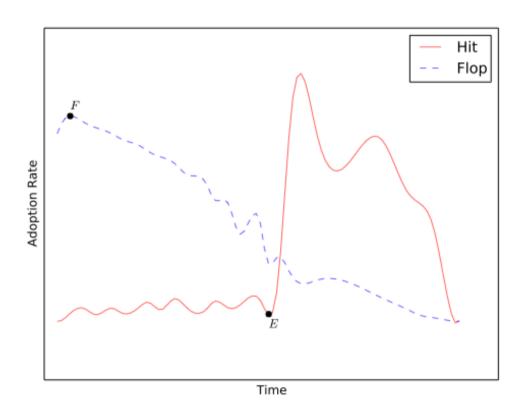
Hits & Flops: qualitative definitions

• Hit

 A good whose trend <u>slowly increases</u> trough time until reaching an <u>explosion point</u> that marks the start of a sharp rising of its adoptions.

Flop

A good whose adoption trend <u>does</u>
 <u>not increase</u> considerably over time
 or even reaches <u>an early maximum</u>
 only to sharply decrease.



Given a **partial observation** of the **adoptions** of a **novel good** can we decide if it will became an **Hit** or a **Flop**?

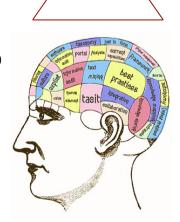
Hit&Flop: Workflow

Measuring Adopters' propensity Toward or Hits/Flops

La Conoscenza Sociale

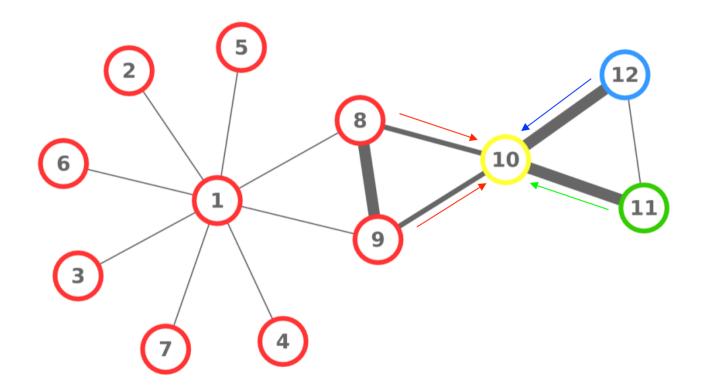


Quello che possiamo Contenere nel nostro cervello E' una minima frazione Della conoscenza umana



Ma le nostre connessioni sociali Contengono ognuna un'altra parte E la loro somma puo' essere significat Come valutare, quindi, una persona?

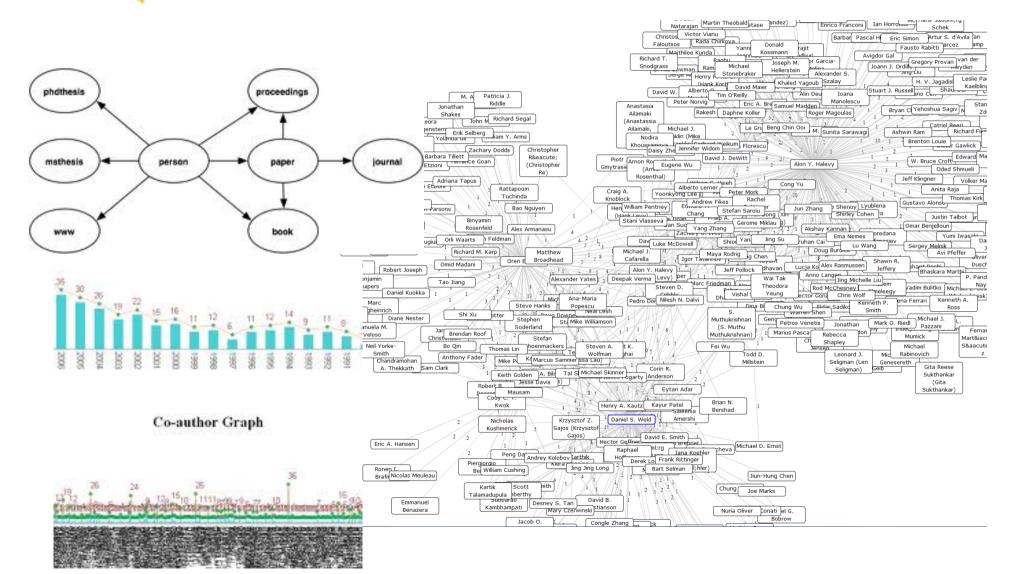
Calcolare la propria conoscenza sociale



Con processi di diffusione su reti possiamo quantificare l'ammontare di "skill" che ogni connessione ci permette di accedere



Le pubblicazioni di 40.000 ricercatori in DataBase & DataMining per 30 anni



Decision-based diffusion models

Herding

[Banerjee 2002]

Herding

- Influence of actions of others
 - Model where everyone sees everyone else's behavior
- Sequential decision making
 - Example: Picking a restaurant
 - Consider you are choosing a restaurant in an unfamiliar town
 - Based on Yelp reviews you intend to go to restaurant A
 - But then you arrive there is no one eating at A but the next door restaurant B is nearly full
 - What will you do?
 - Information that you can infer from other's choices may be more powerful than your own

Herding:

- There is a decision to be made
- People make the decision sequentially
- Each person has some private information that helps guide the decision
- You can't directly observe private information of the others but can see what they do
 - You can make inferences about the private information of others

Herding experiment

- Consider an urn with 3 marbles. It can be either:
 - Majority-blue: 2 blue, 1 red, or
 - Majority-red: 1 blue, 2 red
- Each person wants to best guess whether the urn is majority-blue or majority-red
 - Guess red if P(majority-red | what she has seen or heard) > ½
- Experiment: One by one each person:
 - Draws a marble
 - Privately looks are the color and puts the marble back
 - Publicly guesses whether the urn is majority-red or majority-blue
- You see all the guesses beforehand. How should you make your guess?

State of the world:

Whether the urn is MR or MB

Payoffs:

Utility of making a correct guess

Signals:

- Models private information:
 - The color of the marble that you just draw
- Models public information:
 - The MR vs MB guesses of people before you

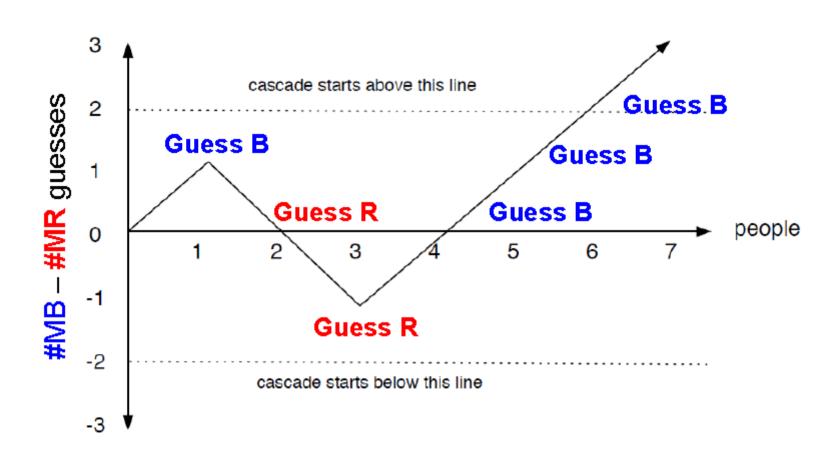
Sequential decision making

- **Decision:** Guess MR if $P(MR|past\ actions] > \frac{1}{2}$
- Analysis (Bayes rule):
 - #1 follows her own color (private signal)!
 - Why? $P(MR | \mathbf{r}] = \frac{P(MR)P(r | MR)}{P(r)} = \frac{1/2 \cdot 2/3}{1/2} = 2/3$ $P(r) = P(r | MB)P(MB) + P(r | MR)P(MR) = \frac{1}{2} \frac{1}{3} + \frac{1}{2} \frac{2}{3} = 1/2$
 - #2 guesses her own color (private signal)!
 - #2 knows #1 revealed her color. So, #2 gets 2 colors.
 - If they are the same, decision is easy.
 - If not, break the tie in favor of her own color

Sequential decision making

- #3 follows majority signal!
 - Knows #1, #2 acted on their colors. So, #3 gets 3 signals.
 - If #1 and #2 made opposite decisions, #3 goes with her own color. Future people will know #3 revealed its signal $P(MR \mid r, r, b] = 2/3$
 - If #1 and #2 made same choice, #3's decision conveyed no info. Cascade has started!
- How does this unfold? You are N-th person
 - #MB = #MR : you guess your color
 - |#MB #MR|=1 : your color makes you indifferent, or reinforces you guess
 - |#MB #MR| ≥ 2 : Ignore your signal. Go with majority.

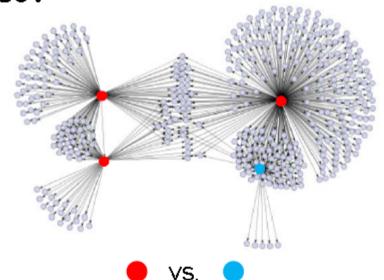
Cascade begins when the difference between the number of blue and red guesses reaches 2



Influence maximization

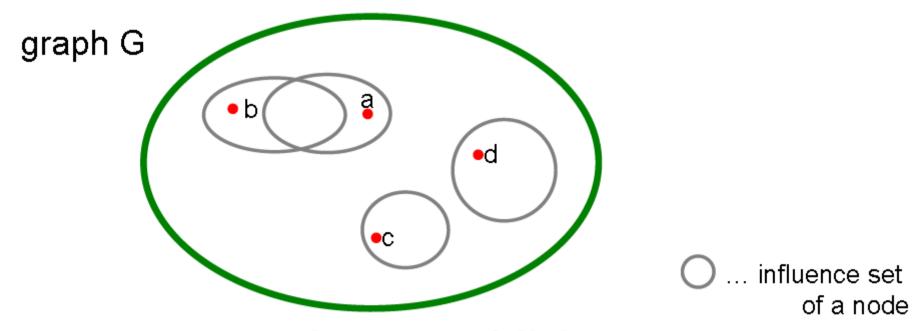
How to create big cascade?

- Blogs Information epidemics
 - Which are the influential/infectious blogs?
 - Which blogs create big cascades?
- Viral marketing
 - Who are the influencers?
 - Where should I advertise?
- Disease spreading
 - Where to place monitoring stations to detect epidemics?



Most influential sets of nodes

- S: is initial active set
- f(S): the expected size of final active set

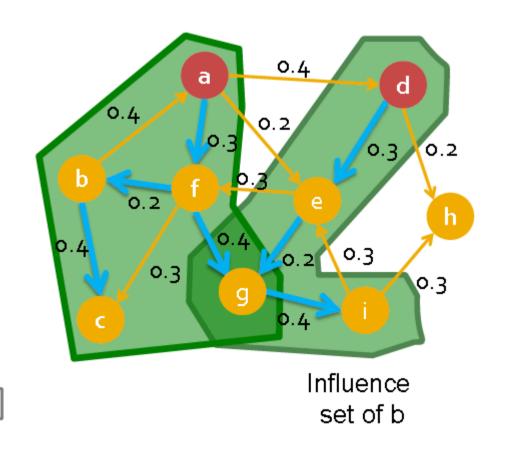


Set S is more influential if f(S) is larger f({a,b} < f({a,c}) < f({a,d})</p>

Most influential sets of nodes

Problem:

• Most influential set of size k: set S of k nodes producing largest expected cascade size f(S) if activated [Domingos-Richardson '01]



- Optimization problem: $\max_{S \text{ of size } k} f(S)$

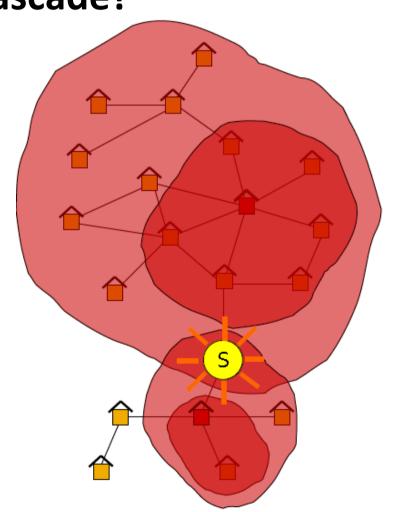
How hard is the problem?

- NP-HARD!
- But if f(S) is «diminishing returns»
 - Monotonic and submodular
- Then the approximated solution computed with a greedy algorithm (hill climbing) has a bounded distance with the global optimum!

Related problem: outbreak detection

Which node(s) initiated a cascade?

- Given a real city water distribution network
- And data on how contaminants spread in the network
- Detect the contaminant as quickly as possible



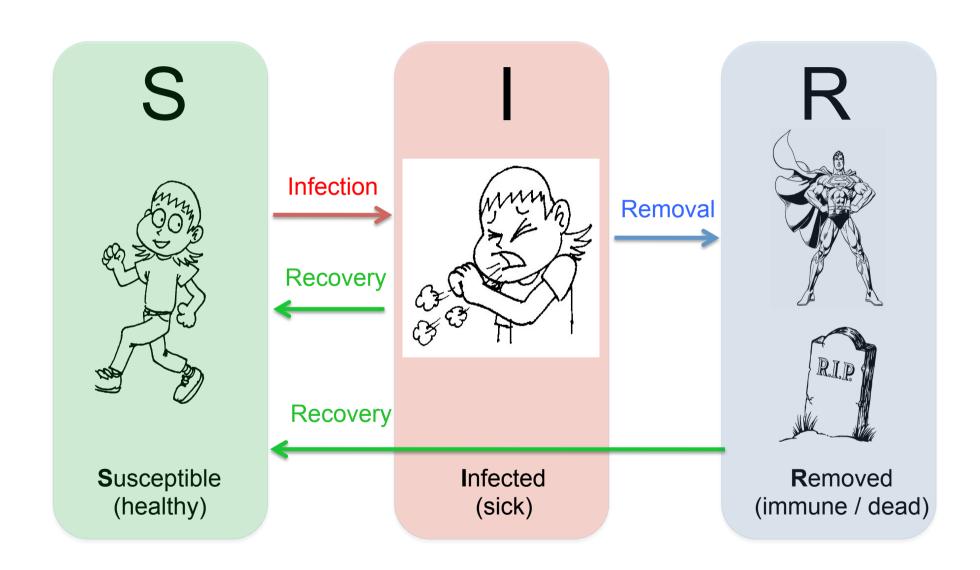
Probabilistic models of diffusion

Epidemic modeling

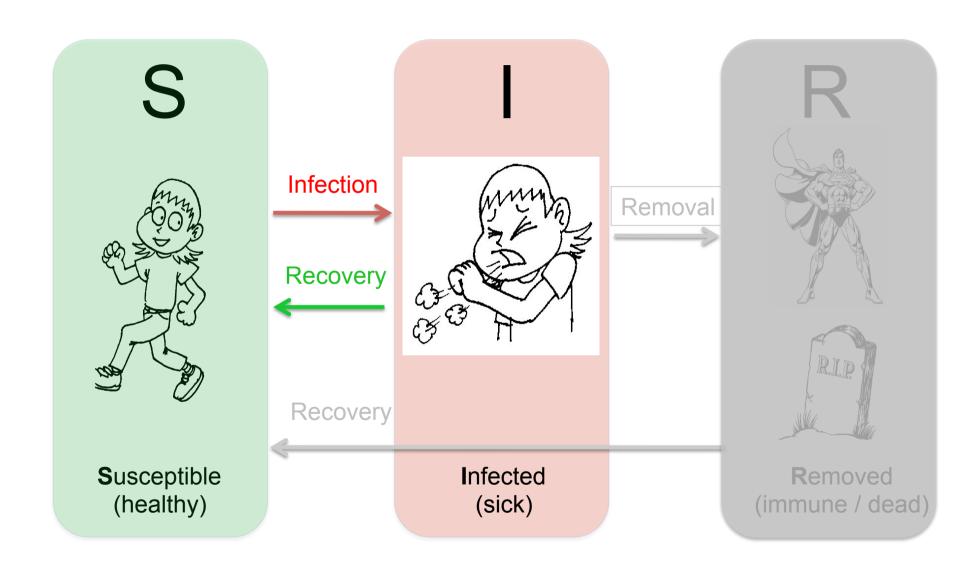
Classical Models of Epidemics

Epidemic Modeling (classical models)

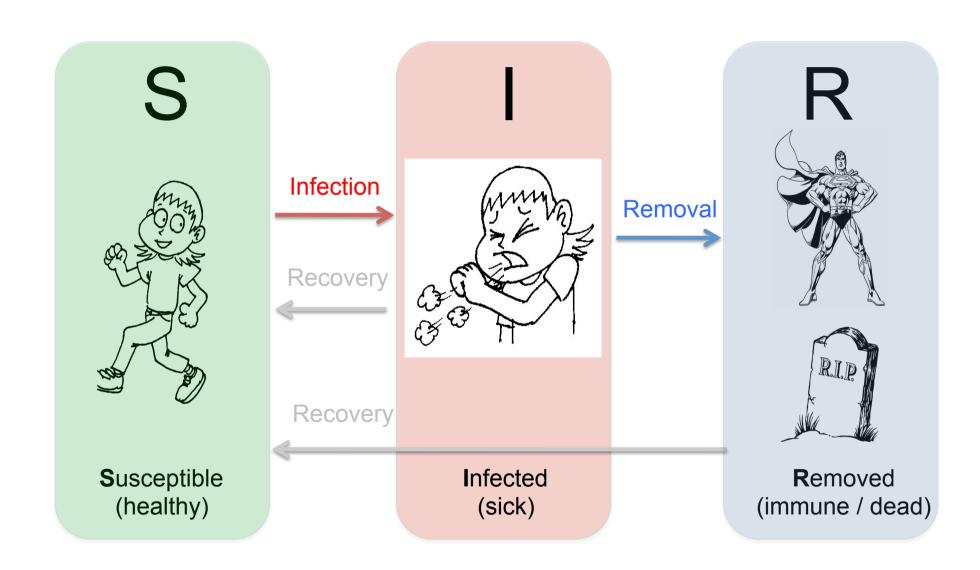
Classical Epidemic Models – Basic States



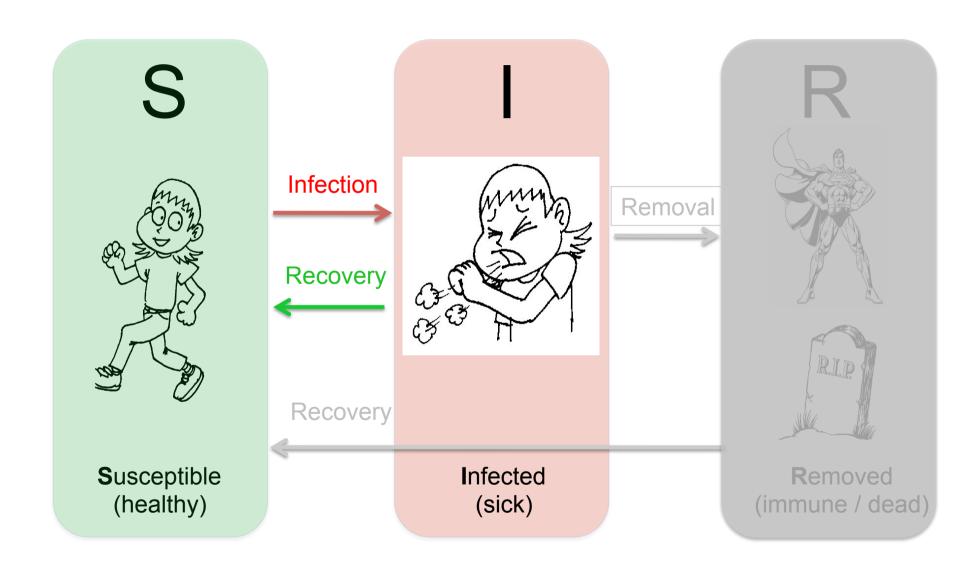
SIS Model: Common Cold



Example 2: Flu, SARS, Plague, ...



SIS Model: Common Cold



SIS Model Dynamics

$$\frac{di}{dt} = \beta i(1-i) - \mu i = i(\beta - \mu - \beta i)$$

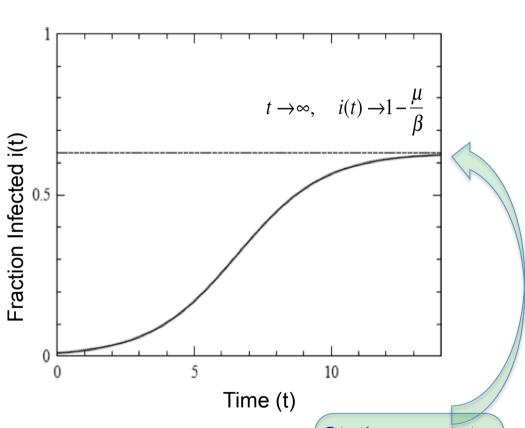
$$\overline{||} S \overline{||} > S$$

$$\frac{di}{i} + \frac{di}{1 - \mu/\beta - i} = (\beta - \mu)dt$$

$$\ln(i) - \ln(1 - \mu/\beta - i) = (\beta - \mu)t + c$$

$$\frac{i}{1-\mu/\beta-i} = Ce^{(\beta-\mu)t} \qquad C = e^c$$

$$\therefore i(t) = \left(1 - \frac{\mu}{\beta}\right) \frac{Ce^{(\beta - \mu)t}}{1 + Ce^{(\beta - \mu)t}}$$



Stationary state:

$$\frac{di}{dt} = \beta i (1 - i) - \mu i = 0$$

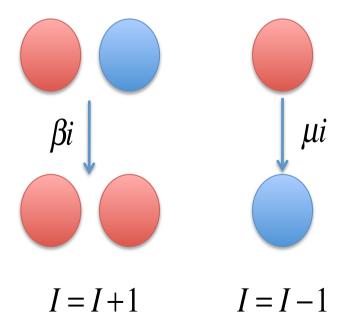
SIS model: fraction infected individuals saturates below 1.

SIS Model: Epidemic Threshold and Basic Reproductive Number

$$\frac{di}{dt} = \beta i (1 - i) - \mu i$$

If
$$\mu \approx \beta$$
, $i \rightarrow 0$

"Epidemic threshold"



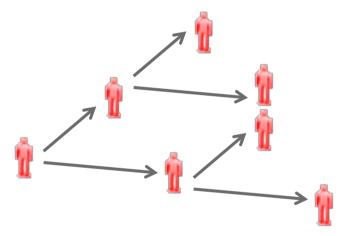
$$\lambda \equiv \frac{\beta}{\mu}$$
 "Basic reproductive number"

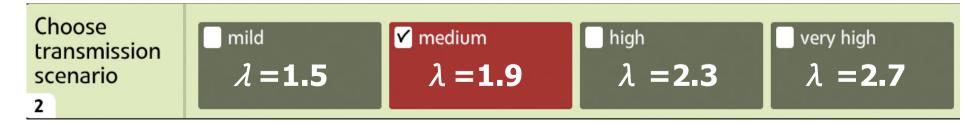
On average, how many infected individuals will be infected by one infected individual?

 $\lambda > 1$: Outbreak, $\lambda < 1$: Die out

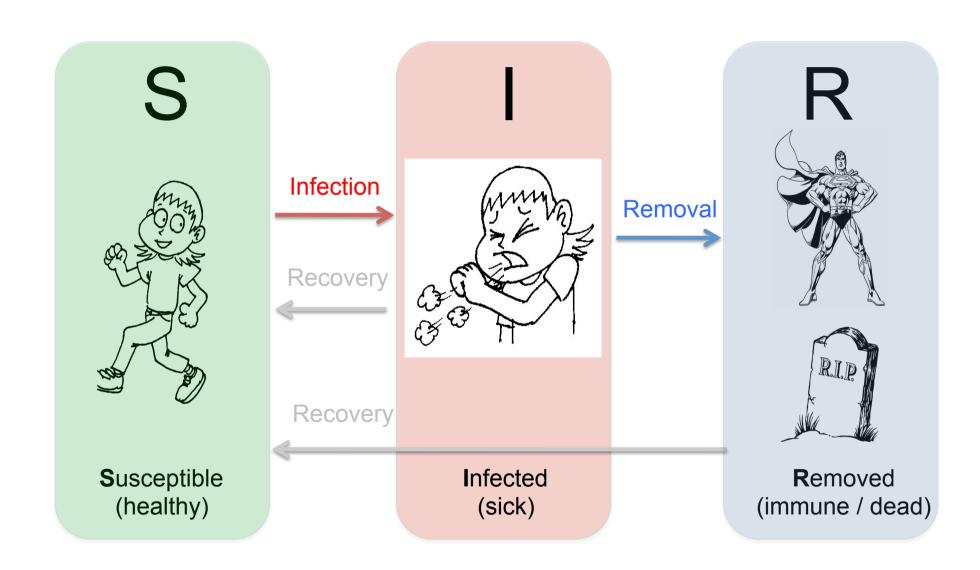
reproductive number λ : average # of infectious individuals generated by one infected in a fully susceptible population.

e.g.
$$\lambda = 2$$





Example 2: Flu, SARS, Plague, ...

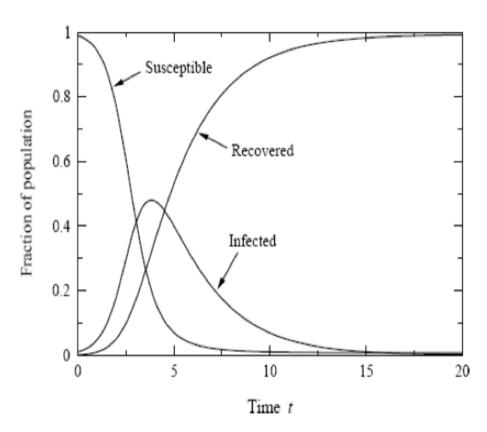


SIR Model

$$\frac{\mathrm{d}s(t)}{\mathrm{d}t} = \beta \langle k \rangle i(t) \left[1 - r(t) - i(t) \right]$$

$$\frac{\mathrm{d}i(t)}{\mathrm{d}t} = -\mu i(t) + \beta \langle k \rangle i(t) \left[1 - r(t) - i(t) \right]$$

$$\frac{\mathrm{d}r(t)}{\mathrm{d}t} = \mu i(t).$$



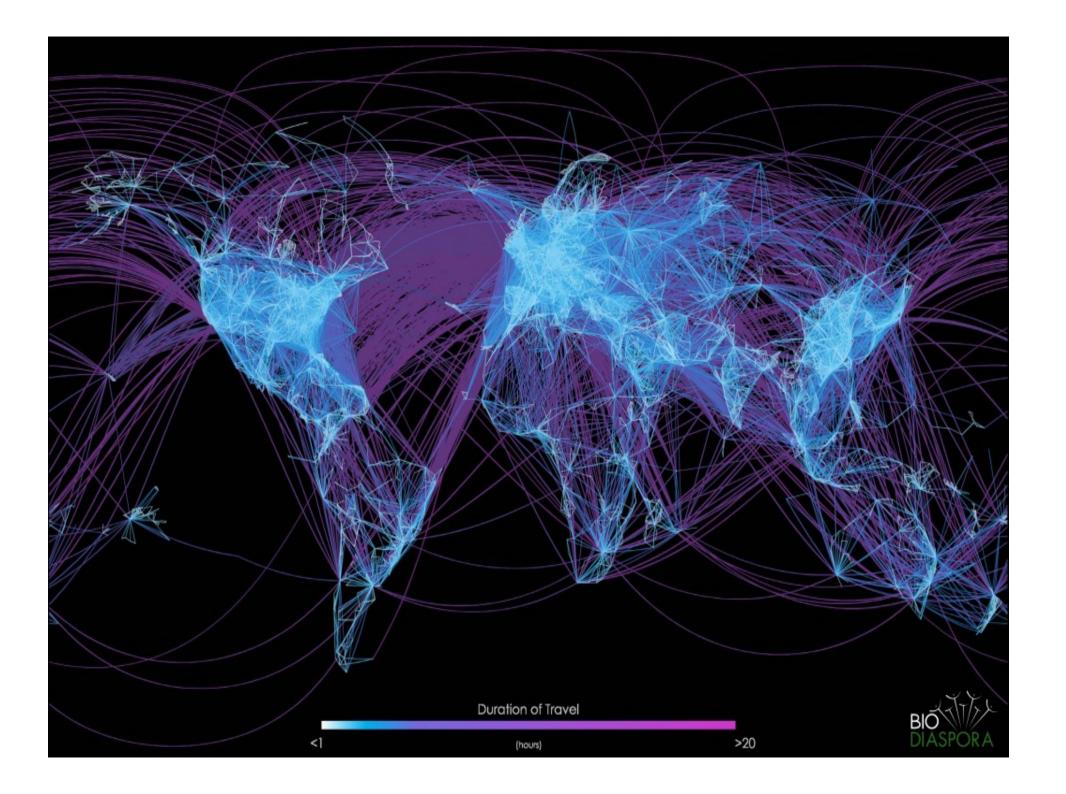
 SIR model: the fraction infected peaks and the fraction recovered saturates.

Epidemic modeling on networks

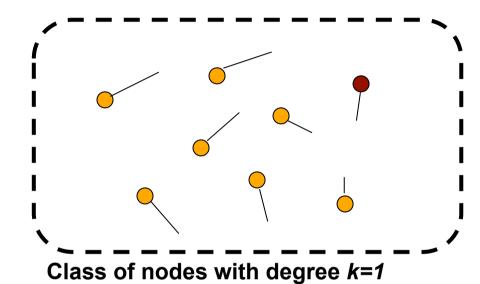
[Vespignani et al., since 2002]

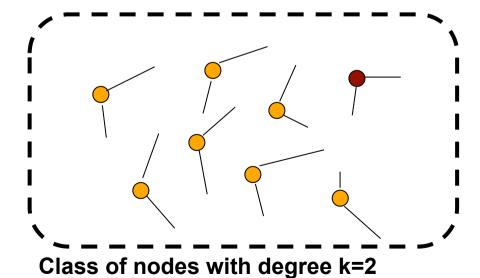
Gleamviz





SIS model on a network: Degree based representation





Split nodes by their degrees

$$i_k = \frac{I_k}{N_k}, \quad i = \sum_k P(k)i_k$$

SIS model:

$$\frac{di_k(t)}{dt} = \beta(1 - i_k(t))k\Theta_k(t) - \mu i_k(t)$$

Proportional to k

Density of infected neighbors of nodes with degree *k*



I am susceptible with k neighbors, and $\Theta_k(t)$ of my neighbors are infected.

(Vespignani)

Early time behavior – SI model – the characteristic time vanishes!

$$\tau = \frac{\langle k \rangle}{\beta (\langle k^2 \rangle - \langle k \rangle)}$$

 $\tau = \frac{\langle k \rangle}{\beta (\langle k^2 \rangle - \langle k \rangle)}$ The timescale it takes for an epidemics to grow. The smaller is τ the factor if

$$\tau_{ER} = \frac{1}{\beta \langle k \rangle}$$

→ The more connected the network is. the faster does the epidemic spread.

SF network (y<3):

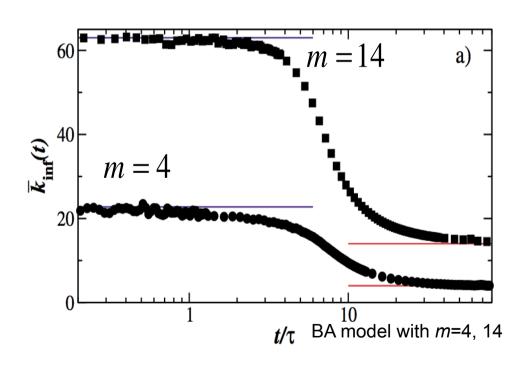
$$\langle k^2 \rangle \rightarrow \infty$$
 for $N \rightarrow \infty \rightarrow \tau \rightarrow 0$

For heterogeneous networks, the characteristic time vanishes, which means that the epidemic becomes instantaneous. The reason: the hubs get infected first, which then rapidly reach most nodes.

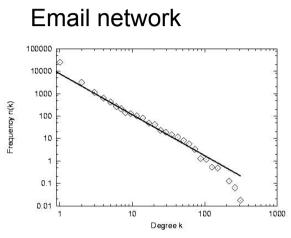
Numerical Test:

The average degree of newly infected nodes at time t:

$$\overline{k}_{inf}(t) = \frac{\sum_{k} k \left(I_k(t) - I_k(t-1) \right)}{I(t) - I(t-1)}$$

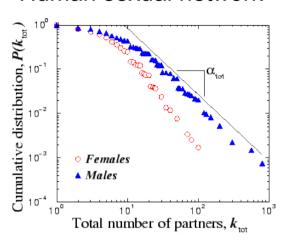


SIS Model – Absence of Epidemic Threshold



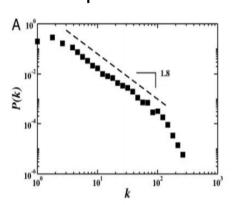
Ebel et al. (2002)

Human sexual network



Lilijeros et al., Nature (2001), Schneeberger et al. STD (2004)

Air transportation network



Colizza et al., PNAS 2006

Many networks will have small or vanishing epidemic threshold!



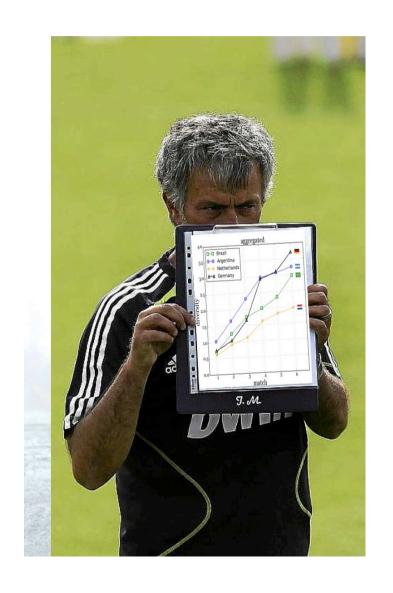
Research highlights

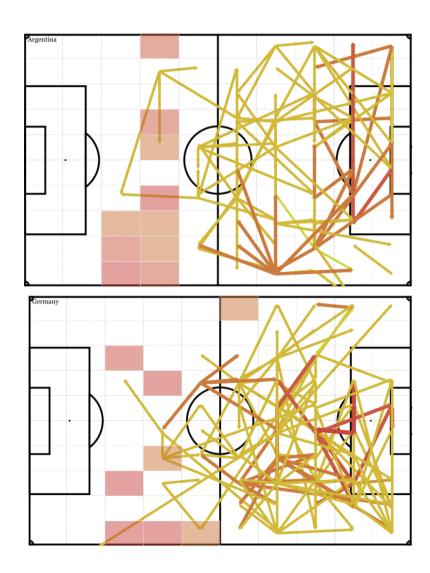
Networks & Sport Data Mining

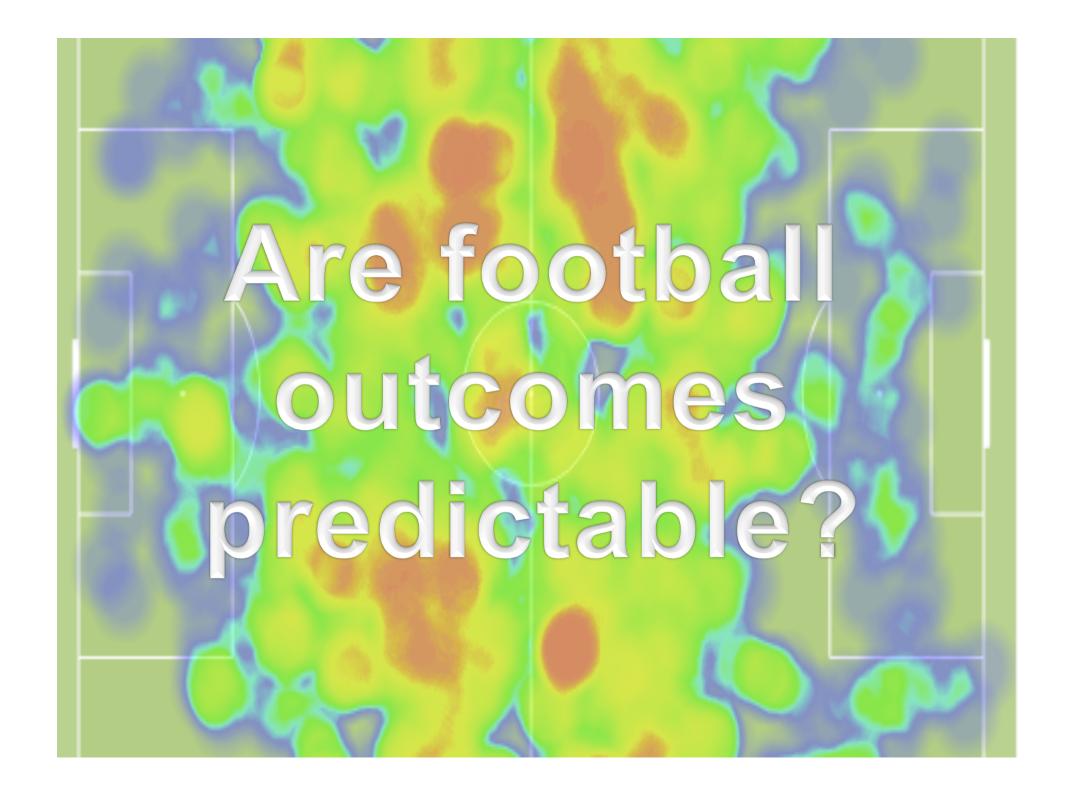
[Cintia, Pappalardo et al at KDD LAB]

The patterns of success in football

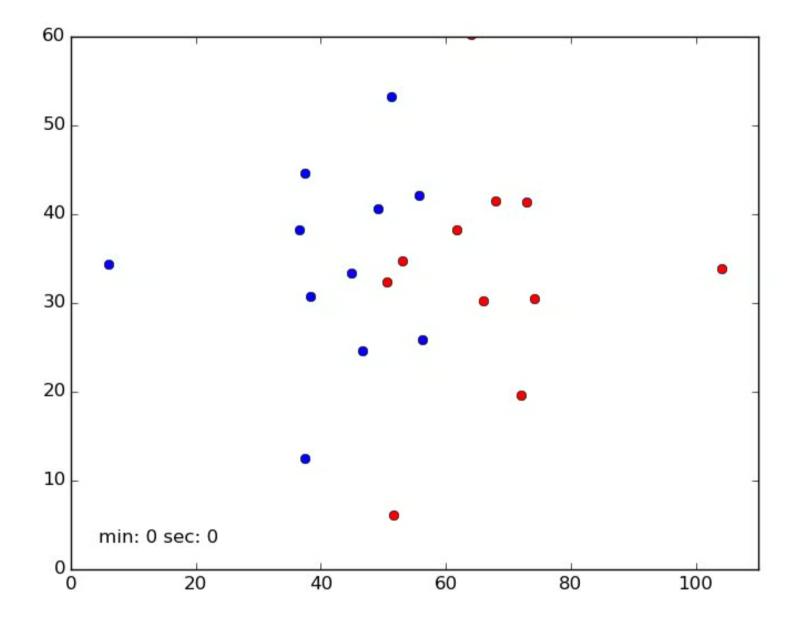
"Football is a simple game: 22 men chase a ball for 90 minutes and at the end, the Germans always win" -- Gary Lineker (after Italy 1990 Final)



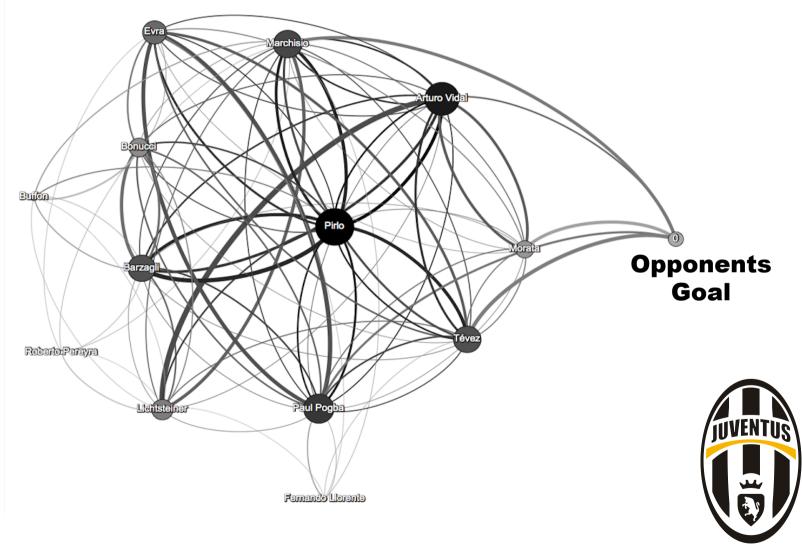




Data from each single match <tackle, 15.4, 41.1, 112> <pass, 25.0, 67.1, 113> <pass,65.0,87.1,115> <assist,82.1,35.8,120> <goal attempt,82.1,35.8,121>

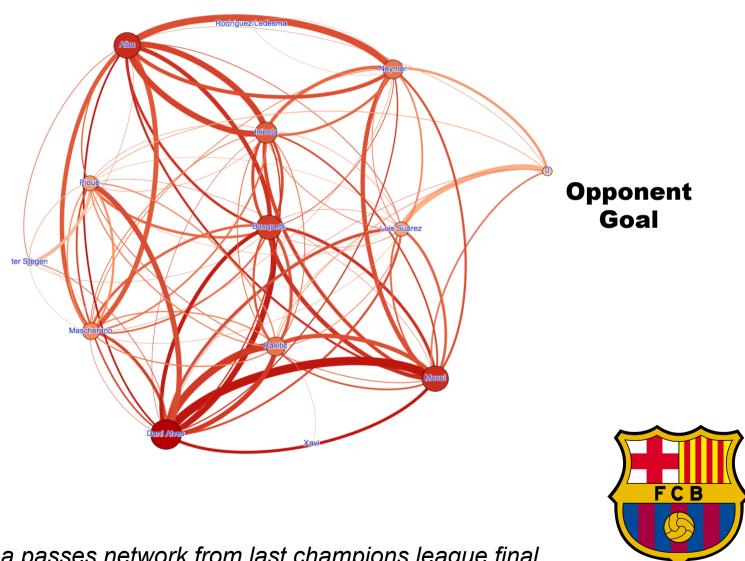


Football As a network



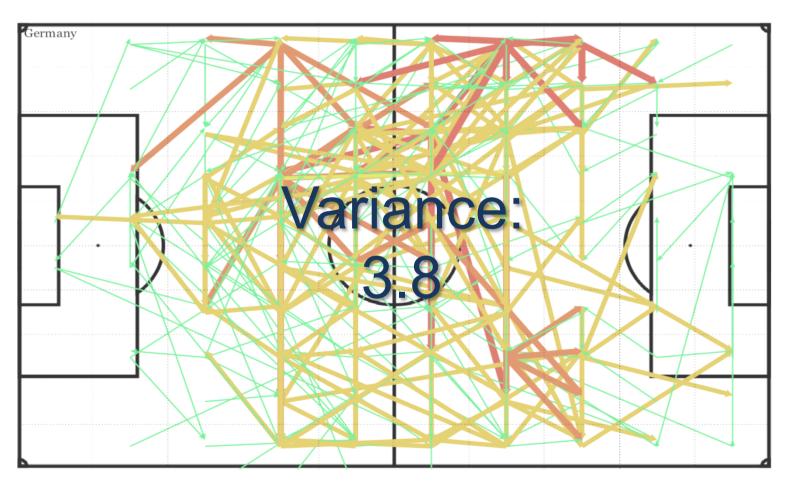
Juventus passes network from last champions league final

Enathall as a Notwork



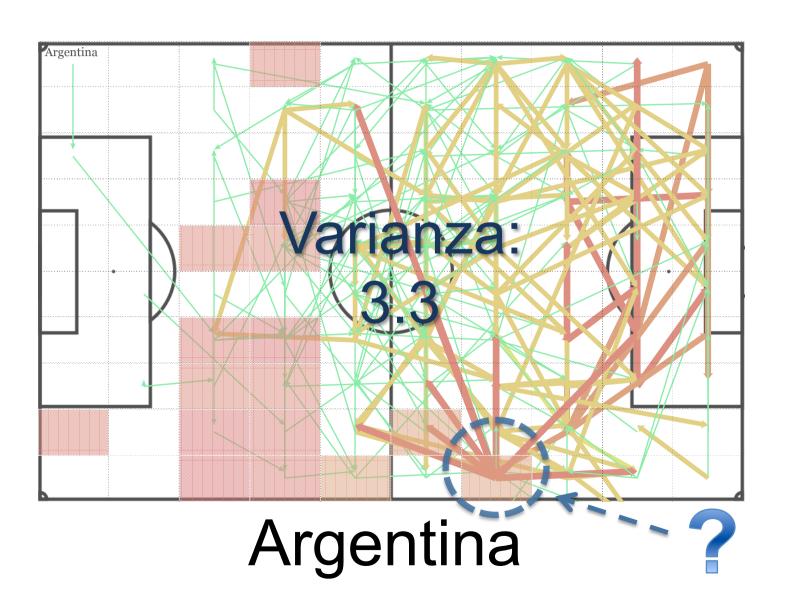
Barcelona passes network from last champions league final

The passes network among zones



Germany

The passes network among zones

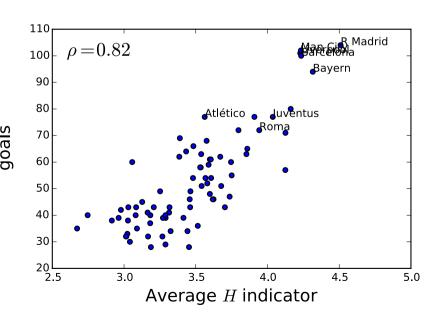


Network analysis for performance

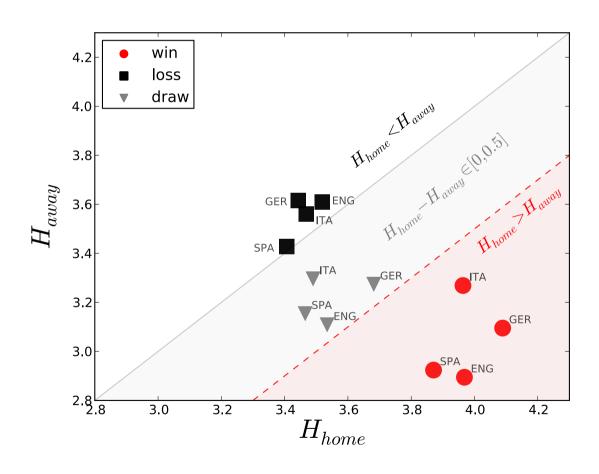
• Networks characteristics as up to proper performance evaluation and outcome prediction

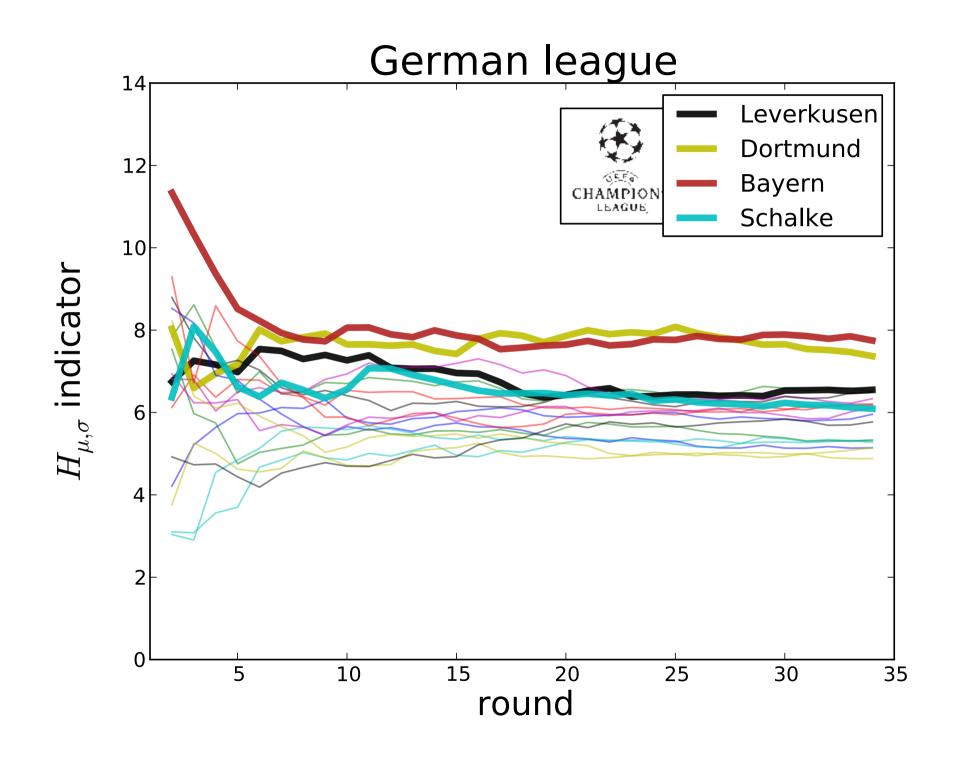
measure	description	
w	total passing volume	
μ_p	μ_p mean players' passing volume σ_p variance of players' passing volume	
σ_p		
μ_z	mean zones' passing volume	
σ_z	variance of zones' passing volume	
H	combination of above measures	

The harsh rule of the goals": Big Data analytics and football team success
Paolo Cintia, Luca Pappalardo, Dino Pedreschi,
Fosca Giannotti and Marco Malvaldi
2015 IEEE/ACM Int. Conf. on Data Science and
Advanced Analytics (DSAA'2015)



Predicting game outcomes





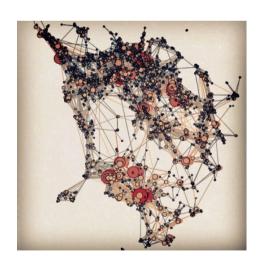


simulated ranking		real ranking	
Bayern	91	Bayern	90
Leverkusen	72	Dortmund	71
Dortmund	68	Schalke	64
Wolfsburg	59	Leverkusen	6 1
Augsburg	58	Wolfsburg	60
Hoffenheim	49	Mönchengladbach	55
Hertha	49	Mainz	53
Mainz	48	Augsburg	52
Schalke	47	Hoffenheim	44
Frankfurt	46	Hannover	42
Mönchengladbach	42	Hertha	41
Hannover	41	Werder	39
Hamburg	38	Freiburg	36
Stuttgart	35	Frankfurt	36
Freiburg	31	Stuttgart	32
Werder	24	Hamburg	27
Braunschweig	22	Nürnberg	26
Nürnberg	17	Braunschweig	25



We are the champions – understanding the patterns of success in football

P.Cintia, L. Pappalardo, F. Simini Kdd Lab ISTI CNR Pisa – University of Pisa – University of Bristol www.kddlab.isti.cnr.it



Big Data Tales

Adventures in data www.bigdatales.com



@bigdatatales

Analysing and mining the retail market as a complex system

Michele Coscia, Fosca Giannotti, Mirco Nanni, Dino Pedreschi, Diego Pennacchioli, Salvatore Rinzivillo

KDDLab ISTI-CNR & University of Pisa IMT Lucca, CID Harvard University











Supermarket transaction data

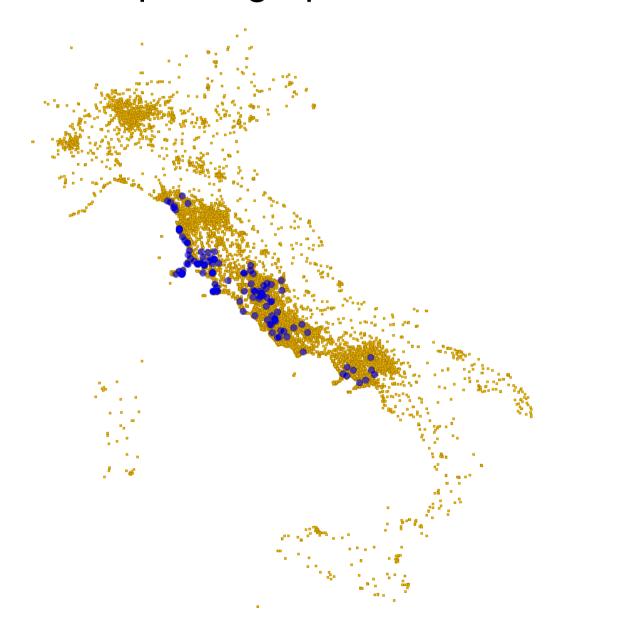
- 1,066,020 customers
- 345,208 products
- 138 stores in 4 Italian regions
- Since January 1st, 2007

MISSION (extract):

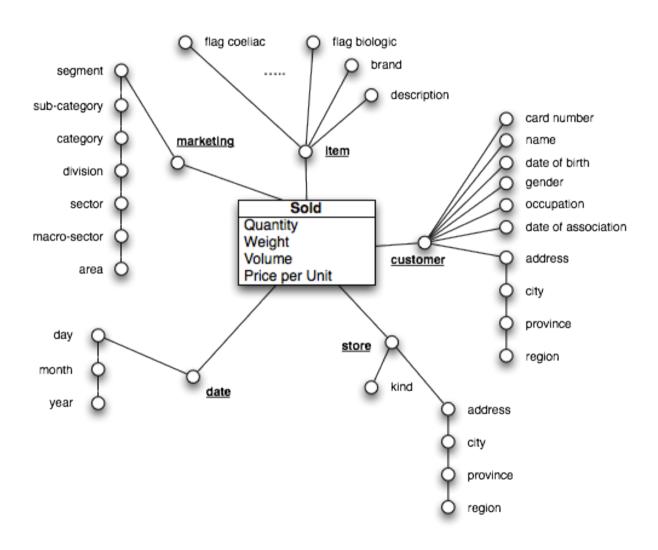
- defend the family budget, offering quality goods and services at the best condition
- promote the spirit of solidarity among customers, employees and their families, offering for their free time socially useful initiatives
- protect health and safety of consumers
- help developing Nations and weaker social categories. even through Fair



Customer/shop Geographical Distribution



Data Model



7,003 marketing segments

The retail market as an ecosystem

Coscia, Pennacchioli, Giannotti, Pedreschi, Rinzivillo EPJ Data Science 2014

Data Selection

- Data from 2007-2009 (period 2009-2011 used as control)
- Only the customers from Livorno
- We aggregate products to their marketing Segment
- We clean not sold or meaningless products
- We fill a 317,269 customers X 4,817 products with the amount purchased (182,821,943)

Census (2011)	343K
registered	212K
At least once	146K
Actives 07-11	102K
Actives 2011	77K

343K / 77K = 4.45 (2.5 persons x family in AVG) [ISTAT]

Data Preparation

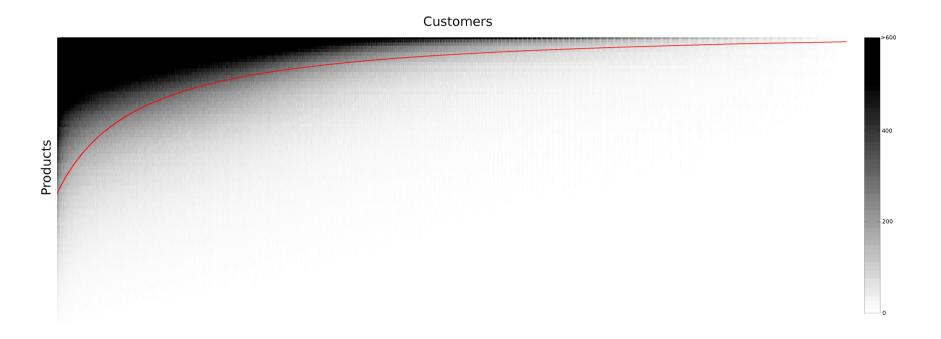
 Sort rows and columns according to their sum

$$lift(X, Y) = \frac{supp(X, Y)}{supp(Y) \times supp(X)}$$

$$M_{cp} = \begin{cases} 1 & \text{if } \text{lift}(c_j, p_i) > 1; \\ 0 & \text{otherwise.} \end{cases}$$

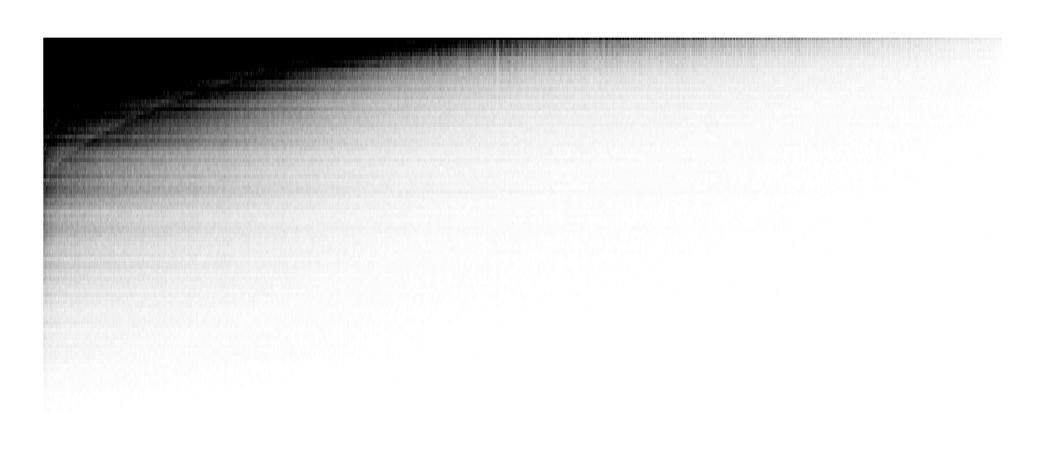
• 37,338,591 ones (2.4431697% fill)

The Retail Purchase Matrix



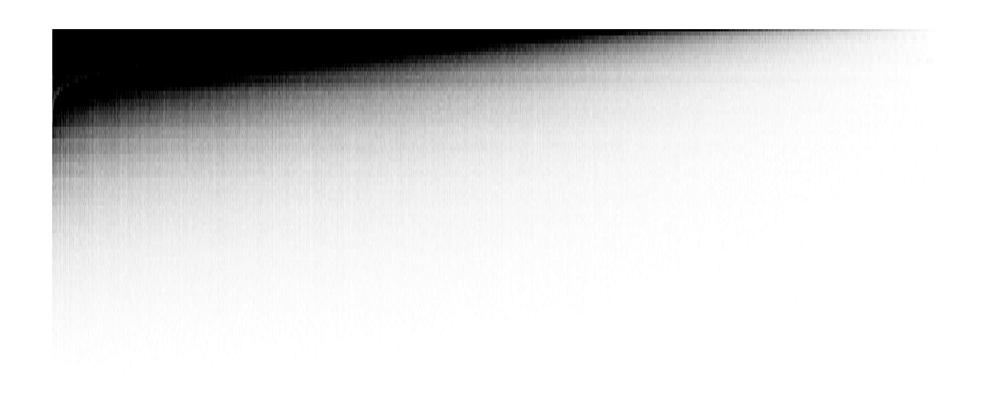
- There are products bought by everyone
- There are customers buying everything
- The volume of sales of a product is identifying who is buying it
- ... is this phenomenon robust?

Total Price instead of Amount of Items

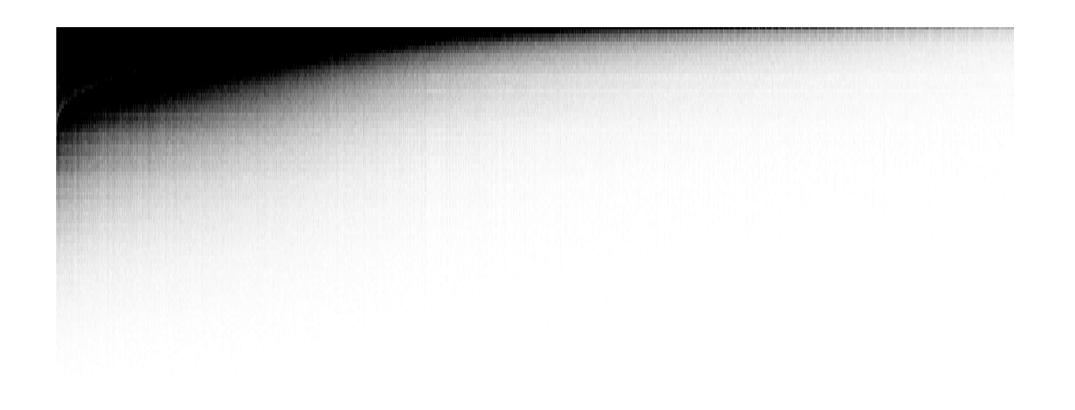


Category instead of Segment

Lazio matrix



Livorno 2009-2011



Null Hypothesis

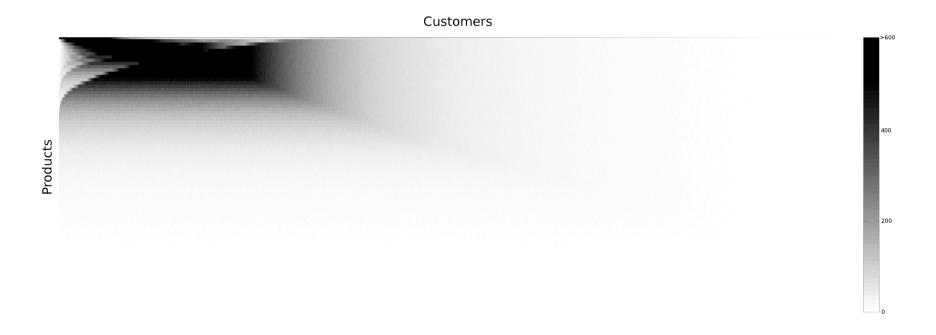
Given the volume of sales of products, and the quantity of products bought by customers, the nestedness of the matrix is inevitable even in a random world where there is no relation between products and customers

Null Model

- The purchases are distributed randomly;
- Customers preserve the total amount of their purchases;
- Each product preserves its sale volume

 We randomize the matrix by preserving the sums of columns and rows

Null Model Matrix



Retail Purchase Law

Average of the one-density at the left of the isocline and zero-density at the right of the isocline $N(M_{c,p},f_*) = \frac{1}{2}(\frac{f_l(M_{c,p},1)}{f_l(M_{c,p},*)} + \frac{f_r(M_{c,p},0)}{f_r(M_{c,p},*)})$

f_*	$N(M_{c,p}, f_*)$
ax + b	0.616106811666
$ax^2 + bx + c$	0.628533747603
$a\log(x) + b$	0.623911138356
ax^b	0.572996769269
$\frac{a}{x}$	0.609588181022
$-\frac{ax+b}{cx+d}$	0.632547410976

$$\alpha j + \beta i + \gamma i j + \delta = 0$$

$$i = -\frac{\alpha j + \delta}{\gamma j + \beta}, \ j = -\frac{\beta i + \delta}{\gamma i + \alpha}$$

$$\alpha = 2342.5757, \ \beta = 14.4349, \ \gamma = 0.0720, \ \delta = -5535548$$

Product Relationships

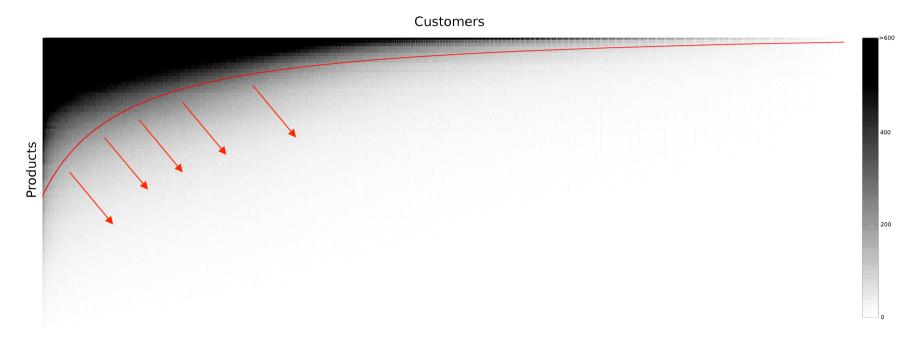
- Before: A => B, association rule
- A and B co-appears unexpectedly X times, therefore they are related
- Now: we introduce an ecology approach
- If product B is directly dependent of A's ecosystem, then A and B are related

Product Relationships

p_i	p_{i-1}	$P(p_i)$	$P(p_i p_{i-1})$
Dishwasher Salt	Dishwasher Soap	8.39%	30.41%
Asparagus	Olive	8.00%	26.12%
Peppers	Chicory	7.31%	23.73%
Canned Soup	Preserved Anchovies	9.96%	32.23%
Wafers	Sugar Candies	11.30%	21.67%

$$\frac{P(p_i|p_{i-1})}{P(p_i)}$$
 = 1.993 in avg

Identifying the "willing customer" set



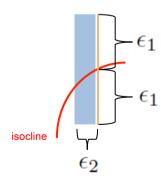
- We select the customers on the isocline: how many of them are willing to buy p?
- How many random customers we need to select without the isocline to have a set of the same size?

Product Relationships

p_i	$ TC^* $	TC	$\frac{ TC_r }{ TC }$
Tomino Cheese	58	137	7.51095
Raw Ham	78	144	5.81250
Apricot Jam	66	127	4.66142
Anchovies	83	144	4.06250

$$TC j - \epsilon_1 \le j' \le j + \epsilon_1 and M_{cp}(c_j, p_i) \ne 1$$

$$TC^* \quad \exists x, M_{cp}(tc, p_x) = 1 \text{ with } i - \epsilon_2 \le x < i$$



by fixing $\epsilon_1 = 100$ and $\epsilon_2 = 2$ averages of the $\frac{|TC_r|}{|TC|}$ ratio is 3.55594.

The hierarchy of Needs

- What are the most basic products?
- What are the most sophisticated products?
- Not only biggest volume sales or higher prize
- To be basic, p should be bought by the least "complex" customers
- To be sophisticated, p should be bought by the customers with more sophisticate need

The product sophistication

- we calculate the sums of the purchase matrix for each product and customer
- we need to correct these sums recursively: we need to calculate the avg level of sophistication of the customers' needs by looking at the avg sophistication of the products that they buy, and then use it to update the avg sophistication of these products
- so, we take the eigenvector associated with the second largest eigenvalue (that is associated with the variance in the system) [HITS variation]

Product Sophistication

Correct the ubiquity of a product

With the complexity of customers buying it

That needs to be recursively corrected

With the ubiquity of the products they buy

It is equivalent to the eigenvector Of the corrected matrix

$$k_{N,p} = \frac{1}{k_{0,p}} \sum_{c} M_{cp} k_{c,N-1}$$

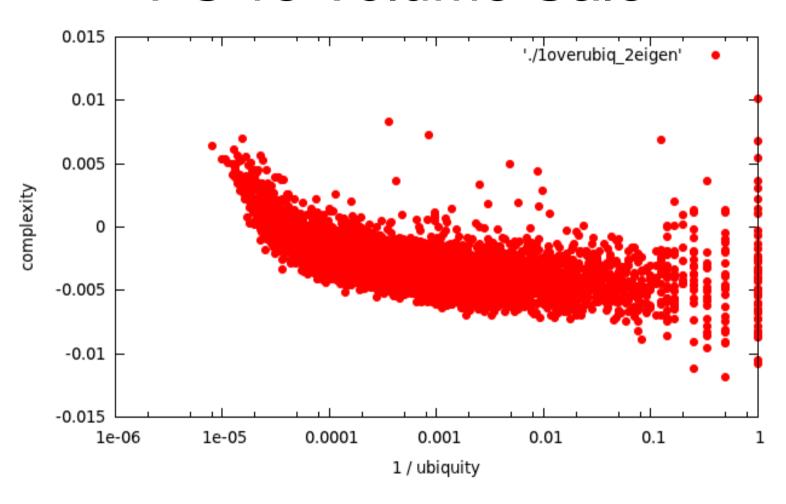
$$k_{N,p} = \frac{1}{k_{0,p}} \sum_{c} M_{cp} \frac{1}{k_{c,0}} \sum_{p'} M_{cp'} k_{N-2,p'}$$

$$k_{N,p} = \sum_{p'} k_{N-2,p'} \sum_{c} \frac{M_{cp} M_{cp'}}{k_{0,p} k_{c,0}}$$

$$k_{N,p} = \sum_{p'} \widetilde{M}_{pp'} k_{N-2,p'}$$

$$\widetilde{M}_{pp'} = \sum_{c} \frac{M_{cp} M_{cp'}}{k_{0,p} k_{c,0}}$$

PS vs Volume Sale



Least and Most Sophisticated Products

p_i	PS
Regular Bread	-4.41
Natural Still Water	-4.19
Yellow Nectarines (Peaches)	-3.84
Semi-Skimmed Fresh Milk	-3.81
Bananas	-3.53

p_i	PS
LCD 28"/30" Televisions	2.91
DVD Music Compilations	2.86
Sauna clothing	2.66
Jewelry Bracelets	2.53
RAM Memories	2.33

Building the Pyramid

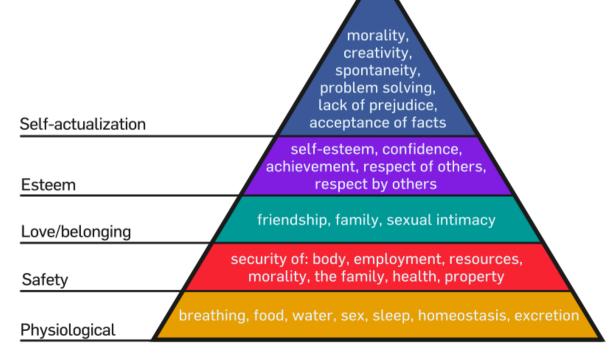
Introduced by Abraham Maslow in 1954

Monodimensional segmentation of the

eigenvector

K-means

• K = 5



The Hierarchy of Needs

Newborn/Child Underwear & Hosiery(22%), Newborn/Child Garments (14%), Cafe Products (7%), Sport (5%), Accessory (4%), Disposable (4%), Childcare (2%)

School & Office Supplies (18%), Toys (7%), Garments for Adults (6%), Pastry (5%), Woman Underwear & Hosiery (4%), Textile (4%), Furnishing (3%), Informatics (3%), Education & Entertainment (3%)

Do-it-yourself (4%), Kitchen Tools (4%), House Cleaning (3%), Plants & Flowers (2%), Man Underwear & Hosiery (2%), Shoes (2%)

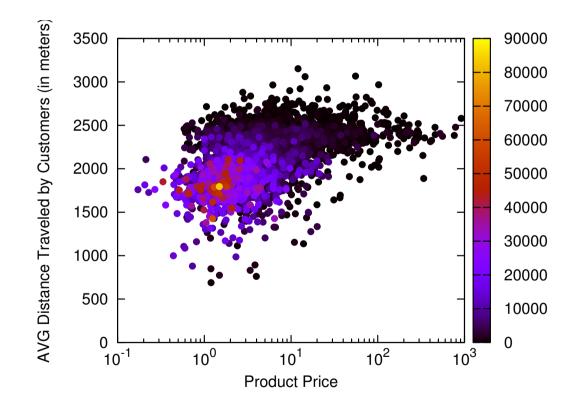
Grocery (20%), Personal Care (10%), Sanitation (8%), Frozen Food (7%), Fish (2%)

Fruit & Vegetables (19%), Fresh Food (17%), Liquids (9%), Bread(7%), Canned Food (7%), Red Meat (6%), Delicatessen (6%), Poultry & Rabbit (2%)

Applicazione spaziale [1]

- each dot is a purchase representative
- if a customer bought products of the same price in different shops, than the distance is weighted with the price

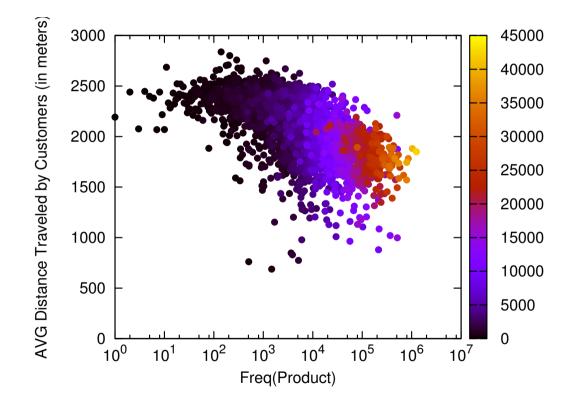
$$d(c_i, p_j) = \sum_{\forall s \in S} \frac{p_j(c_i, s) \times d(c_i, s)}{p_j(c_i, *)}$$



log-normal regression $f(x) = a \log x + b$ $R^2 = 17.25\%$

Applicazione spaziale [1]

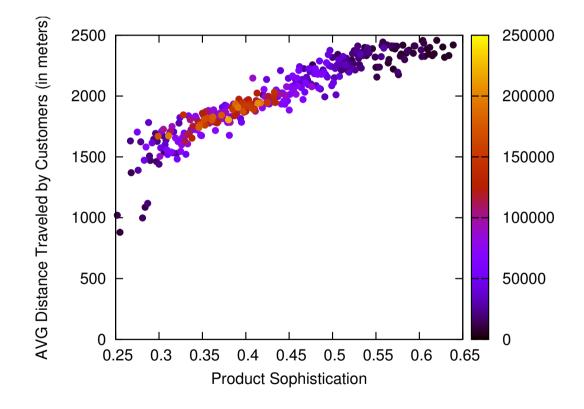
- each dot is a purchase representative
- if a customer bought products of the same frequency in different shops, than the distance is weighted with the frequency



log-normal regression $f(x) = a \log x + b$ $R^2 = 32.38\%$

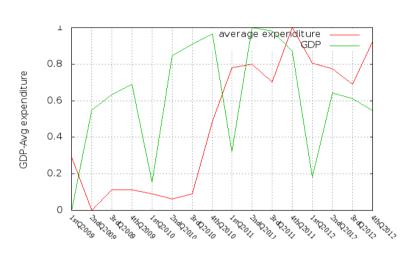
Applicazione spaziale [1]

- each dot is a purchase representative
- if a customer bought products of the same sophistication in different shops, than the distance is weighted with the sophistication

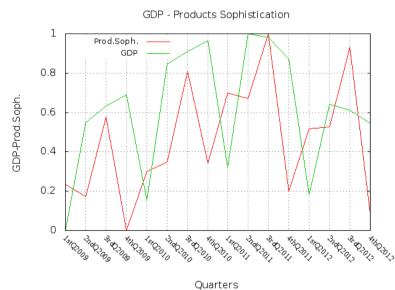


log-normal regression $f(x) = a \log x + b$ $R^2 = 85.72\%$

Misurare il benessere







In prospect ...

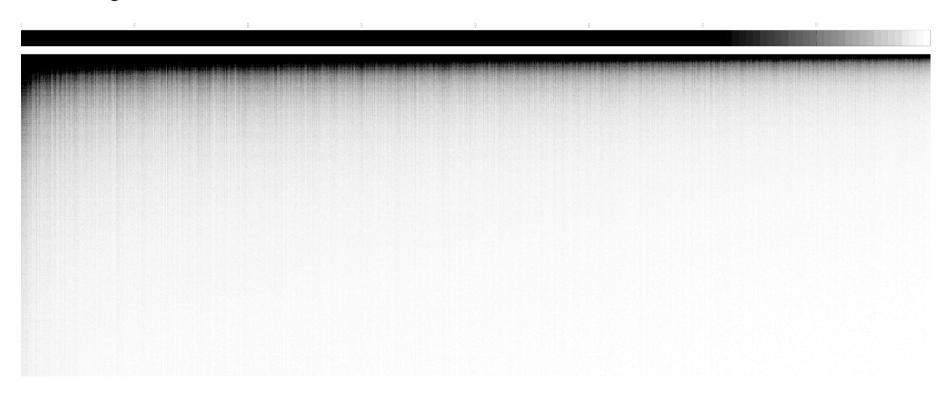
- A novel wave of data driven microeconomics indicators based on retail transaction data
- Measuring and nowcasting indicators using retail transaction data
- A natural convergence between data mining/machine learning and complex system modeling

...and in other domains?

UK LastFM Dataset

Users: 76'866 Artists: 247'311

Listenings: 278'740'507



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 Albert-Laszlo Barabasi. Network Science Book Project <u>http://barabasilab.neu.edu/networksciencebook/</u>

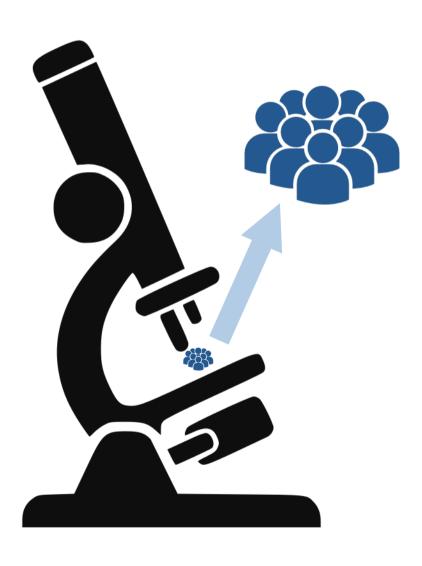
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SNA course @ Università di Pisa

http://didawiki.di.unipi.it/doku.php/wma/start

 Slides from this course are freely adapted from those of Laszlo Barabasi, Jure Leskovec, Fosca Giannotti, besides my own. Thanks!

Big Data Analytics & Social Mining



a tool to measure, understand, and possibly predict human behavior





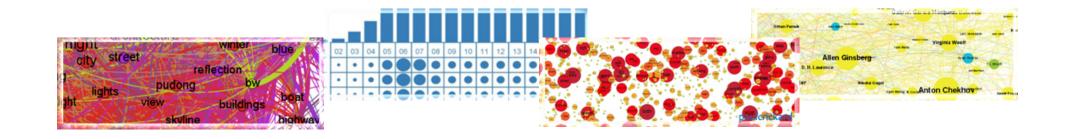
Social Mining & Big Data Analytics

H2020 - www.sobigdata.eu

SoBigData is...



A Multidisciplinary European Infrastructure on Big Data and Social Data Mining providing an integrated ecosystem for ethic-sensitive scientific discoveries and advanced applications of social data mining on the various dimensions of social life, as recorded by "big data".





Social mining a OPEN SCIENCE



- An ecosystem of data, methods and competences for serving the community of researchers and innovators ready to exploit the opportunities of big data and to incorporate it in data-driven science and innovation
- open up new research and innovation avenues in multiple fields, including mathematics, ICT, and human, social and economic sciences, by enabling easy comparison, re-use and integration of state-of-the-art research data, methods, and services, into new research.





The Consortium

























Existing national RI's to be integrated















Activities





















Thematic Clusters





Research Infrastructure



SoBigData



Social Mining & Big Data Ecosystem



Big Data Ecosystem

- Open Data
- Restricted Data
- Virtual Collections

Social Mining

- Text and Social Media Mining
- Social Network Analysis
- Human Mobility Analytics
- Web Analytics
- Visual Analytics
- Social Data

Ethical and Legal Framework

SoBigData

Research Infrastructure



Virtual Access

E-infrastructure



Transnation al Access

Open calls

Exploratory projects



Networking

Training

Dissemination

Innovation Accelerator





SoBigData Access

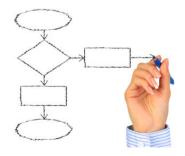
- Transnational Access
 - Exploratory Projects
 - Blue-sky projects

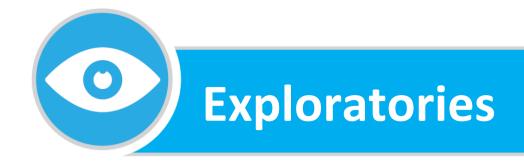




- Virtual Access
 - Data and Methods Catalogi
 - Modular virtual research environment



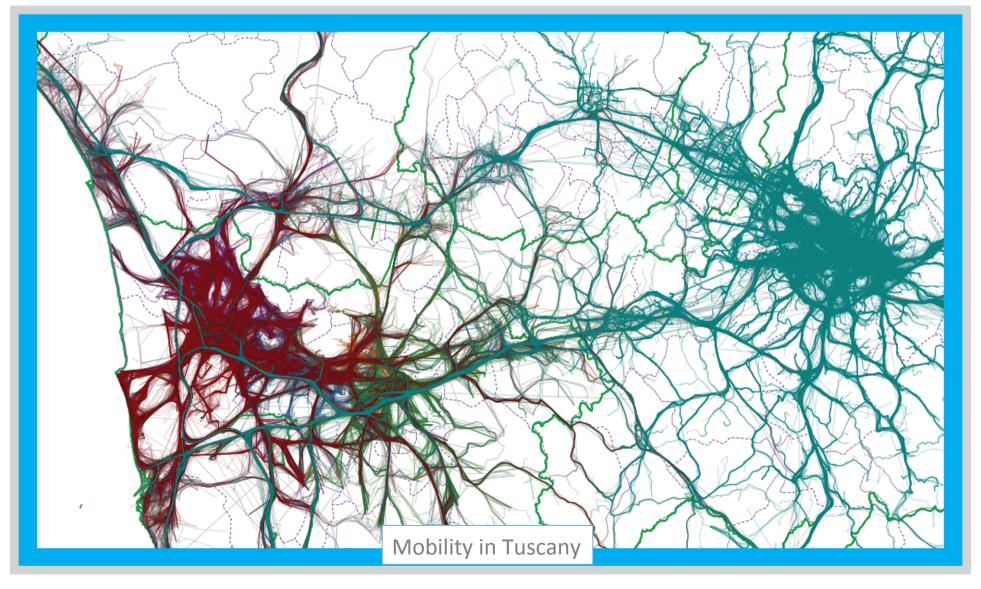




Social Mining Research Environments tailored on specific multidisciplinary domains

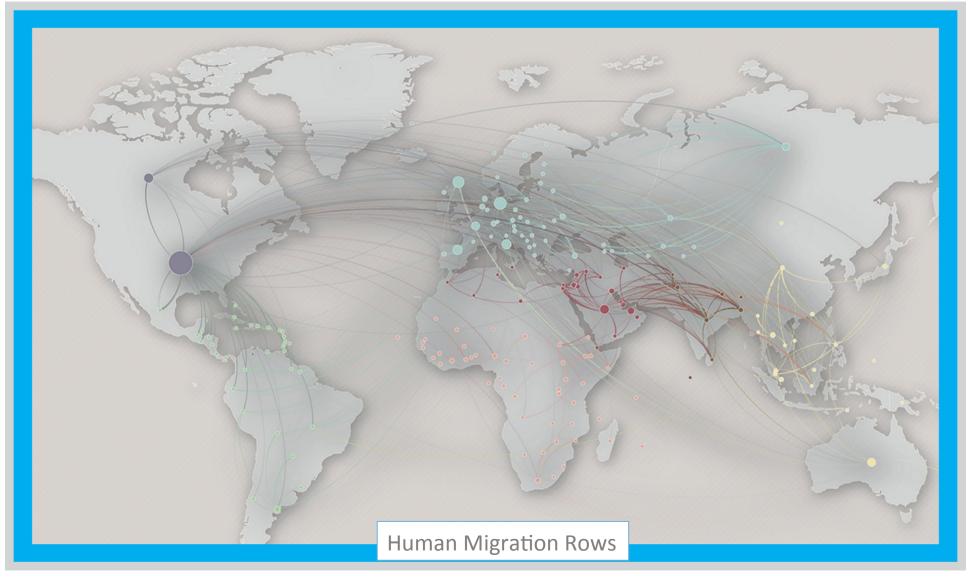


Exploratory: Big Data for Human Mobility



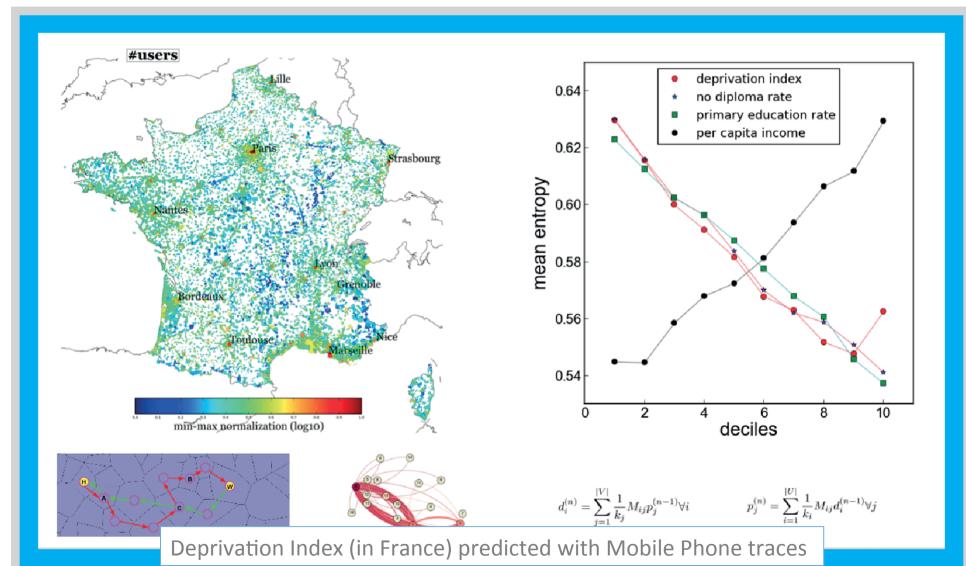


Exploratory: Big Data for Migration Studies





Exploratory: Big Data for Well Being





Exploratory: Big Data for Developing Countries





Exploratory: Big Data for Societal Debates





The SoBigData Stakeholders

- **Big data analysts and social informatics researchers**, who want to enhance their algorithms to deal with social data, gain multi-disciplinary research skills, harmonise existing data and analytics infrastructures, and engage other research communities in the development of these key enabling technologies for the future digital economy and society;
- Economists, social science and humanities researchers, journalists, policy and law makers, who have to analyse the avalanche of (big) social data, in order to gain insight and actionable knowledge.
- Researchers in related communities, who would like to use the algorithms, the analytical competences and data infrastructure;
- Industrial innovators & startuppers, who would like to create rapid proof-of-concepts of data-driven innovative ideas and services;
- The public as a whole, who would like to understand their role in the production, consumption and value-creating of social data.













MASTER BIG DATA 2016





























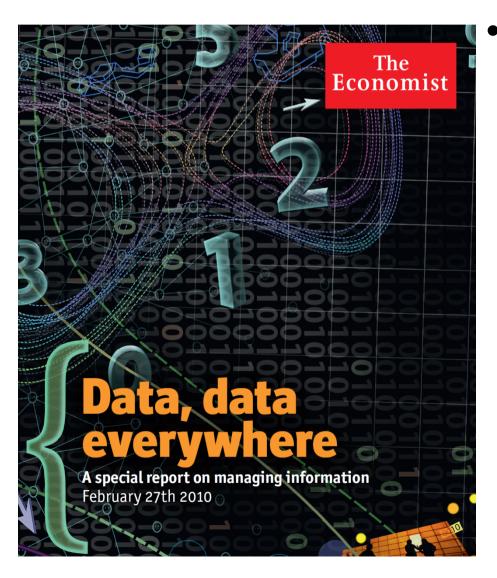




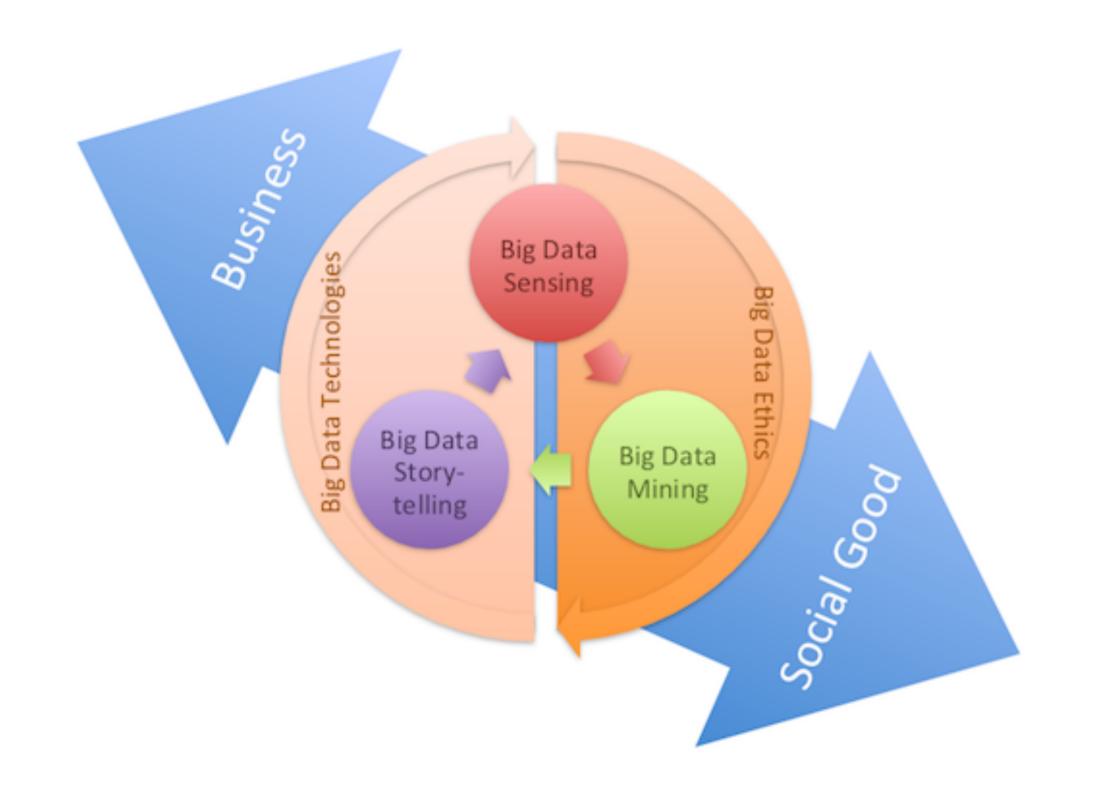


tiscali:

Data scientist



... a new kind of professional has emerged, the data scientist, who combines the skills of software programmer, statistician and storyteller/artist to extract the nuggets of gold hidden under mountains of data.











































www.sobigdata.eu



This is the work of many people for a long time

- Salvo Rinzivillo, Mirco Nanni, Roberto Trasarti, Salvatore Ruggieri, Chiara Renso, Anna Monreale, Franco Turini
- all the fantastic folks at KDD LAB Pisa
- many international collaborators
- Thanks!



























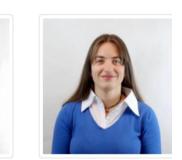


















Knowledge Discovery & Data Mining Lab http://kdd.isti.cnr.it













































Knowledge Discovery & Data Mining Lab http://kdd.isti.cnr.it

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