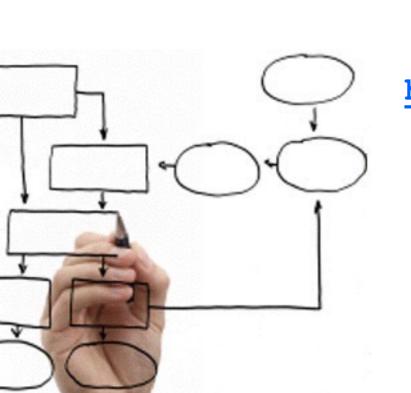
# Methods for the specification and verification of business processes MPB (6 cfu, 295AA)



#### Roberto Bruni

http://www.di.unipi.it/~bruni

\* - P and NP problems

#### Computational Complexity Theory

Computability theory studies the existence of algorithms that can solve a class of problems

For example, no algorithm exists that can be used to decide in a finite amount of time if any C (or Java) program terminates or diverges (on a given input)

Computational complexity theory deals with the resources needed to solve a solvable problem

For example, how many steps (time) or memory (space) it takes to solve a problem

#### Decision problem

A **problem** defines a set of related questions, each of finite length

A problem instance is one such question

For example, the factorization problem is: "given an integer n, return all its prime factors" An instance of the factorization problem is: "return all prime factors of 18"

A decision problem requires just a boolean answer For example: "given a number n, is n prime?" And an instance: "is 18 prime?"

P

The complexity class **P** is the set of decision problems that can be solved by a deterministic (Turing) machine in a **P**olynomial number of steps (time) w.r.t. input size

Problems in P can be (checked and) solved effectively

#### NP

The complexity class **NP** is the set of decision problems that can be **solved** by a **N**on-deterministic (Turing) machine in a **P**olynomial number of steps (time)

Equivalently **NP** is the set of decision problems whose solutions can be **checked** by a deterministic (Turing) machine in a polynomial number of steps (time)

Solutions of problems in NP can be checked effectively

#### P vs NP

The question of whether **P** is the same set as **NP** is the most important open question in computer science

Intuitively, it is much harder to solve a problem than to check the correctness of a solution

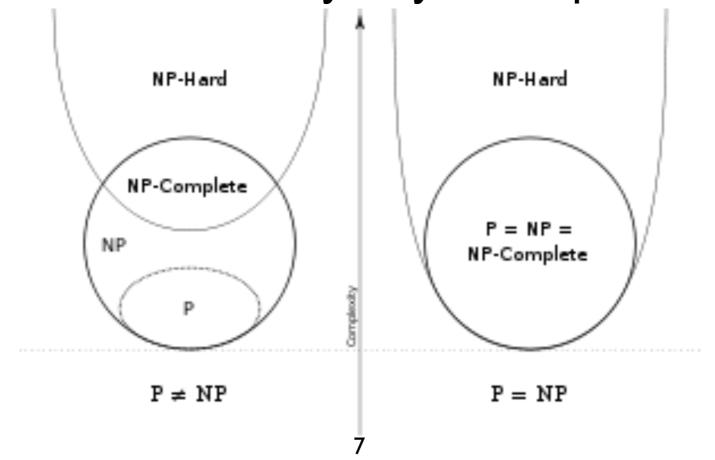
A fact supported by our daily experience, which leads us to conjecture **P** ≠ **NP** 

What if "solving" is not really harder than "checking"? what if **P** = **NP**?

#### NP-completeness

A problem Q in **NP** is **NP-complete** if every other problem in **NP** can be reduced to Q (in polynomial time)

(finding an effective way to solve such a problem Q would allow to solve effectively any other problem in **NP**)

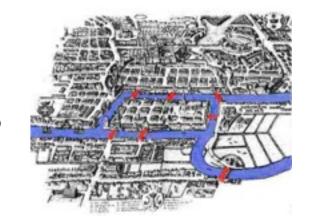


#### Eulerian circuit problem (P)

Given a graph G, is it possible to draw an Eulerian circuit over it? (i.e. a circuit that traverses each edge exactly once)

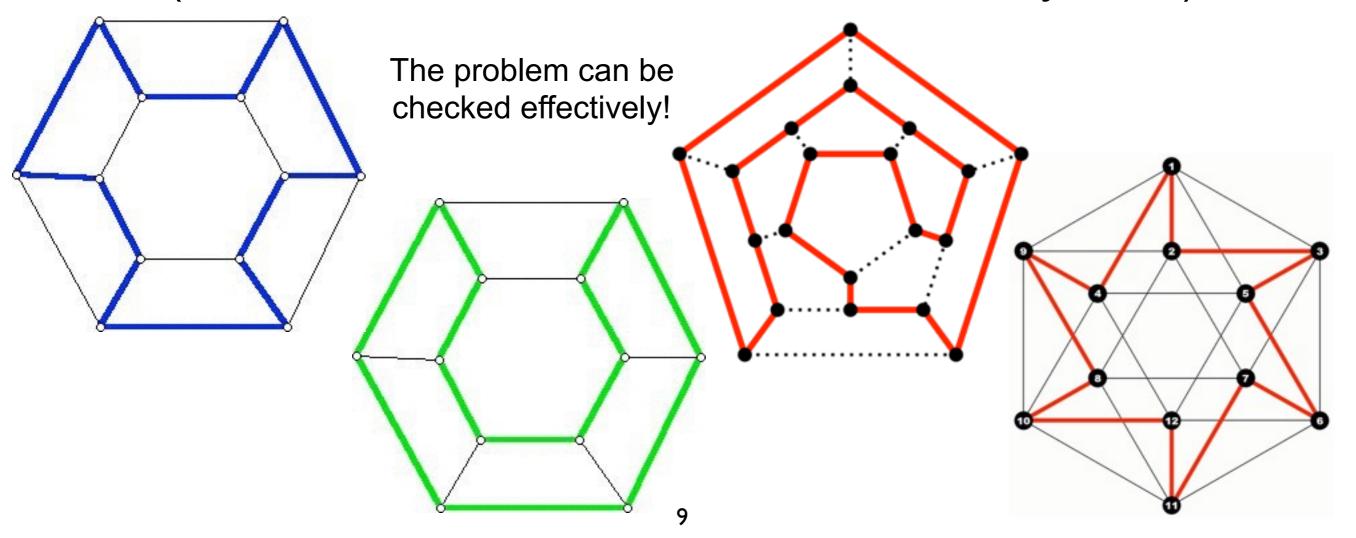
We have seen that it is the same problem as:

Given a graph G, is the degree of each vertex even?

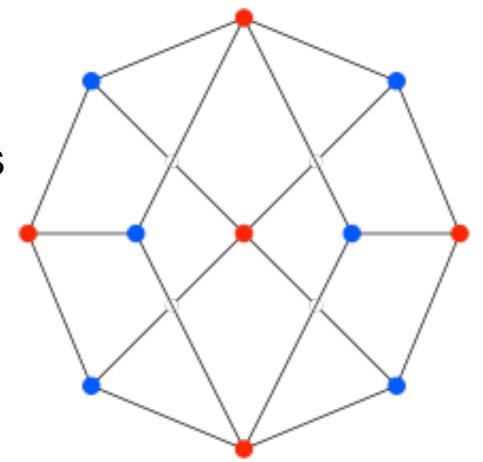


The problem can be solved effectively!

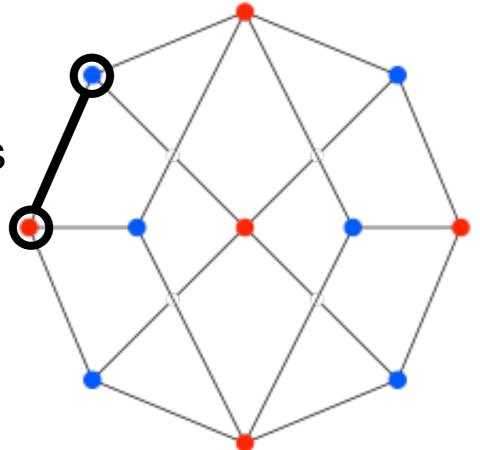
Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



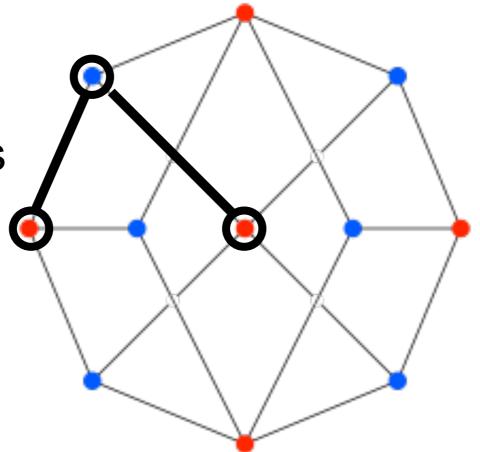
Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



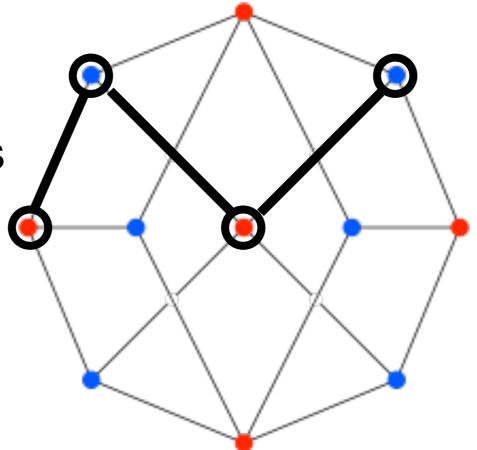
Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



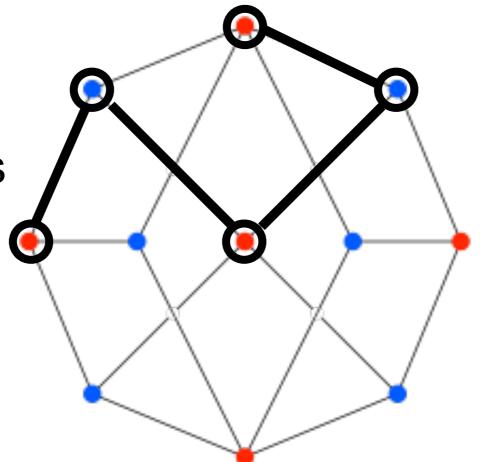
Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)

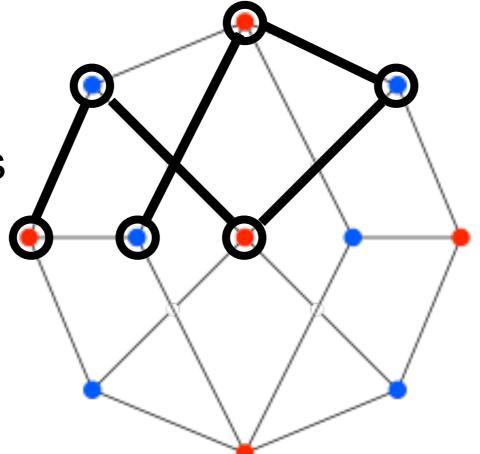


Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)

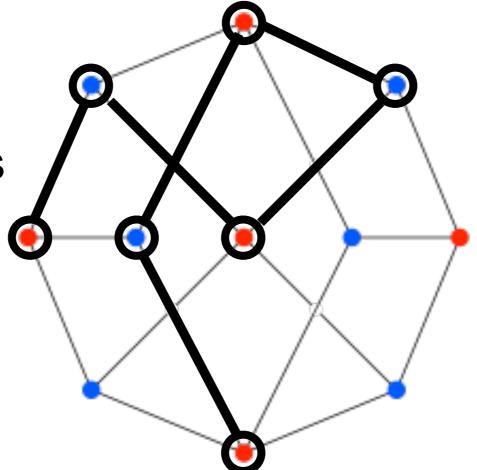


Given a graph G,

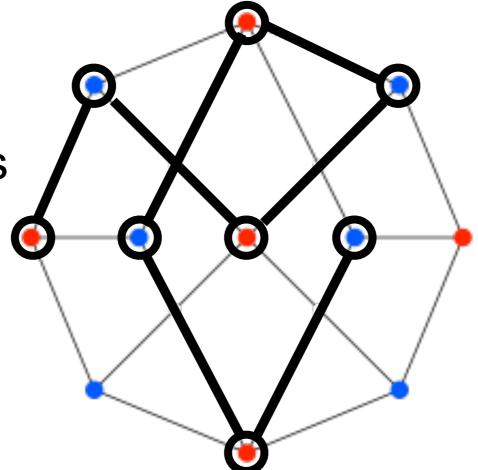
is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



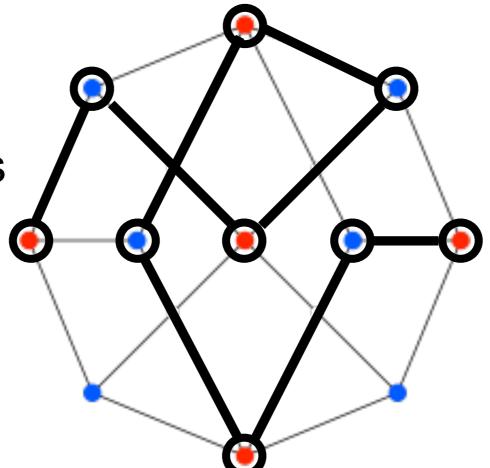
Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)



Given a graph G, is it possible to draw an Hamiltonian circuit over it? (i.e. a circuit that visits each vertex exactly once)

