

Knowledge discovery & data mining

Classification & fraud detection

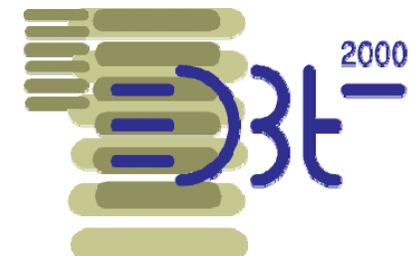
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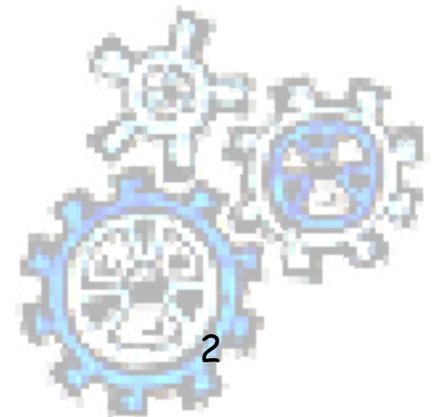
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Module outline

- **The classification task**
- **Main classification techniques**
 - Bayesian classifiers
 - Decision trees
 - Hints to other methods
- **Application to a case-study in fiscal fraud detection: audit planning**



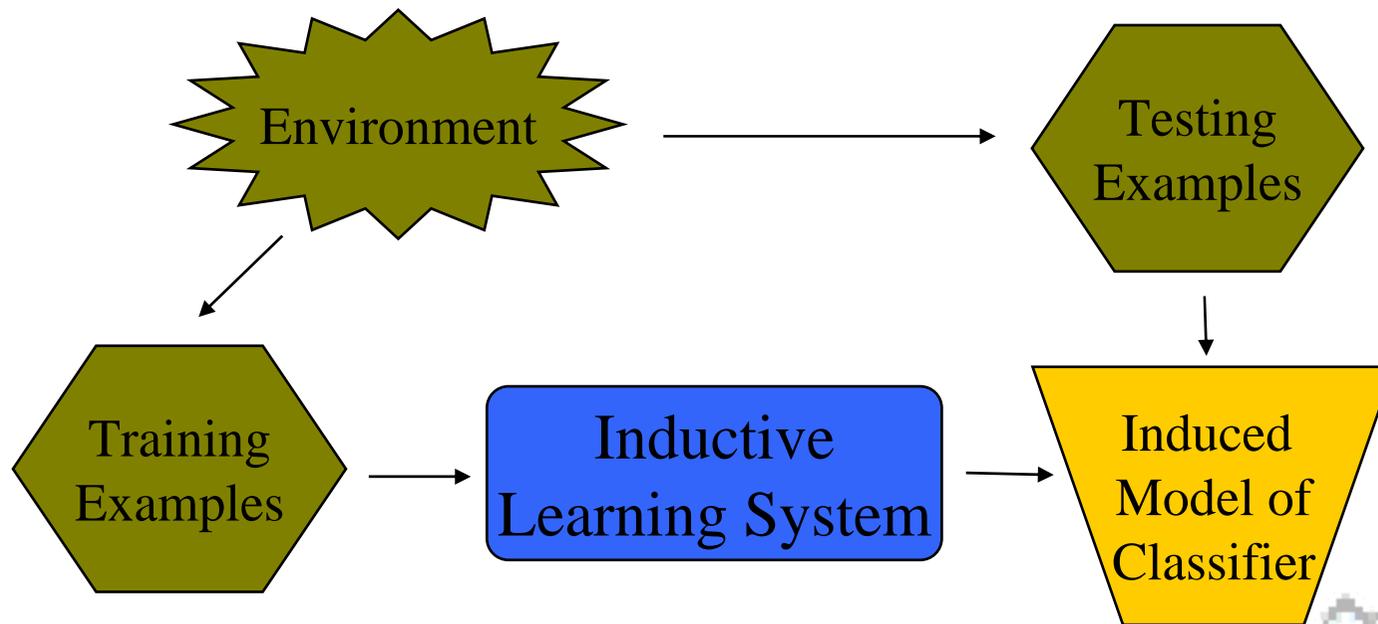
The classification task

- Input: a **training set** of tuples, each labelled with one class label
- Output: a **model** (classifier) which assigns a class label to each tuple based on the other attributes.
- The model can be used to **predict** the class of new tuples, for which the class label is missing or unknown
- Some natural applications
 - credit approval
 - medical diagnosis
 - treatment effectiveness analysis



Classification systems and inductive learning

Basic Framework for Inductive Learning



$(x, f(x))$

$h(x) \cong f(x)?$

A problem of representation and search for the best hypothesis, $h(x)$.

Output Classification

$(x, h(x))$

Train & test

- The tuples (observations, samples) are partitioned in **training set** + **test set**.
- Classification is performed in two steps:
 1. training - build the model from training set
 2. test - check accuracy of the model using test set

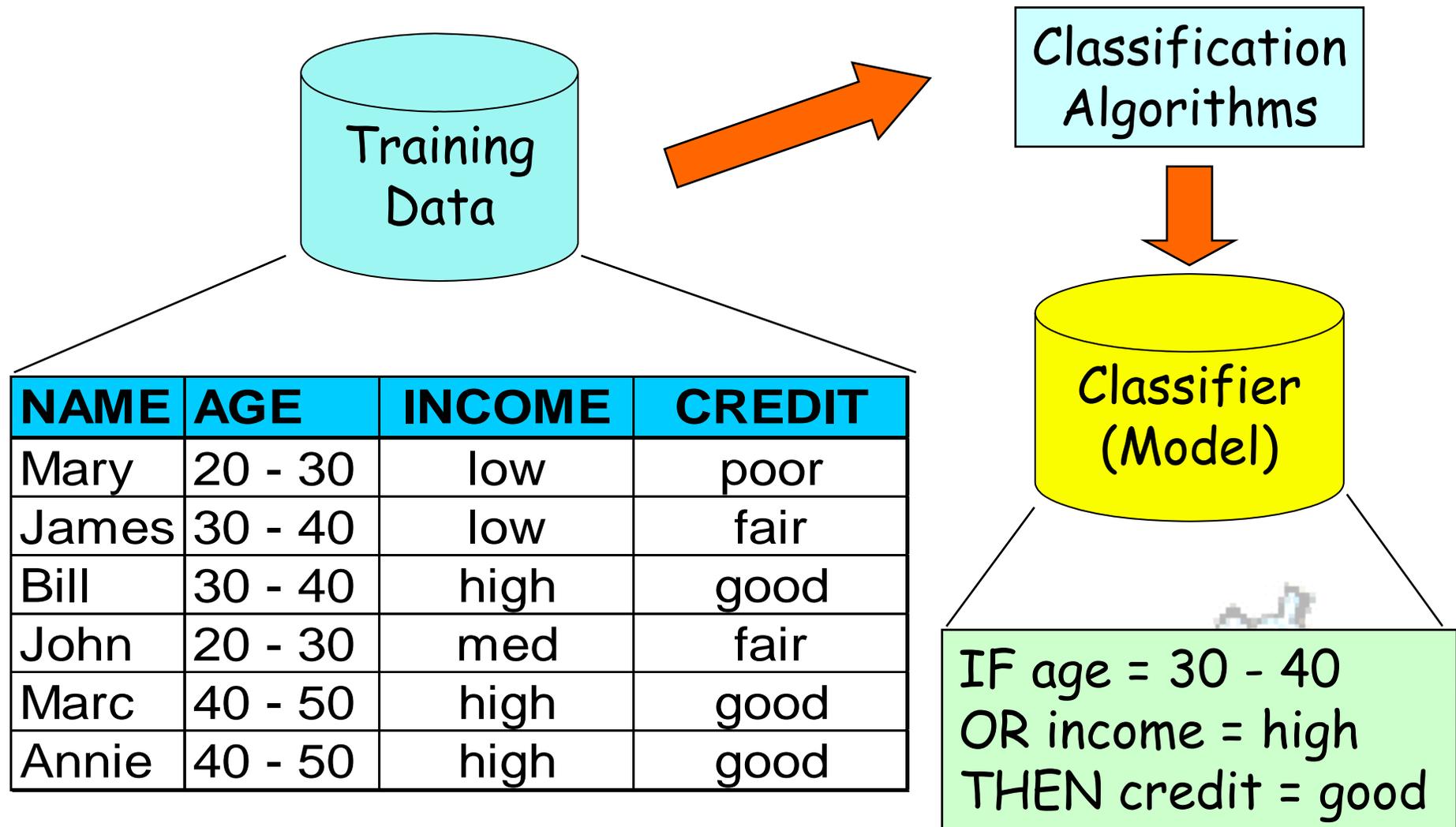


Train & test

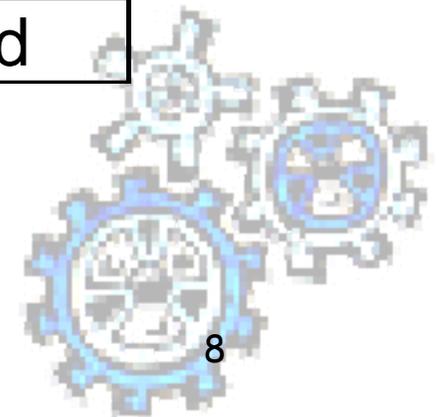
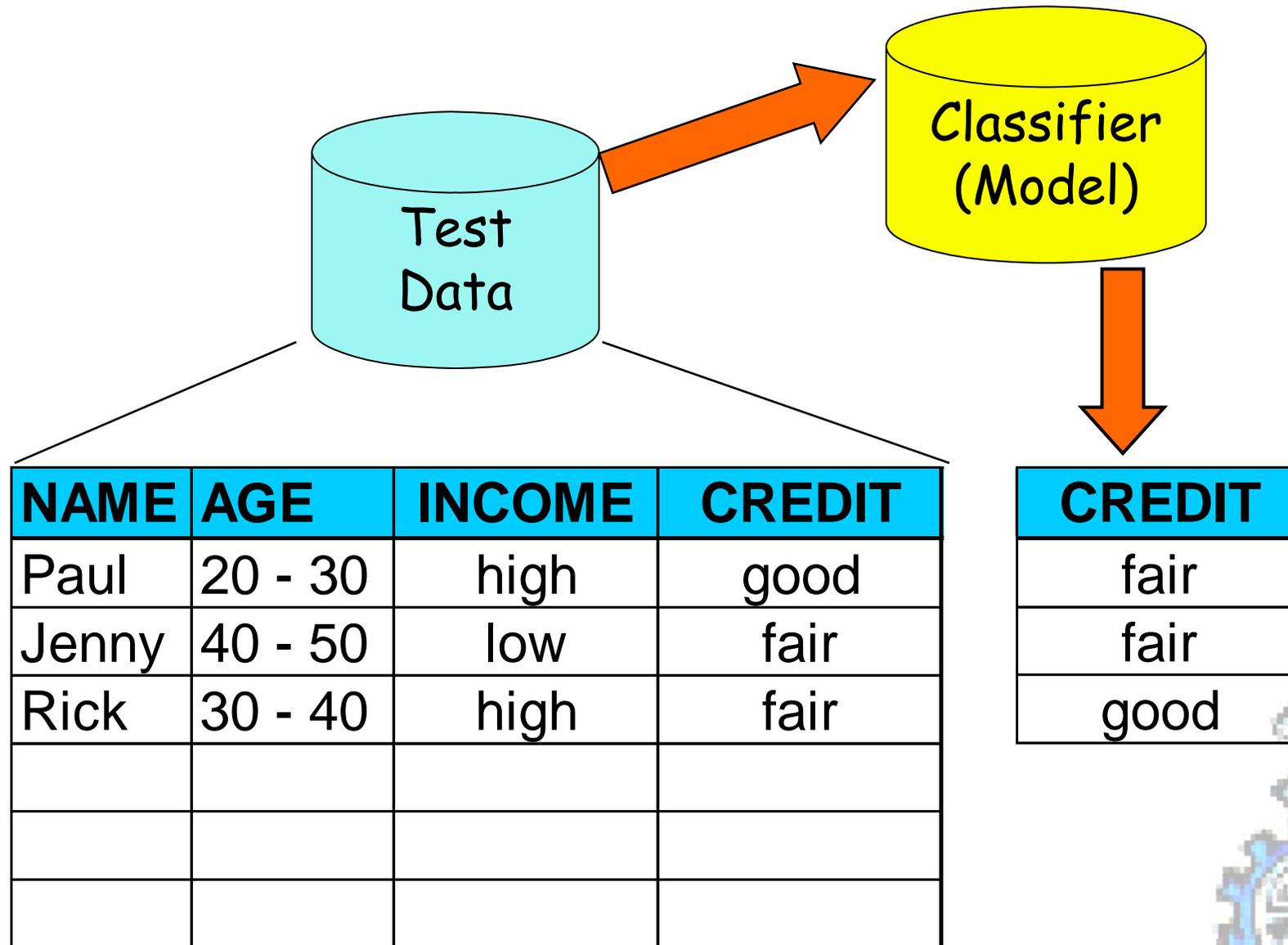
- Kind of models
 - IF-THEN rules
 - Other logical formulae
 - Decision trees
- Accuracy of models
 - The known class of test samples is matched against the class predicted by the model.
 - Accuracy rate = % of test set samples correctly classified by the model.



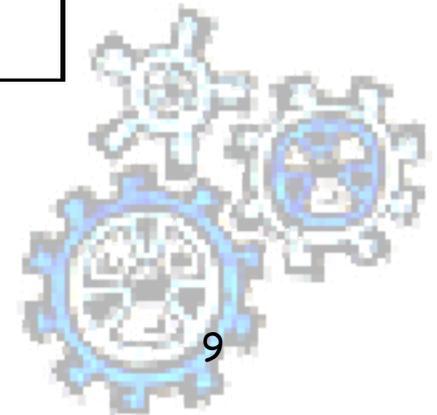
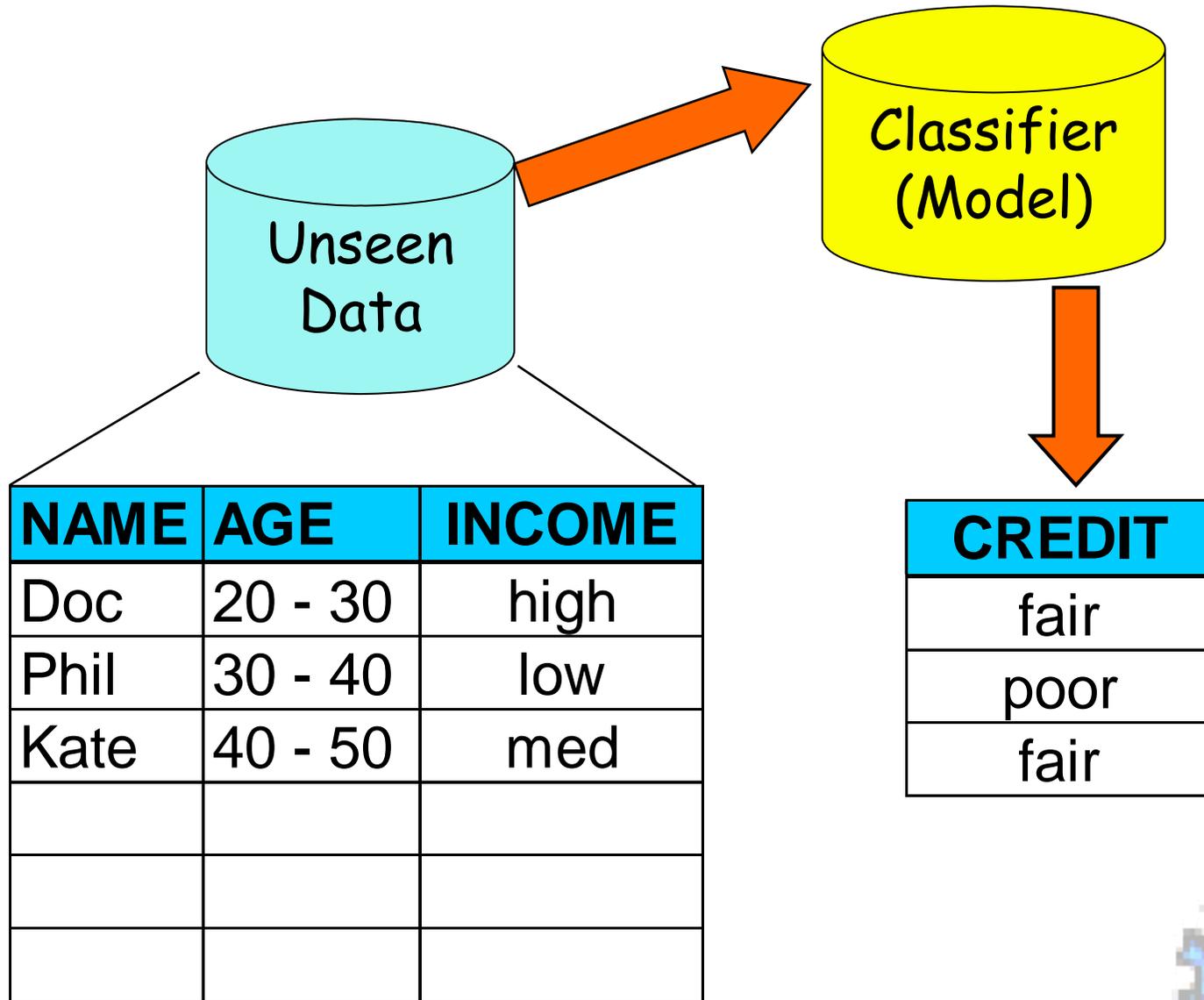
Training step



Test step

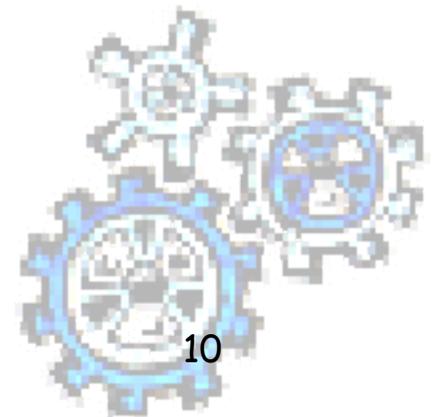


Prediction



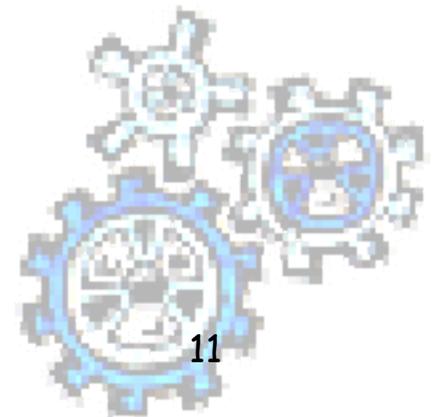
Machine learning terminology

- **Classification = supervised learning**
 - use training samples with known classes to classify new data
- **Clustering = unsupervised learning**
 - training samples have no class information
 - guess classes or clusters in the data



Comparing classifiers

- Accuracy
- Speed
- Robustness
 - w.r.t. noise and missing values
- Scalability
 - efficiency in large databases
- Interpretability of the model
- Simplicity
 - decision tree size
 - rule compactness
- Domain-dependent quality indicators



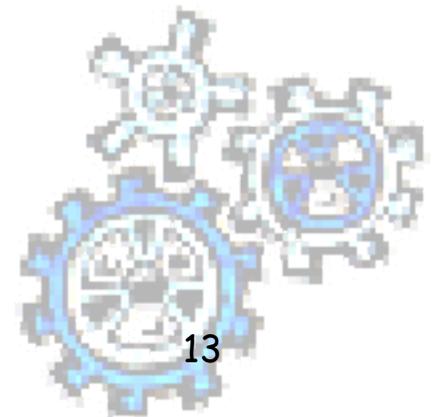
Classical example: play tennis?

⌘ Training set from Quinlan's book

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
rain	mild	high	false	P
rain	cool	normal	false	P
rain	cool	normal	true	N
overcast	cool	normal	true	P
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Bayesian classification

- The classification problem may be formalized using **a-posteriori probabilities**:
- $P(C|X)$ = prob. that the sample tuple $X = \langle x_1, \dots, x_k \rangle$ is of class C .
- E.g. $P(\text{class}=\text{N} \mid \text{outlook}=\text{sunny}, \text{windy}=\text{true}, \dots)$
- Idea: assign to sample X the class label C such that $P(C|X)$ is maximal



Estimating a-posteriori probabilities

- **Bayes theorem:**

$$P(C|X) = P(X|C) \cdot P(C) / P(X)$$

- $P(X)$ is constant for all classes
- $P(C)$ = relative freq of class C samples
- C such that $P(C|X)$ is maximum =
 C such that $P(X|C) \cdot P(C)$ is maximum
- **Problem: computing $P(X|C)$ is unfeasible!**



Naïve Bayesian Classification

- Naïve assumption: **attribute independence**

$$P(x_1, \dots, x_k | C) = P(x_1 | C) \cdot \dots \cdot P(x_k | C)$$

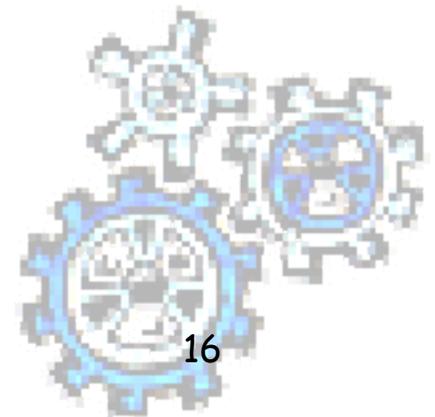
- If i -th attribute is **categorical**:

$P(x_i | C)$ is estimated as the relative freq of samples having value x_i as i -th attribute in class C

- If i -th attribute is **continuous**:

$P(x_i | C)$ is estimated thru a Gaussian density function

- Computationally easy in both cases



Play-tennis example: estimating $P(x_i|C)$

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
rain	mild	high	false	P
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sunny	cool	normal	false	P
rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N

$$P(p) = 9/14$$

$$P(n) = 5/14$$

outlook

$$P(\text{sunny}|p) = 2/9$$

$$P(\text{sunny}|n) = 3/5$$

$$P(\text{overcast}|p) = 4/9$$

$$P(\text{overcast}|n) = 0$$

$$P(\text{rain}|p) = 3/9$$

$$P(\text{rain}|n) = 2/5$$

temperature

$$P(\text{hot}|p) = 2/9$$

$$P(\text{hot}|n) = 2/5$$

$$P(\text{mild}|p) = 4/9$$

$$P(\text{mild}|n) = 2/5$$

$$P(\text{cool}|p) = 3/9$$

$$P(\text{cool}|n) = 1/5$$

humidity

$$P(\text{high}|p) = 3/9$$

$$P(\text{high}|n) = 4/5$$

$$P(\text{normal}|p) = 6/9$$

$$P(\text{normal}|n) = 2/5$$

windy

$$P(\text{true}|p) = 3/9$$

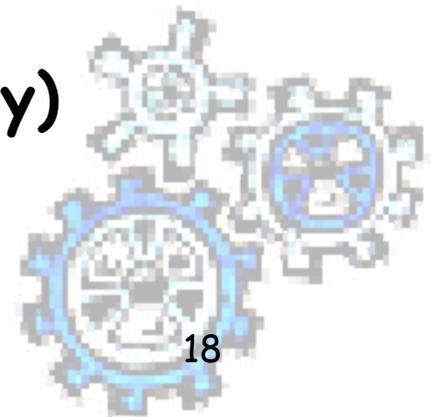
$$P(\text{true}|n) = 3/5$$

$$P(\text{false}|p) = 6/9$$

$$P(\text{false}|n) = 2/5$$

Play-tennis example: classifying X

- An unseen sample $X = \langle \text{rain, hot, high, false} \rangle$
- $P(X|p) \cdot P(p) =$
 $P(\text{rain}|p) \cdot P(\text{hot}|p) \cdot P(\text{high}|p) \cdot P(\text{false}|p) \cdot P(p) =$
 $3/9 \cdot 2/9 \cdot 3/9 \cdot 6/9 \cdot 9/14 = 0.010582$
- $P(X|n) \cdot P(n) =$
 $P(\text{rain}|n) \cdot P(\text{hot}|n) \cdot P(\text{high}|n) \cdot P(\text{false}|n) \cdot P(n) =$
 $2/5 \cdot 2/5 \cdot 4/5 \cdot 2/5 \cdot 5/14 = 0.018286$
- Sample X is classified in class n (don't play)



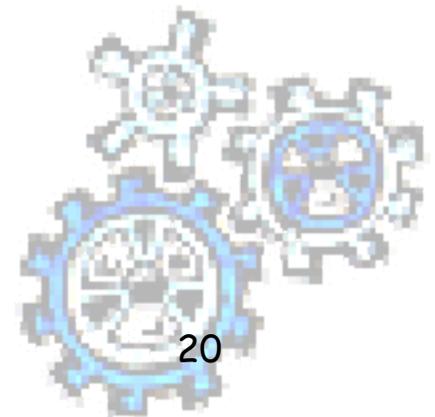
The independence hypothesis...

- ... makes computation possible
- ... yields optimal classifiers when satisfied
- ... but is seldom satisfied in practice, as attributes (variables) are often correlated.
- Attempts to overcome this limitation:
 - **Bayesian networks**, that combine Bayesian reasoning with causal relationships between attributes
 - **Decision trees**, that reason on one attribute at the time, considering most important attributes first



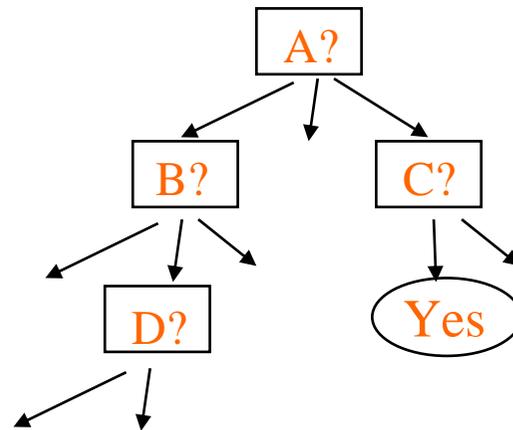
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Decision trees

- A tree where
- **internal node** = test on a single attribute
- **branch** = an outcome of the test
- **leaf node** = class or class distribution

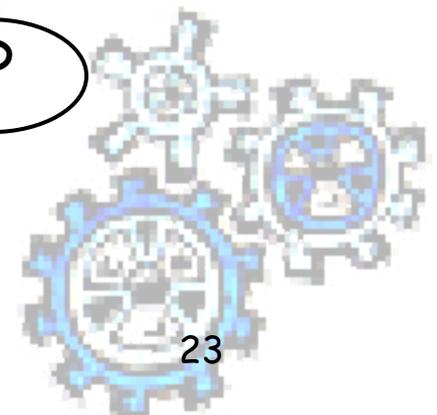
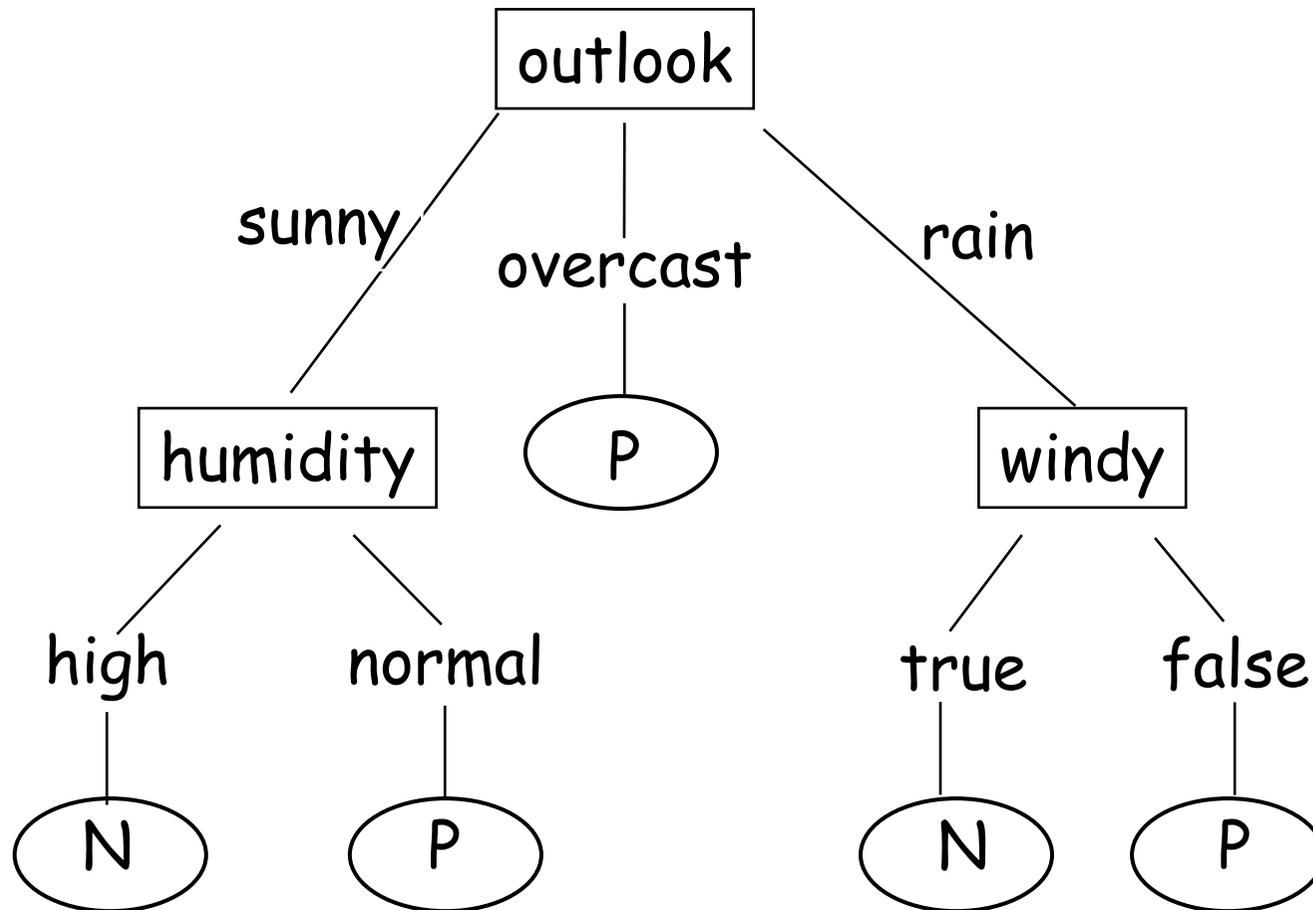


Classical example: play tennis?

⌘ Training set from Quinlan's book

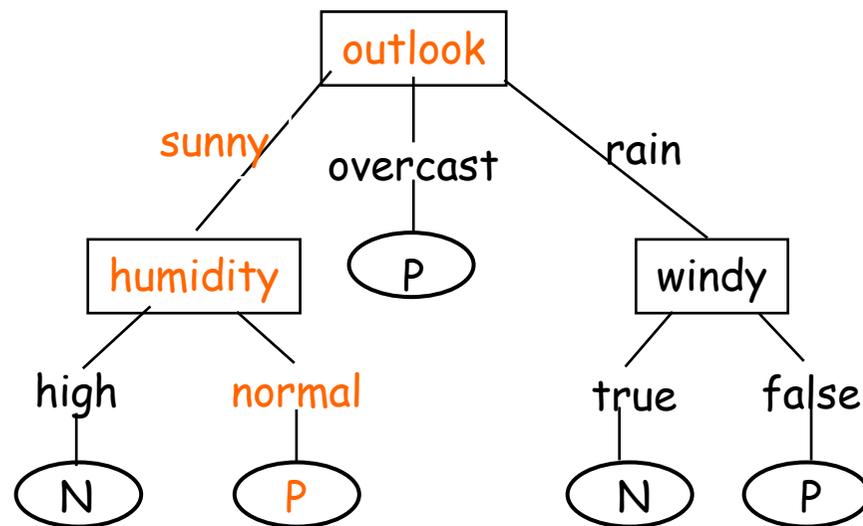
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rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
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Decision tree obtained with ID3 (Quinlan 86)



From decision trees to classification rules

- One rule is generated for each **path** in the tree from the root to a leaf
- Rules are generally simpler to understand than trees



**IF outlook=sunny
AND humidity=normal
THEN play tennis**



Decision tree induction

- Basic algorithm
 - top-down recursive
 - divide & conquer
 - greedy (may get trapped in local maxima)
- Many variants:
 - from **machine learning**: ID3 (Iterative Dichotomizer), C4.5 (Quinlan 86, 93)
 - from **statistics**: CART (Classification and Regression Trees) (Breiman et al 84)
 - from **pattern recognition**: CHAID (Chi-squared Automated Interaction Detection) (Magidson 94)
- Main difference: divide (**split**) criterion

Generate_DT(samples, attribute_list) =

- 1) Create a new node **N**;
- 2) If **samples** are all of class **C** then label **N** with **C** and exit;
- 3) If **attribute_list** is empty then label **N** with **majority_class(N)** and exit;
- 4) Select **best_split** from **attribute_list**;
- 5) For each value **v** of attribute **best_split**:
 - ⌘ Let **S_v** = set of samples with **best_split=v** ;
 - ⌘ Let **N_v** = **Generate_DT(S_v, attribute_list \ best_split)** ;
 - ⌘ Create a branch from **N** to **N_v** labeled with the test **best_split=v** ;



Criteria for finding the best split

- **Information gain (ID3 - C4.5)**
 - Entropy, an information theoretic concept, measures impurity of a split
 - Select attribute that maximize entropy reduction
- **Gini index (CART)**
 - Another measure of impurity of a split
 - Select attribute that minimize impurity
- **χ^2 contingency table statistic (CHAID)**
 - Measures correlation between each attribute and the class label
 - Select attribute with maximal correlation

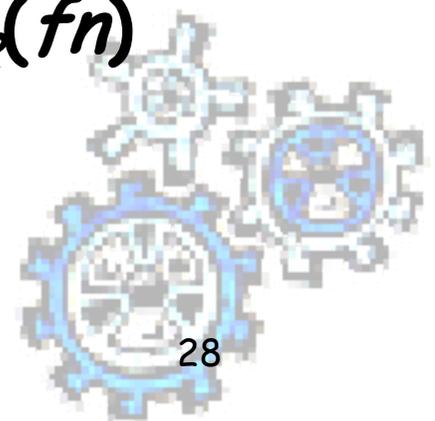
Information gain (ID3 - C4.5)

E.g., two classes, *Pos* and *Neg*, and dataset *S* with *p* *Pos*-elements and *n* *Neg*-elements.

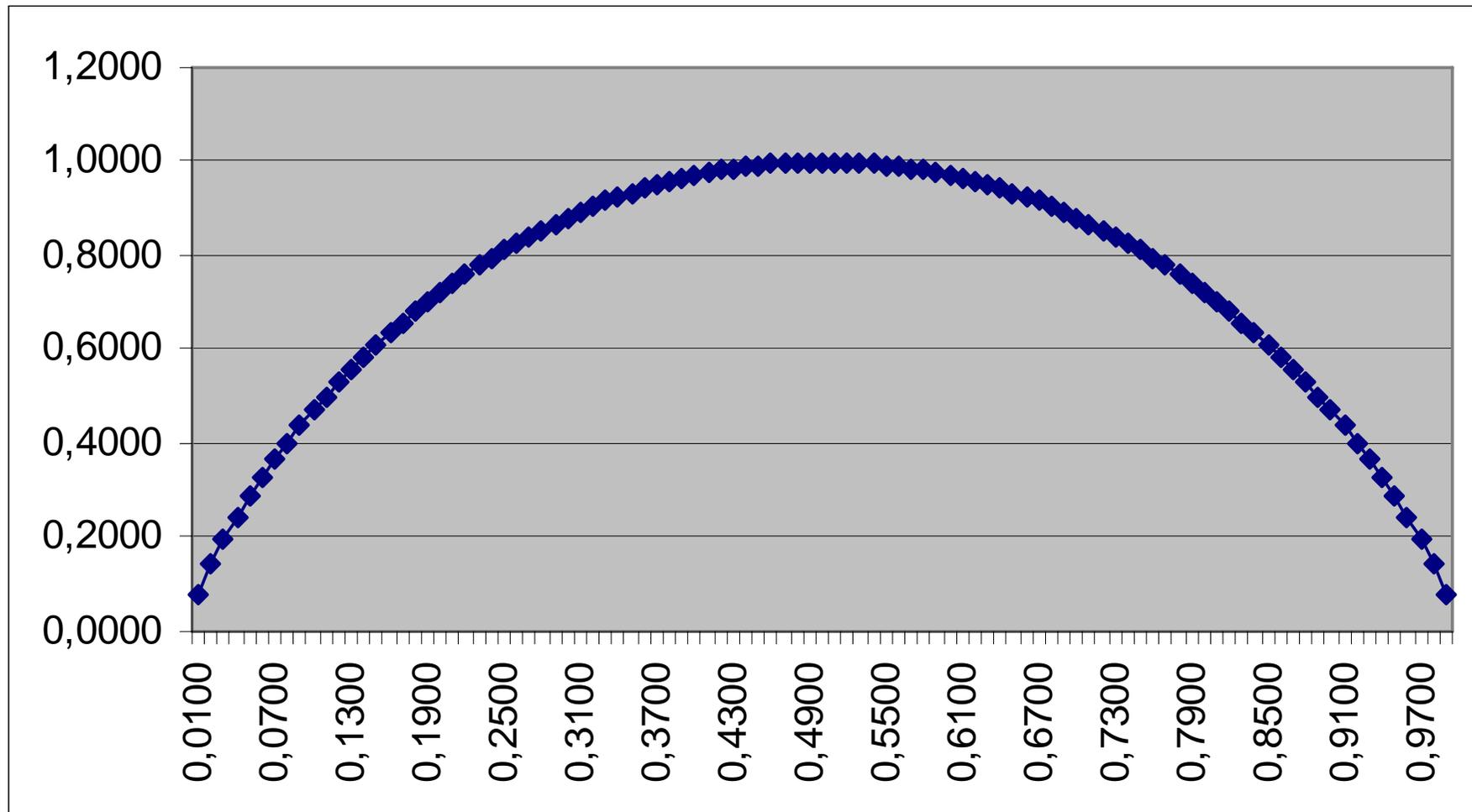
- Amount of information to decide if an arbitrary example belongs to *Pos* or *Neg*:

- $fp = p / (p+n)$ $fn = n / (p+n)$

$$I(p, n) = - fp \cdot \log_2(fp) - fn \cdot \log_2(fn)$$



Entropy



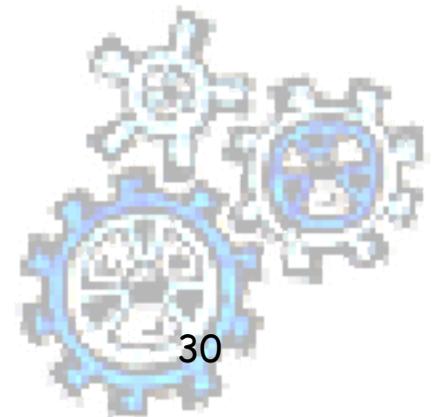
Information gain (ID3 - C4.5)

- Entropy = information needed to classify samples in a split according to an attribute
- Splitting S with attribute A results in partition $\{S_1, S_2, \dots, S_k\}$
- p_i (resp. n_i) = # elements in S_i from Pos (resp. Neg)

$$E(A) = \sum_{i \in [1, k]} I(p_i, n_i) \cdot (p_i + n_i) / (p + n)$$

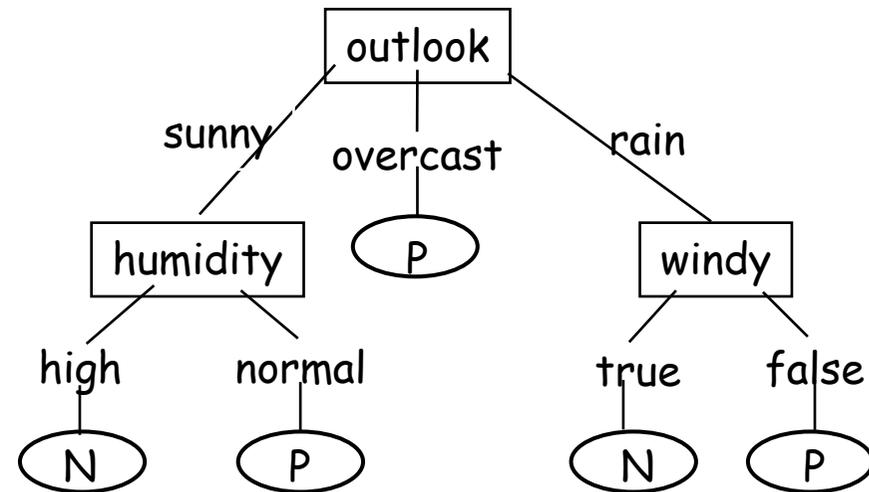
$$gain(A) = I(p, n) - E(A)$$

- Select A which maximizes $gain(A)$
- Extensible to continuous attributes



Information gain - play tennis example

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
rain	mild	high	false	P
rain	cool	normal	false	P
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sunny	cool	normal	false	P
rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N



⌘ Choosing best split at root node:

⌘ $gain(outlook) = 0.246$

⌘ $gain(temperature) = 0.029$

⌘ $gain(humidity) = 0.151$

⌘ $gain(windy) = 0.048$

⌘ Criterion biased towards attributes with many values - corrections proposed (*gain ratio*)



Gini index (CART)

- E.g., two classes, *Pos* and *Neg*, and dataset *S* with *p* *Pos*-elements and *n* *Neg*-elements.

- $fp = p / (p+n)$ $fn = n / (p+n)$

$$gini(S) = 1 - fp^2 - fn^2$$

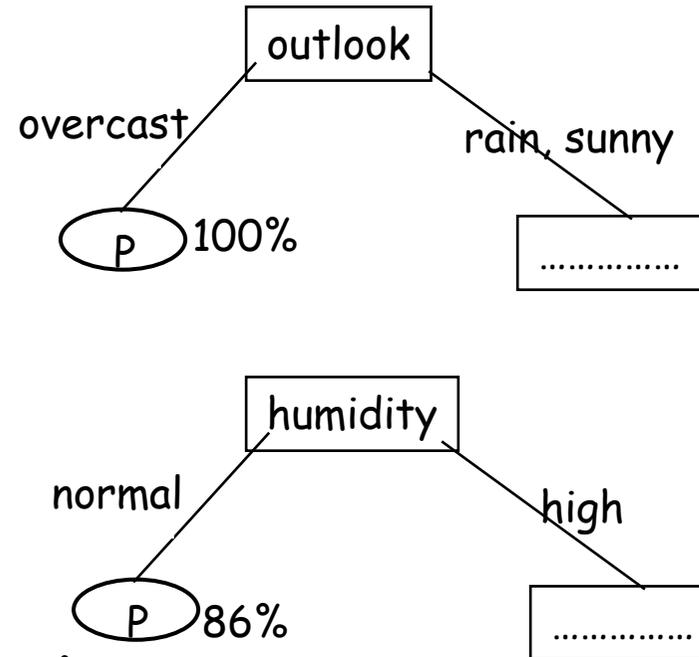
- If dataset *S* is split into *S*₁, *S*₂ then

$$gini_{split}(S_1, S_2) = gini(S_1) \cdot (p_1+n_1)/(p+n) + gini(S_2) \cdot (p_2+n_2)/(p+n)$$



Gini index - play tennis example

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
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rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N



⌘ Two top best splits at root node:

⌘ Split on outlook:

⌘ S_1 : {overcast} (4Pos, 0Neg) S_2 : {sunny, rain}

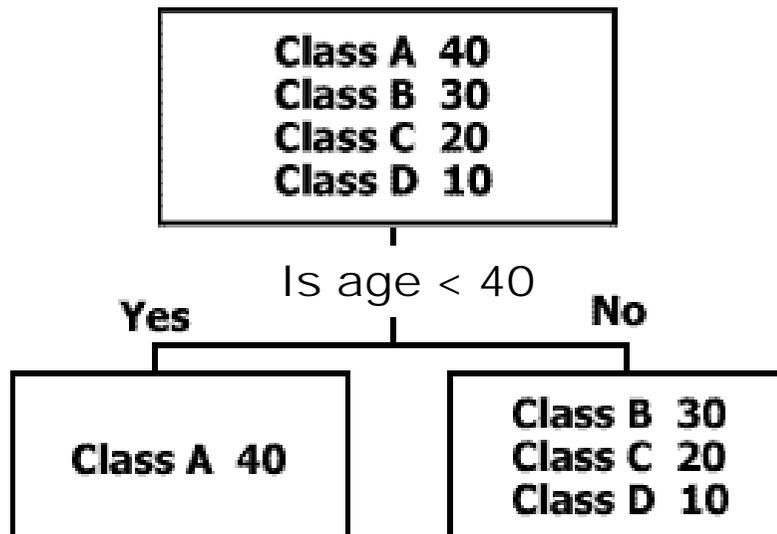
⌘ Split on humidity:

⌘ S_1 : {normal} (6Pos, 1Neg) S_2 : {high}

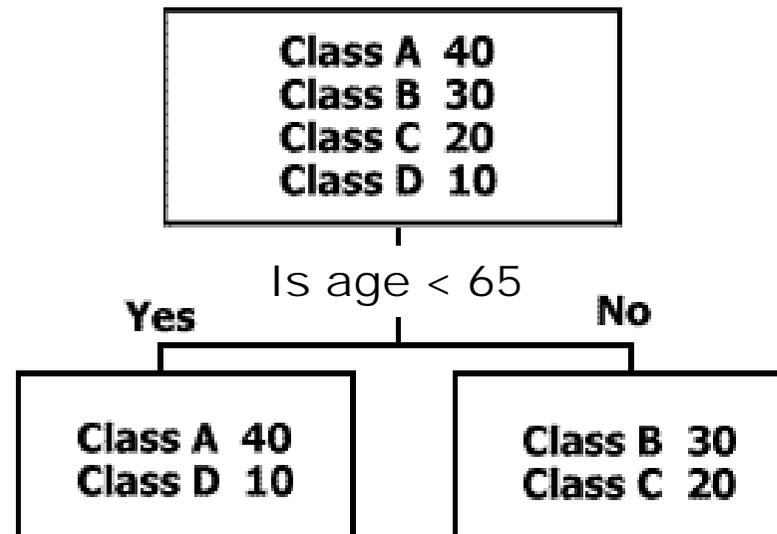


Entropy vs. Gini (on continuous attributes)

- Gini tends to isolate the largest class from all other classes



- Entropy tends to find groups of classes that add up to 50% of the data



Other criteria in decision tree construction

- **Branching scheme:**
 - binary vs. k -ary splits
 - categorical vs. continuous attributes
- **Stop rule:** how to decide that a node is a leaf:
 - all samples belong to same class
 - *impurity* measure below a given threshold
 - no more attributes to split on
 - no samples in partition
- **Labeling rule:** a leaf node is labeled with the class to which most samples at the node belong



The *overfitting* problem

- Ideal goal of classification: find the **simplest** decision tree that **fits the data** and **generalizes to unseen data**
 - intractable in general
- A decision tree may become too complex if it **overfits** the training samples, due to
 - noise and outliers, or
 - too little training data, or
 - local maxima in the greedy search
- Two heuristics to avoid overfitting:
 - **Stop earlier**: Stop growing the tree earlier.
 - **Post-prune**: Allow overfit, and then simplify the tree.

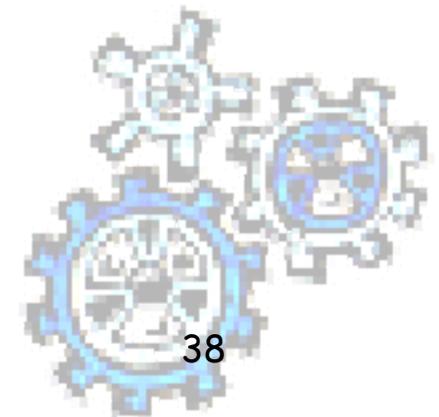
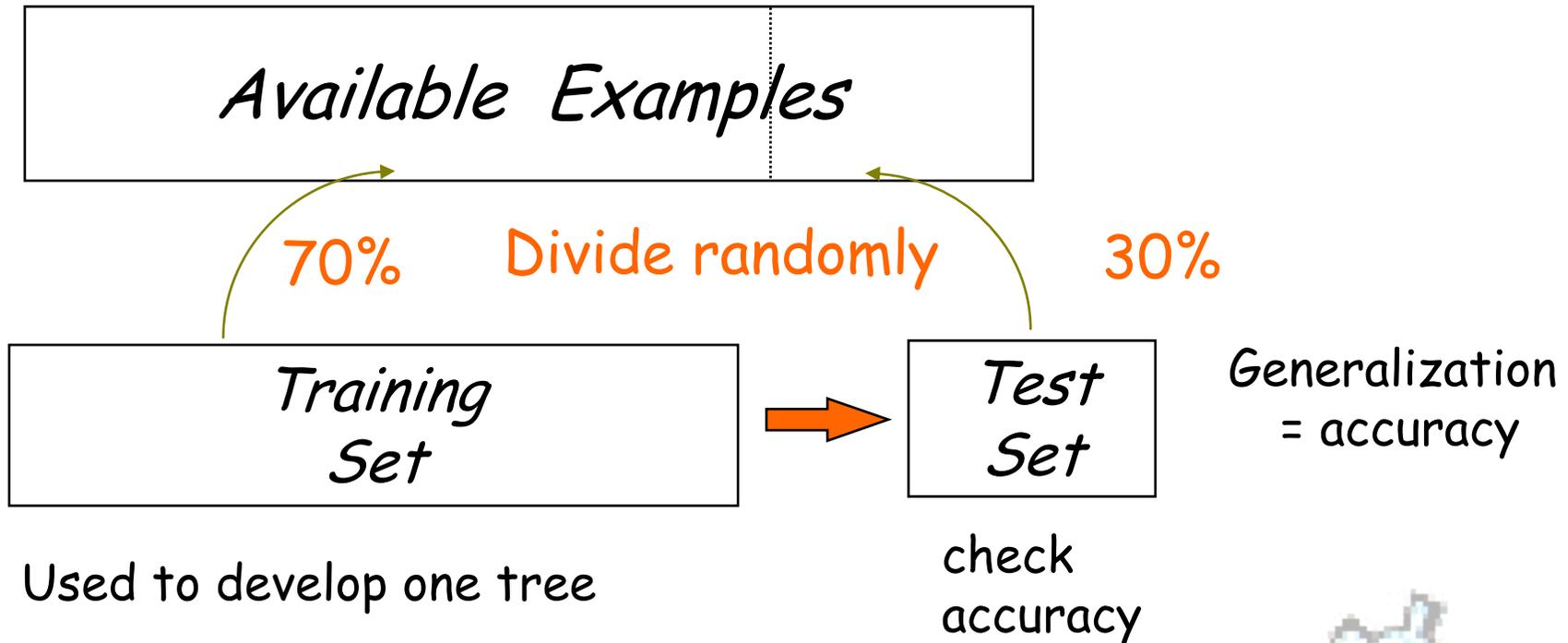


Stopping vs. pruning

- **Stopping**: Prevent the split on an attribute (predictor variable) if it is below a level of statistical significance - simply make it a leaf (CHAID)
- **Pruning**: After a complex tree has been grown, replace a split (subtree) with a leaf if the *predicted* validation error is no worse than the more complex tree (CART, C4.5)
- Integration of the two: **PUBLIC** (Rastogi and Shim 98) - estimate pruning conditions (lower bound to minimum cost subtrees) during construction, and use them to stop.

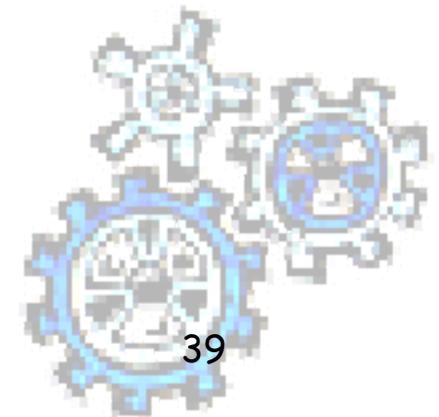
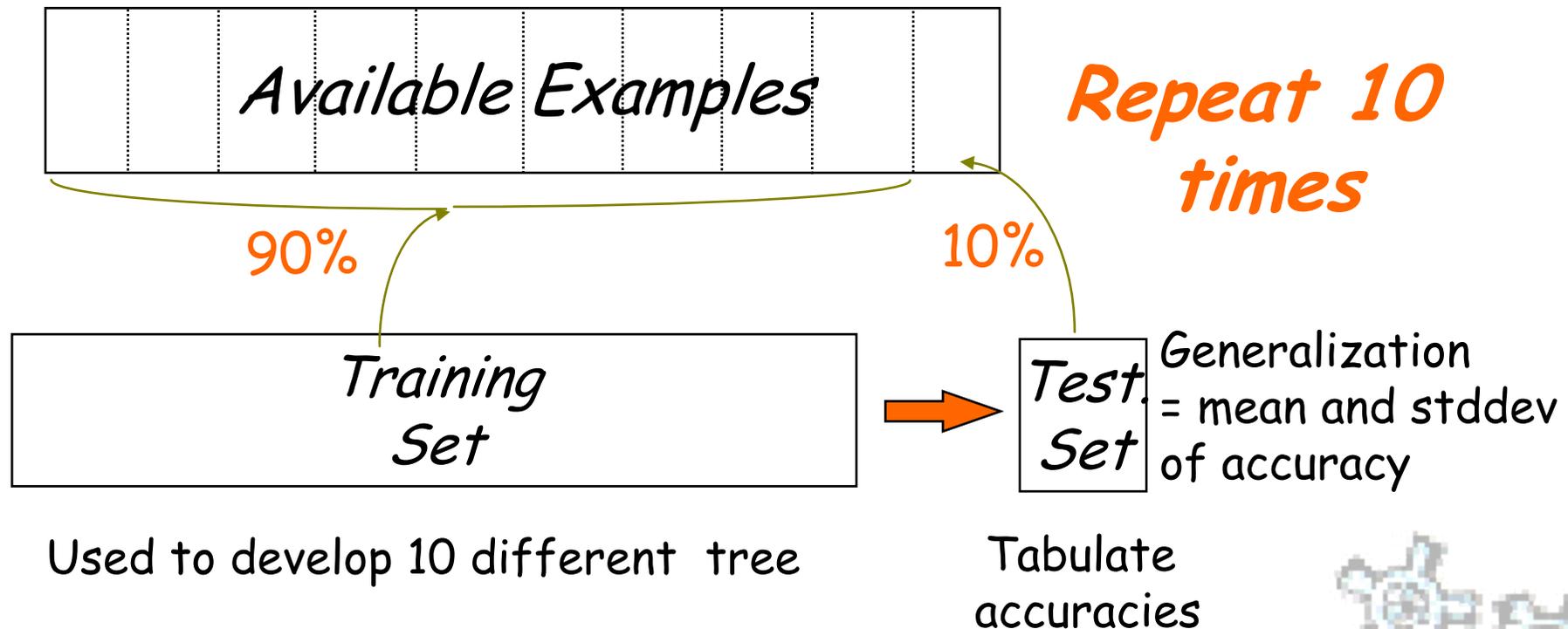


If dataset is large



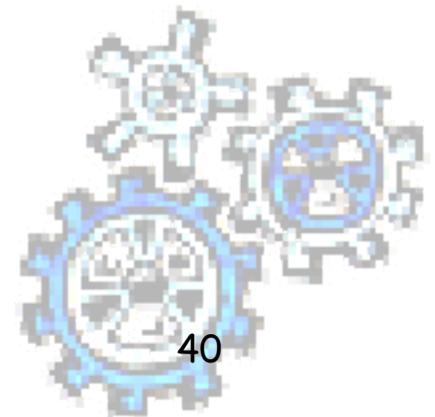
If data set is not so large

■ Cross-validation



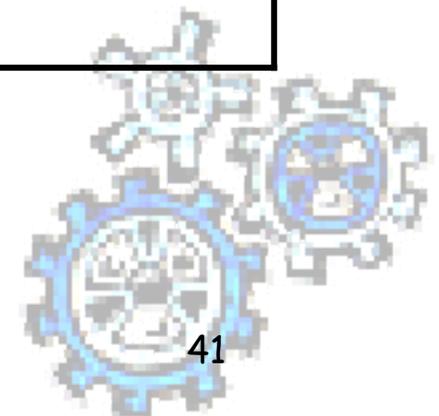
Categorical vs. continuous attributes

- Information gain criterion may be adapted to continuous attributes using binary splits
- Gini index may be adapted to categorical.
- Typically, discretization is not a pre-processing step, but is performed **dynamically** during the decision tree construction.



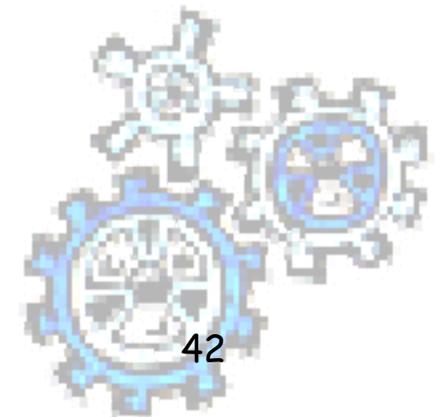
Summarizing ...

tool→	C4.5	CART	CHAID
arity of split	binary and K-ary	binary	K-ary
split criterion	information gain	gini index	χ^2
stop vs. prune	prune	prune	stop
type of attributes	categorical +continuous	categorical +continuous	categorical



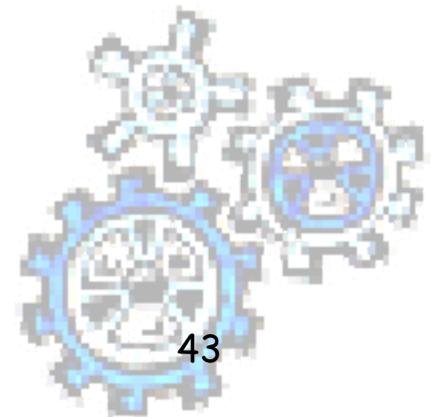
Scalability to large databases

- What if the dataset does not fit main memory?
- Early approaches:
 - Incremental tree construction (Quinlan 86)
 - Merge of trees constructed on separate data partitions (Chan & Stolfo 93)
 - Data reduction via sampling (Cattlet 91)
- Goal: handle order of 1G samples and 1K attributes
- Successful contributions from data mining research
 - **SLIQ** (Mehta et al. 96)
 - **SPRINT** (Shafer et al. 96)
 - **PUBLIC** (Rastogi & Shim 98)
 - **RainForest** (Gehrke et al. 98)



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Backpropagation

- Is a **neural network** algorithm, performing on multilayer feed-forward networks (Rumelhart et al. 86).
- A network is a set of **connected input/output** units where each connection has an associated **weight**.
- The weights are adjusted during the training phase, in order to correctly predict the class label for samples.



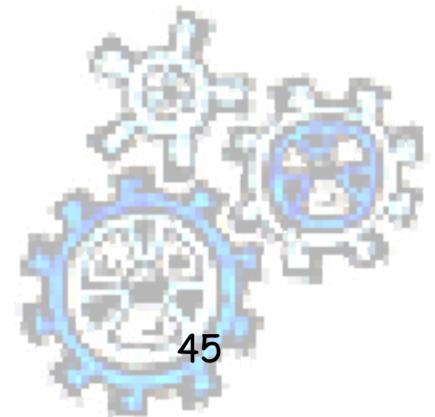
Backpropagation

PROS

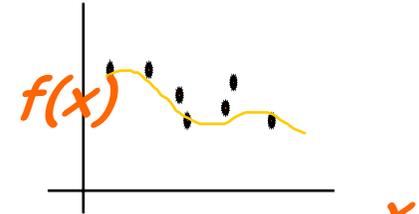
- High accuracy
- Robustness w.r.t. noise and outliers

CONS

- Long training time
- Network topology to be chosen empirically
- Poor interpretability of learned weights



Prediction and (statistical) regression



- Regression = construction of models of continuous attributes as functions of other attributes
- The constructed model can be used for prediction.
- E.g., a model to predict the sales of a product given its price
- Many problems solvable by **linear regression**, where attribute Y (**response variable**) is modeled as a linear function of other attribute(s) X (**predictor variable(s)**):

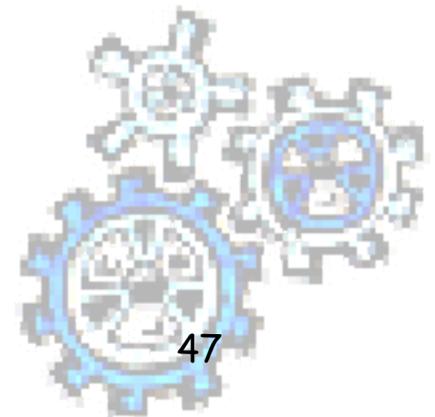
$$Y = a + b \cdot X$$

- Coefficients a and b are computed from the samples using the **least square method**.



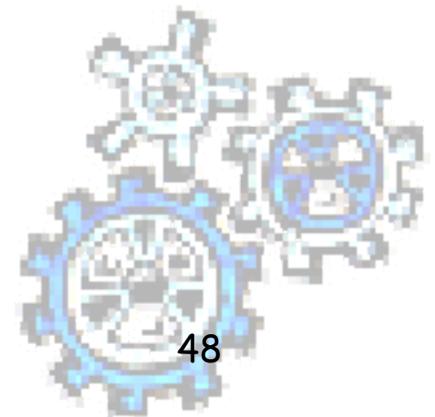
Other methods (not covered)

- *K*-nearest neighbors algorithms
- Case-based reasoning
- Genetic algorithms
- Rough sets
- Fuzzy logic
- Association-based classification (Liu et al 98)



Module outline

- The classification task
- Main classification techniques
 - Decision trees
 - Bayesian classifiers
 - Hints to other methods
- Application to a case-study in fraud detection: planning of fiscal audits



Fraud detection and audit planning

- A major task in fraud detection is constructing *models* of fraudulent behavior, for:
 - preventing future frauds (*on-line* fraud detection)
 - **discovering past frauds** (*a posteriori* fraud detection)
- Focus on a posteriori FD: **analyze historical audit data to plan effective future audits**
- Audit planning is a key factor, e.g. in the fiscal and insurance domain:
 - tax evasion (from incorrect/fraudulent tax declarations) estimated in Italy between 3% and 10% of GNP

Case study

- Conducted by our Pisa KDD Lab (Bonchi et al 99)
- A data mining project at the Italian Ministry of Finance, with the aim of assessing:
 - the potential of a KDD process oriented to **planning audit strategies**;
 - a **methodology** which supports this process;
 - an integrated **logic-based environment** which supports its development.



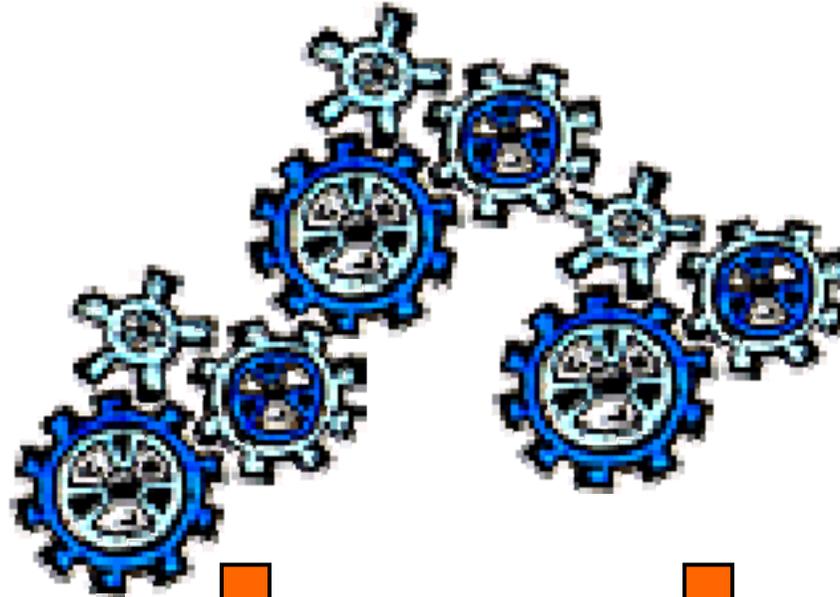
Audit planning

- Need to face a trade-off between conflicting issues:
 - *maximize audit benefits*: select subjects to be audited to maximize the recovery of evaded tax
 - *minimize audit costs*: select subjects to be audited to minimize the resources needed to carry out the audits.
- Is there a KDD methodology which may be **tuned** according to these options?
- How extracted knowledge may be combined with domain knowledge to obtain useful audit models?

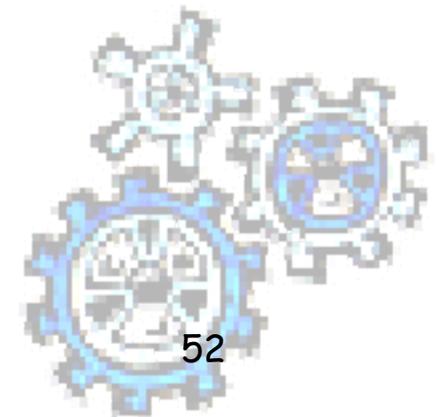


Autofocus data mining

policy options, business rules

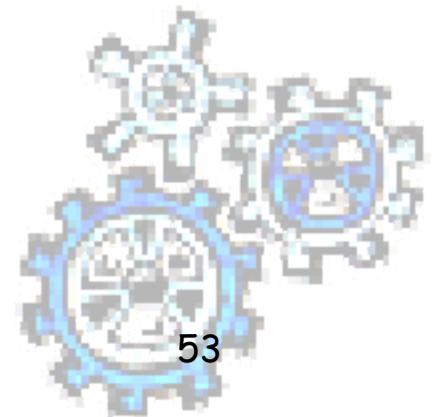


fine parameter tuning of mining tools



Classification with decision trees

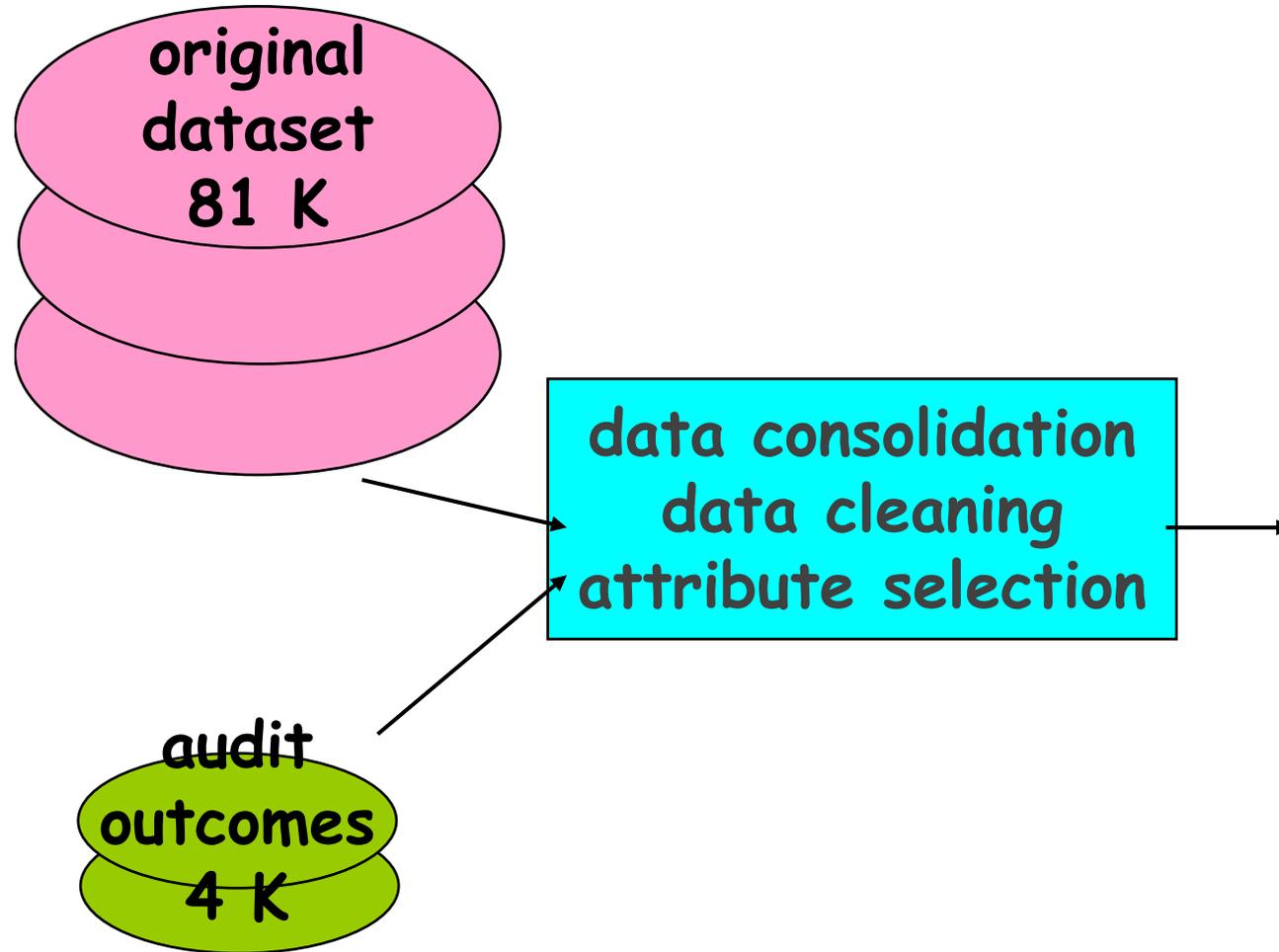
- Reference technique:
 - Quinlan's **C4.5**, and its evolution **C5.0**
- Advanced mechanisms used:
 - pruning factor
 - misclassification weights
 - boosting factor



Available data sources

- Dataset: **tax declarations**, concerning a targeted class of Italian **companies**, integrated with other sources:
 - social benefits to employees, official budget documents, electricity and telephone bills.
- Size: **80 K** tuples, 175 numeric attributes.
- A subset of **4 K** tuples corresponds to the **audited** companies:
 - outcome of audits recorded as the **recovery** attribute (= **amount of evaded tax ascertained**)

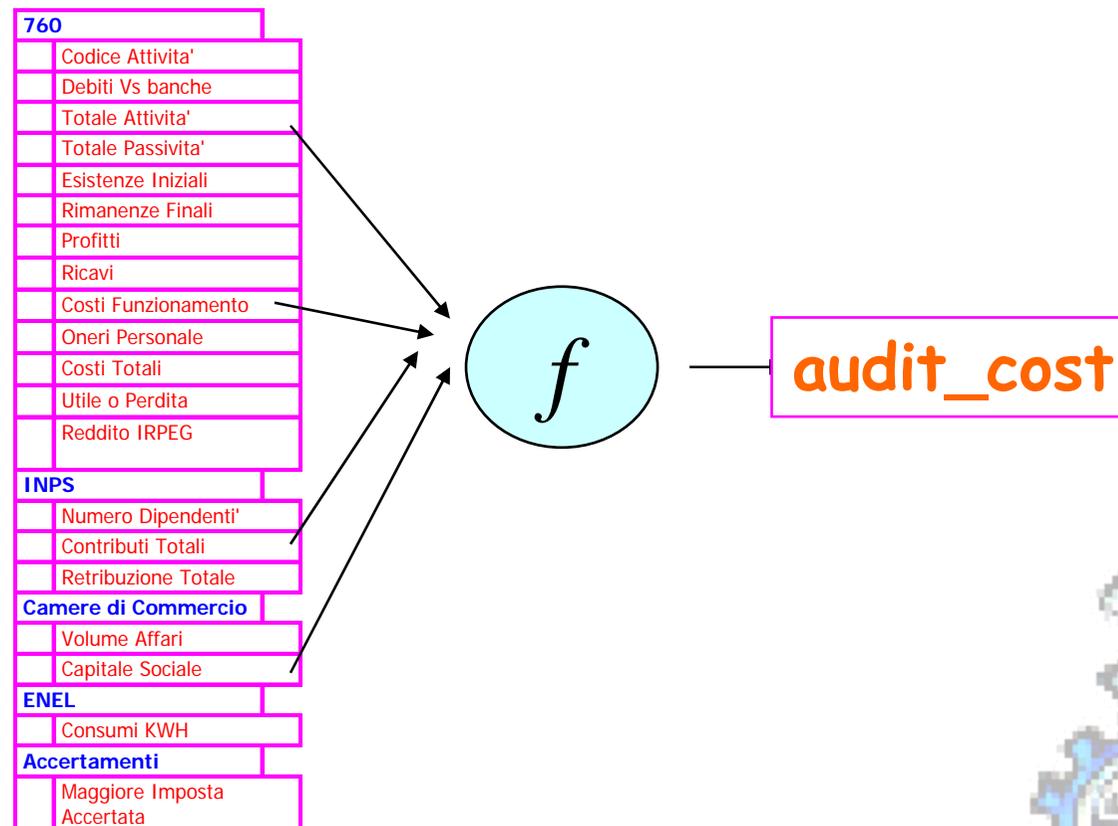
Data preparation



TAX DECLARATION	
Codice Attivita'	
Debiti Vs banche	
Totale Attivita'	
Totale Passivita'	
Esistenze Iniziali	
Rimanenze Finali	
Profitti	
Ricavi	
Costi Funzionamento	
Oneri Personale	
Costi Totali	
Utile o Perdita	
Reddito IRPEG	
SOCIAL BENEFITS	
Numero Dipendenti'	
Contributi Totali	
Retribuzione Totale	
OFFICIAL BUDGET	
Volume Affari	
Capitale Sociale	
ELECTRICITY BILLS	
Consumi KWH	
AUDIT	
Recovery	

Cost model

- A derived attribute **audit_cost** is defined as a function of other attributes



Cost model and the target variable

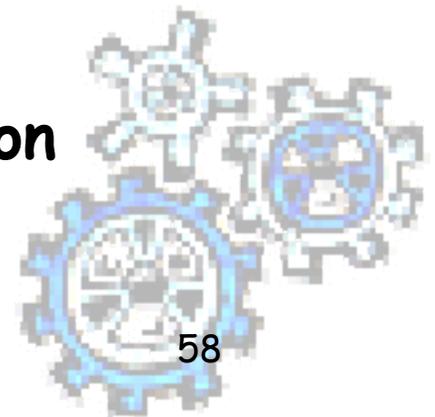
- recovery of an audit after the audit cost
 $\text{actual_recovery} = \text{recovery} - \text{audit_cost}$
- target variable (class label) of our analysis is set as the **Class of Actual Recovery (c.a.r.)**:

- $\text{c.a.r.} = \begin{cases} \text{negative} & \text{if } \text{actual_recovery} \leq 0 \\ \text{positive} & \text{if } \text{actual_recovery} > 0. \end{cases}$



Training set & test set

- Aim: build a binary classifier with **c.a.r.** as target variable, and evaluate it
- Dataset is partitioned into:
 - training set, to build the classifier
 - test set, to evaluate it
- Relative size: **incremental samples** approach
- In our case, the resulting classifiers improve with larger training sets.
- Accuracy test with 10-fold cross-validation



Quality assessment indicators

- The obtained classifiers are evaluated according to several **indicators**, or metrics
- **Domain-independent** indicators
 - confusion matrix
 - misclassification rate
- **Domain-dependent** indicators
 - audit #
 - actual recovery
 - profitability
 - relevance



Domain-independent quality indicators

■ confusion matrix (of a given classifier)

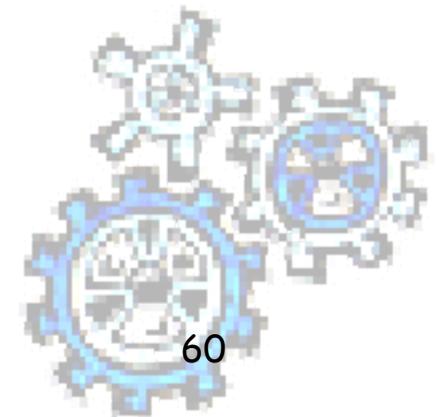
negative	positive	← classified as
TN	FP	actual class negative
FN	TP	actual class positive

TN (TP): true negative (positive) tuples

FN (FP): false negative (positive) tuples

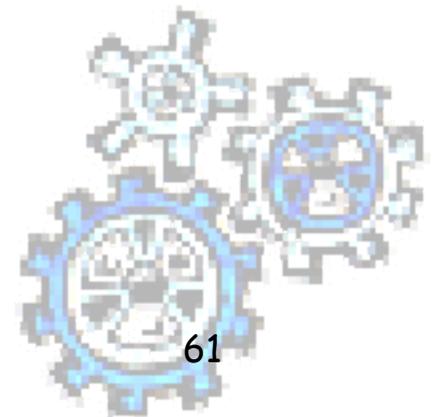
misclassification rate =

$$\# (\text{FN} \cup \text{FP}) / \# \text{ test-set}$$



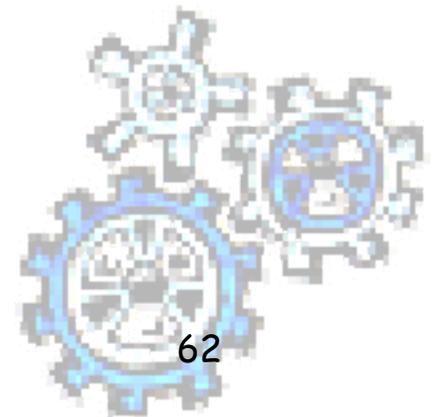
Domain-dependent quality indicators

- **audit #** (of a given classifier): number of tuples classified as positive =
 $\# (FP \cup TP)$
- **actual recovery**: total amount of actual recovery for all tuples classified as positive
- **profitability**: average actual recovery per audit
- **relevance**: ratio between profitability and misclassification rate



The REAL case

- Classifiers can be compared with the REAL case, consisting of the whole test-set:
- audit # (REAL) = 366
- actual recovery(REAL) = 159.6 M euro



Controlling classifier construction

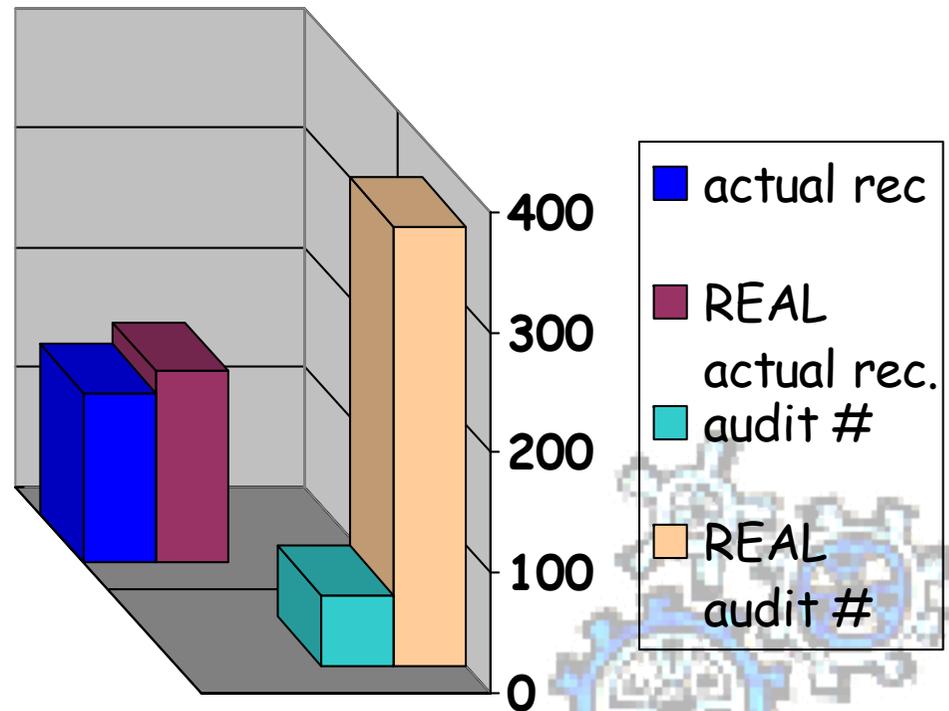
- *maximize audit benefits*: minimize FN
- *minimize audit costs*: minimize FP
- hard to get both!
 - unbalance tree construction towards either negatives or positives
- which parameters may be tuned?
 - misclassification weights, e.g., trade 1 FN for 10 FP
 - replication of minority class
 - boosting and pruning level



Model evaluation: classifier 1 (min FP)

- no replication in training-set (unbalance towards negative)
- 10-trees adaptive boosting

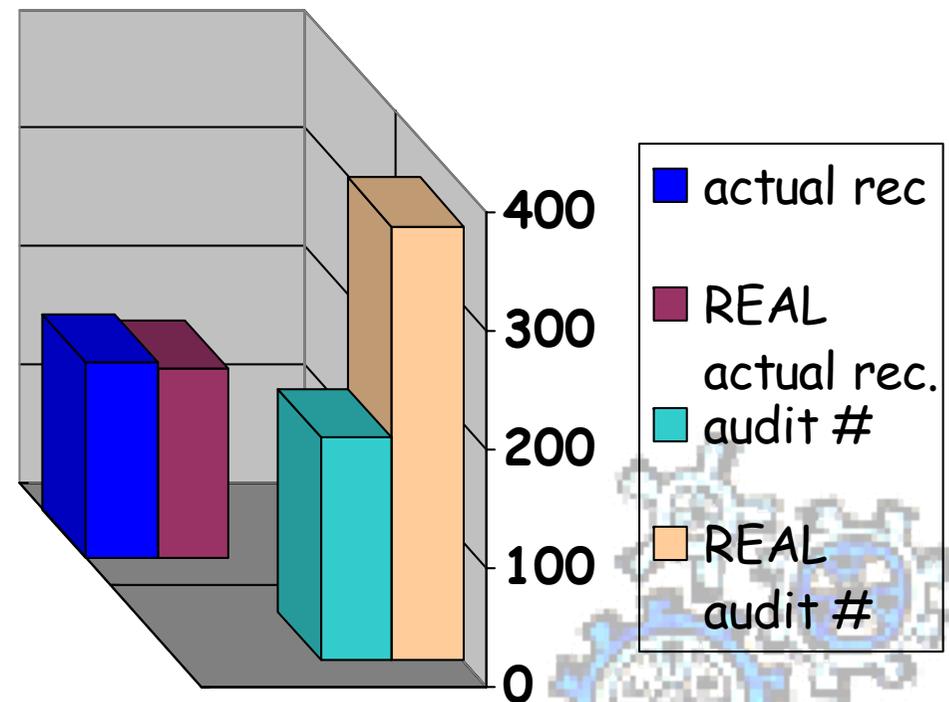
- *misc. rate* = 22%
- *audit #* = 59 (11 FP)
- *actual rec.* = 141.7 Meuro
- *profitability* = 2.401



Model evaluation: classifier 2 (min FN)

- replication in training-set (balanced neg/pos)
- misc. weights (trade 3 FP for 1 FN)
- 3-trees adaptive boosting

- *misc. rate* = 34%
- *audit #* = 188 (98 FN)
- *actual rec.* = 165.2 Meuro
- *profitability* = 0.878



What have we achieved?

- Idea of a **KDD methodology** tailored for a vertical application: **audit planning**
 - define an audit cost model
 - monitor training- and test-set construction
 - assess the quality of a classifier
 - tune classifier construction to specific policies
- Its formalization requires a flexible **KDSE - knowledge discovery support environment**, supporting:
 - integration of deduction and induction
 - integration of domain and induced knowledge
 - separation of conceptual and implementation level



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