DATA MINING 2 Exercises – Time Series

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a.a. 2019/2020

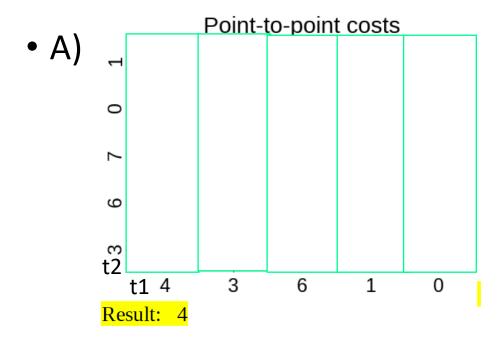


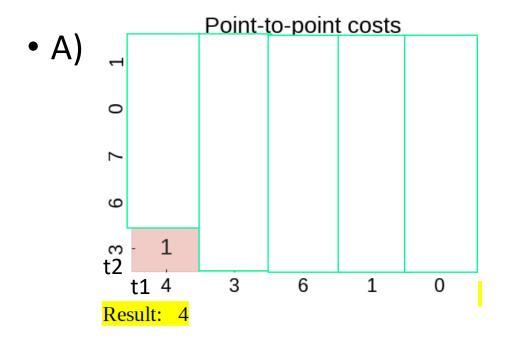
Dynamic Time Warping

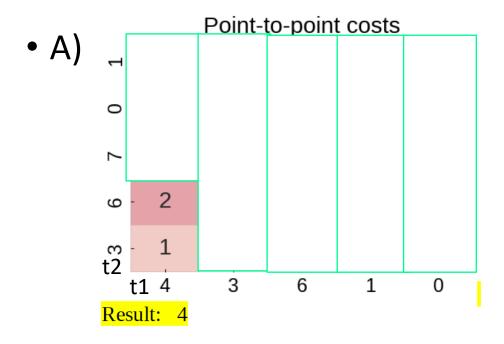
DTW – Exercise 1

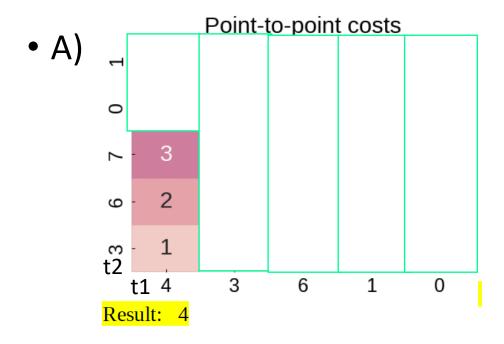
• Given the following input time series:

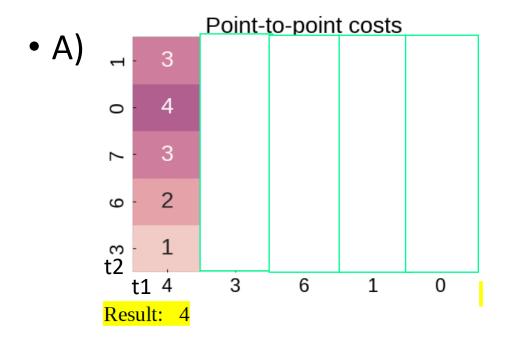
- A) Compute the distance between "t1" and "t2", using the DTW with distance between points computed as d(x,y) = |x y|.
- B) If we repeat the computation of point (A) above, this time with a Sakoe-Chiba band of size r=1, does the result change? Why?
- C) If we compute DTW(T1,T2), where T1 is equal to t1 in reverse order (namely T1=<0,1,6,3,4>) and similarly for T2 (namely T2=<1,0,7,6,3>), is it true that DTW(T1,T2) = DTW(t1,t2)? Discuss the problem without providing any computation.

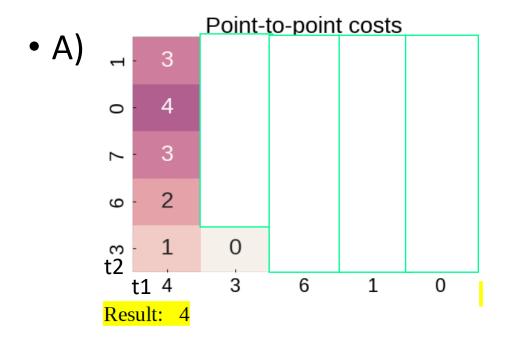


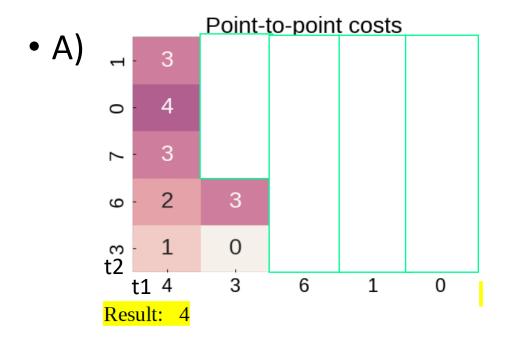


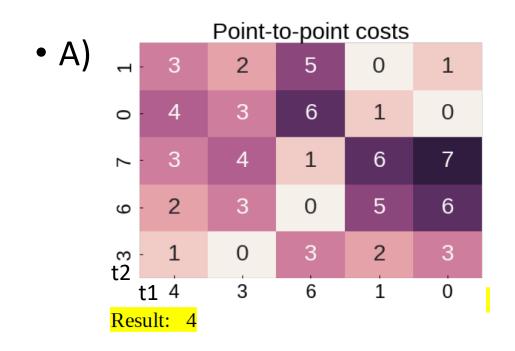


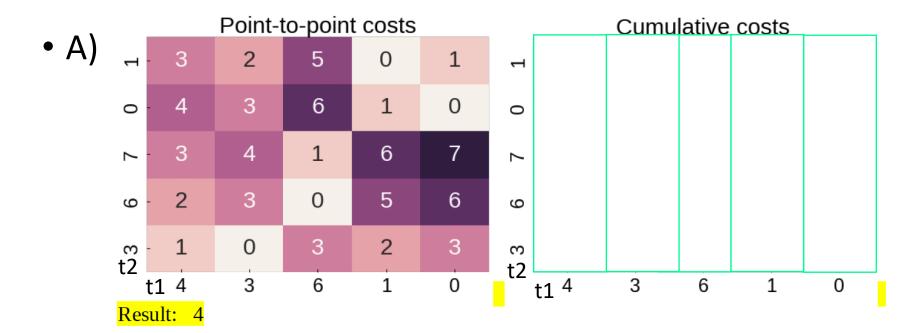


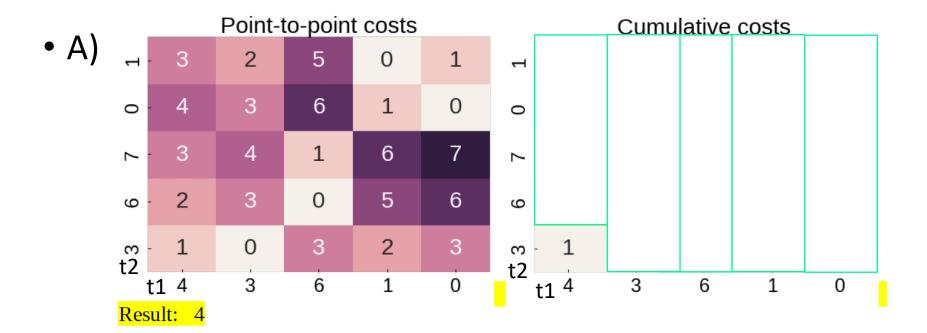


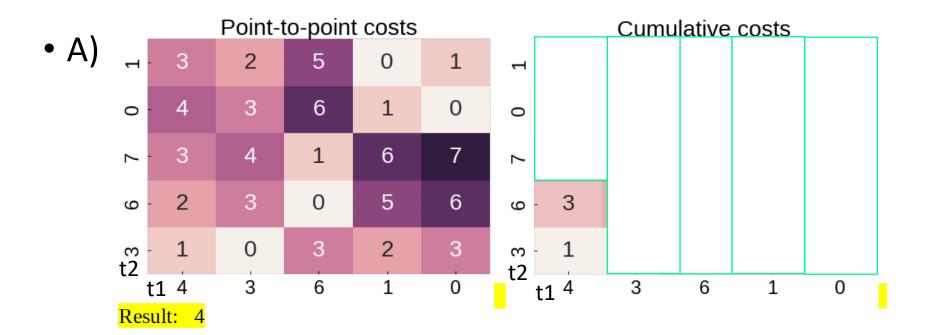


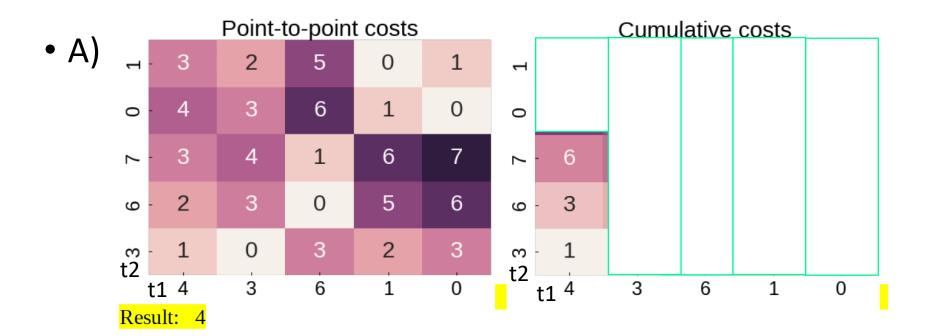


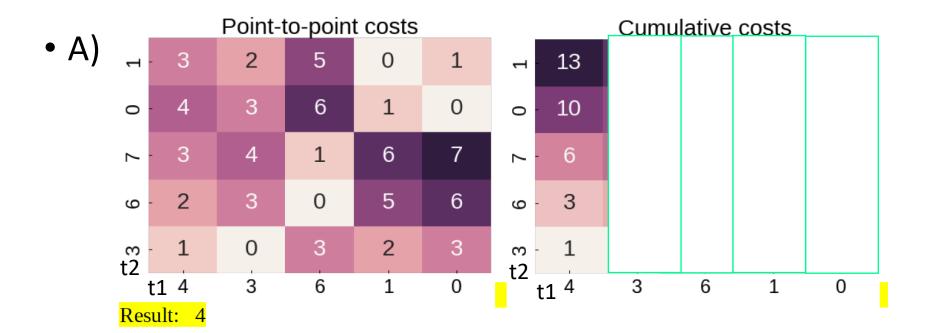


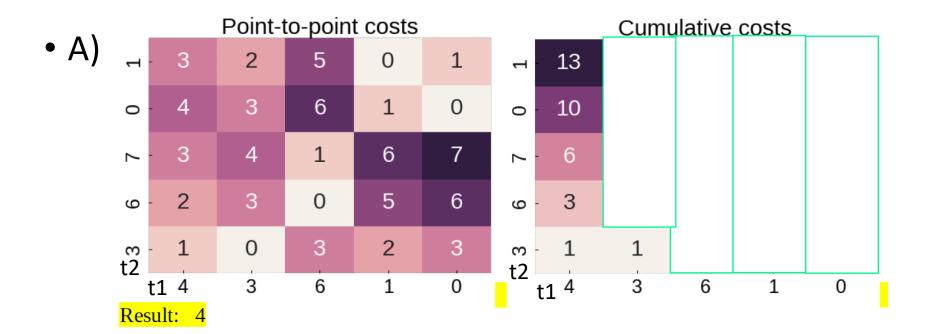


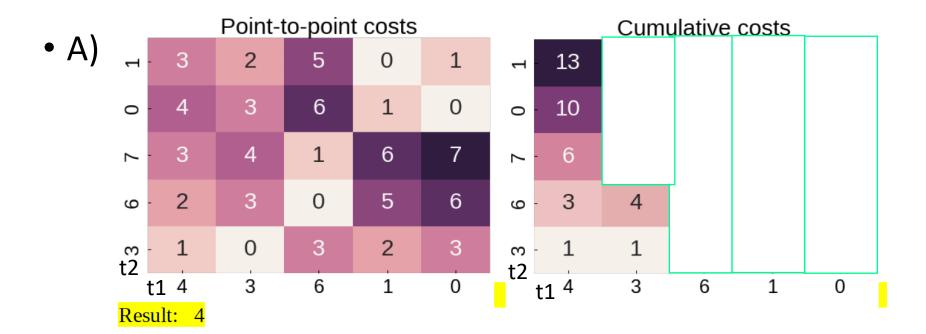


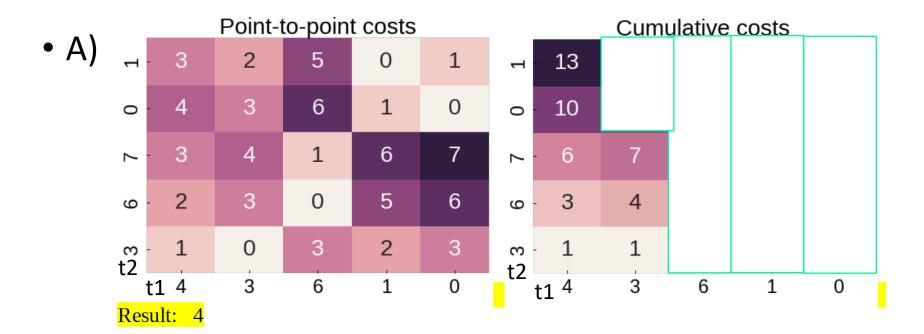


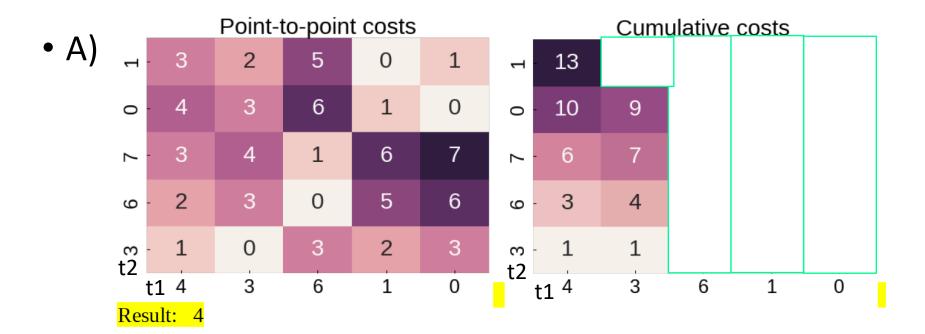


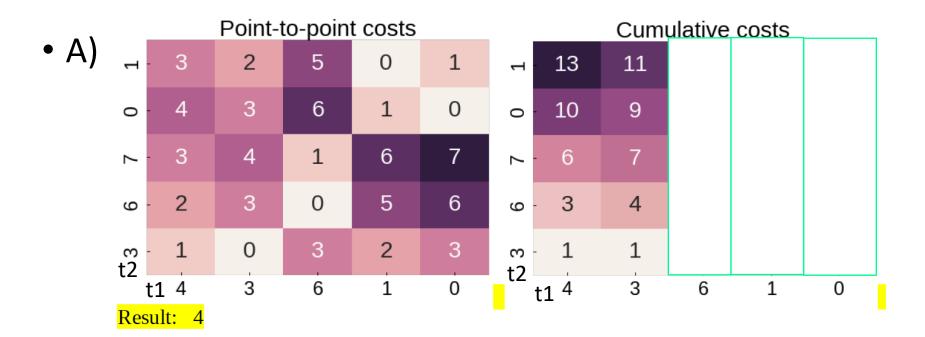


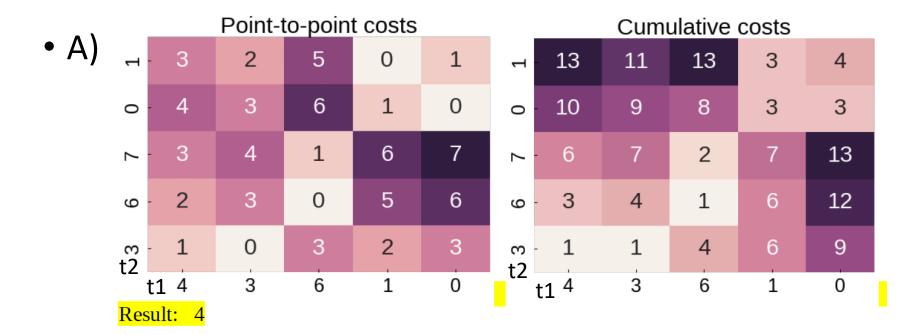


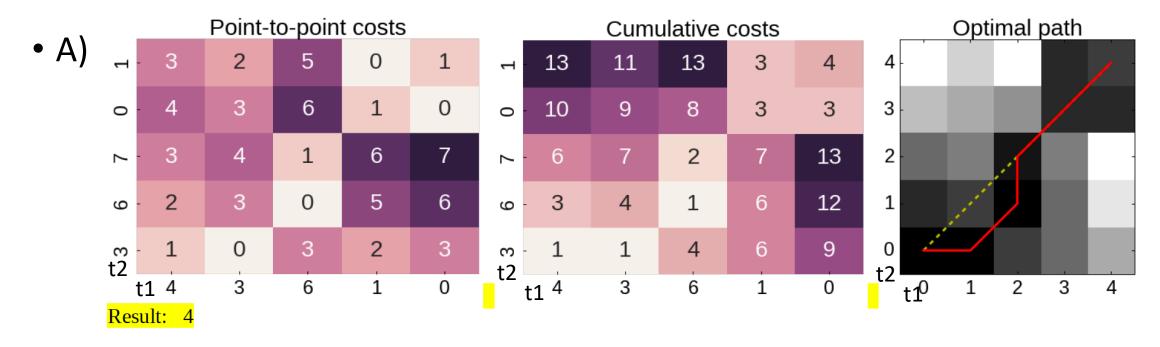












- B) No. Because the DTW optimal path remains inside the band of size r=1
- C) Yes. The optimal path in one direction is the same in the opposite direction. Though, the cumulative costs matrix might look different.

DTW – Exercise 2

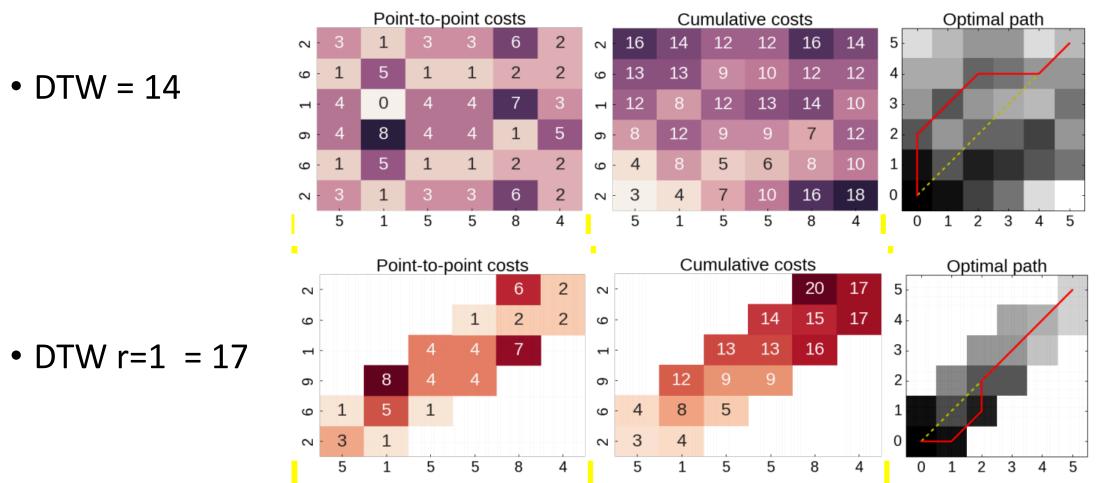
Given the following time series:
t = < 2, 6, 9, 1, 6, 2 >
q = < 5, 1, 5, 5, 8, 4 >

compute

- (i) their Manhattan and Euclidean distance,
- (ii) their DTW, and (iii) their DTW with Sakoe-Chiba band of size r=1 (i.e. all cells at distance <= 1 from the diagonal are allowed).
- For points (ii) and (iii) show the cost matrix and the optimal path found.

DTW – Exercise 2 - Solution

• Euclidean = sqrt(74) = 8.6, Manhattan = 20



DTW – Exercise 3

• Given the following time series:

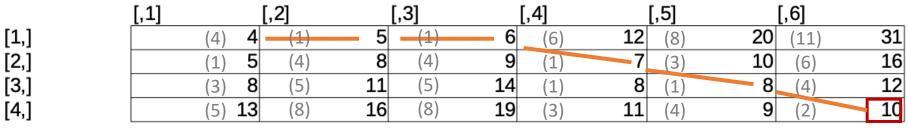
ID	Time series
W	< 6, 11, 13, 15 >
Х	< 10, 7, 7, 12, 14, 17 >
Y	< 9, 11, 14, 13, 20 >

 Compute the distances among all pairs of time series adopting a Dynamic Time Warping distance, and computing the distances between single points as d(x,y) = | x - y |. For each pair of time series compared also show the matrix used to compute the final result.

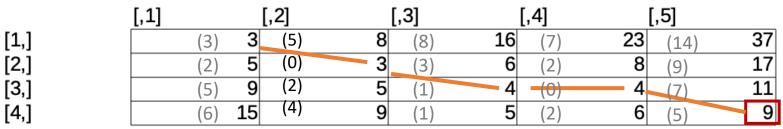
ID	Time series
W	< 6, 11, 13, 15 >
Х	< 10, 7, 7, 12, 14, 17 >
Y	< 9, 11, 14, 13, 20 >

DTW – Exercise 3 - Solution

W – X

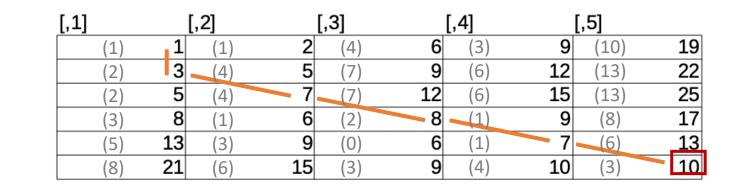


W – Y



X – Y

[1,] [2,] [3,] [4,] [5,] [6,]

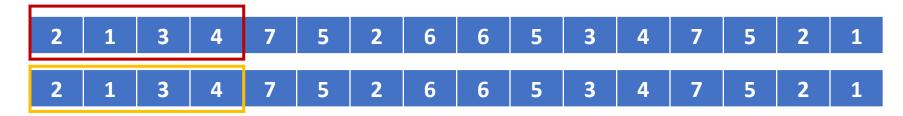


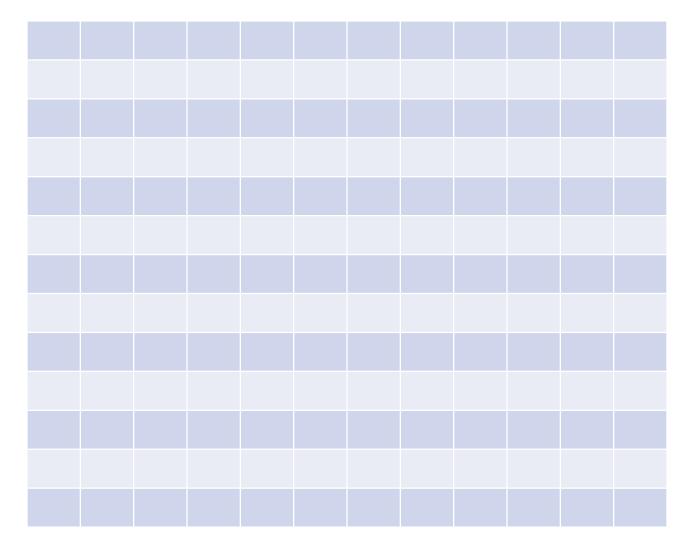
Matrix Profile

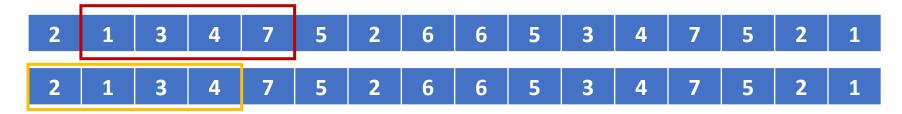
Given the TS x = <2,1,3,4,7,5,2,6,6,5,3,4,7,5,2,1> and the

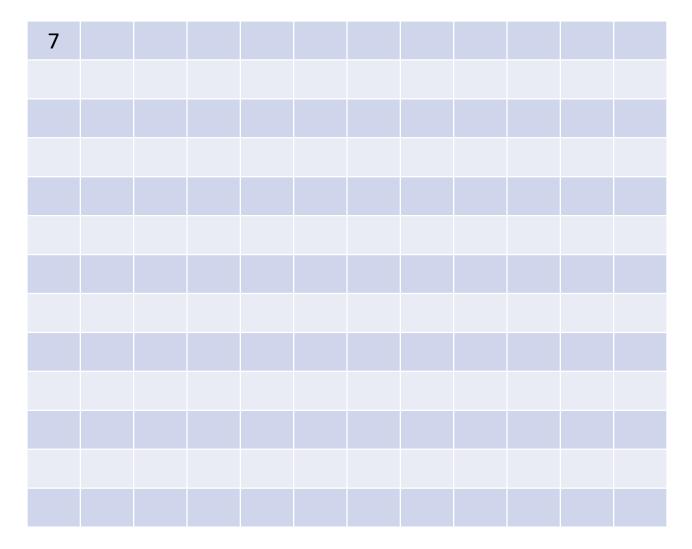
- 1. Build the Matrix Profile for x with m=4 using the Manahttan distance as distance function between subsequences.
- 2. Draw the Matrix Profile
- 3. Identify the motifs with distance equals 0 and length equals to m
- 4. Which is a correct value for m that would have retrieved less motifs with distance equaks to 0?

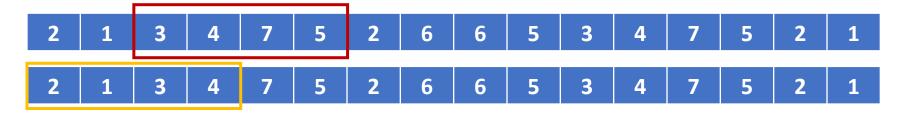


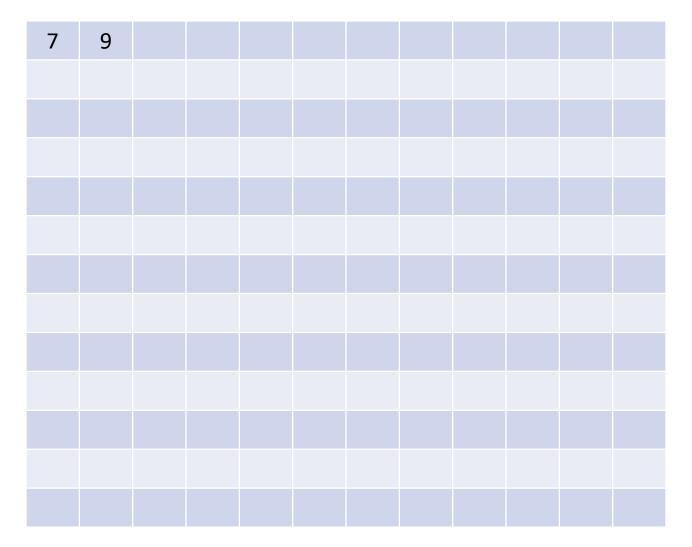


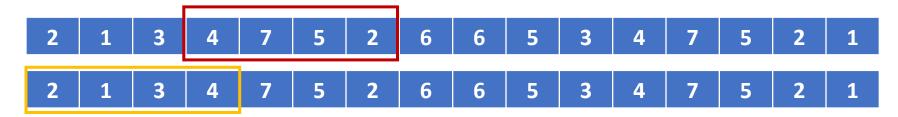


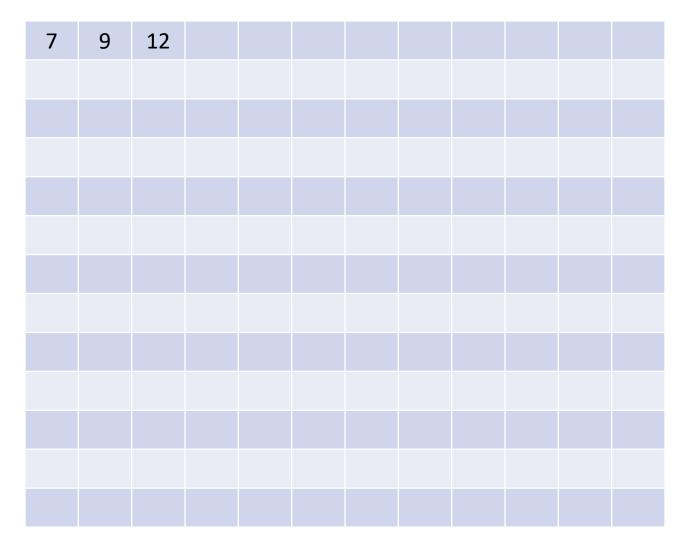






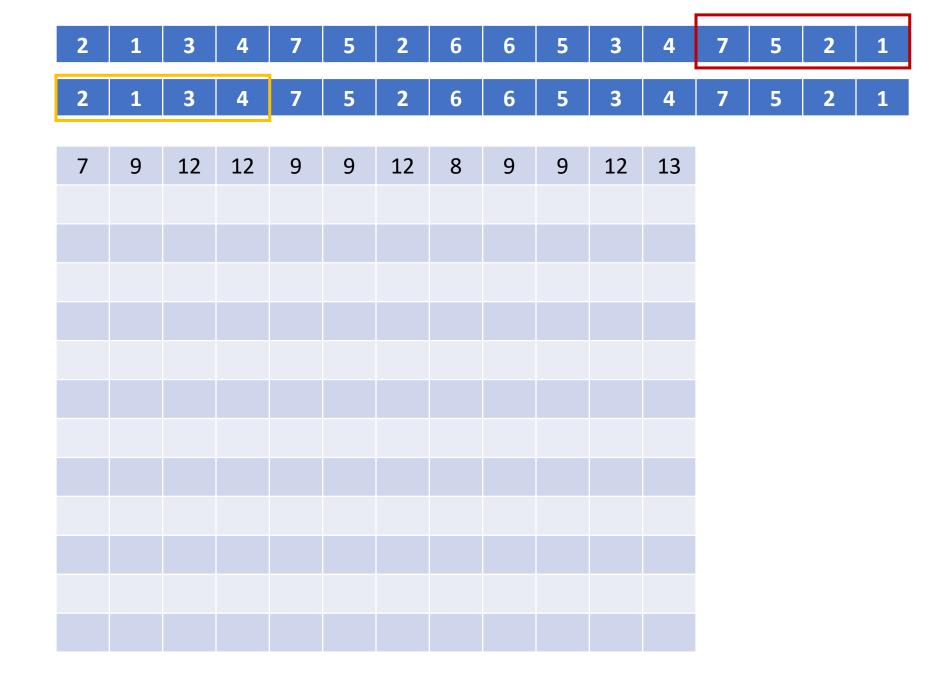


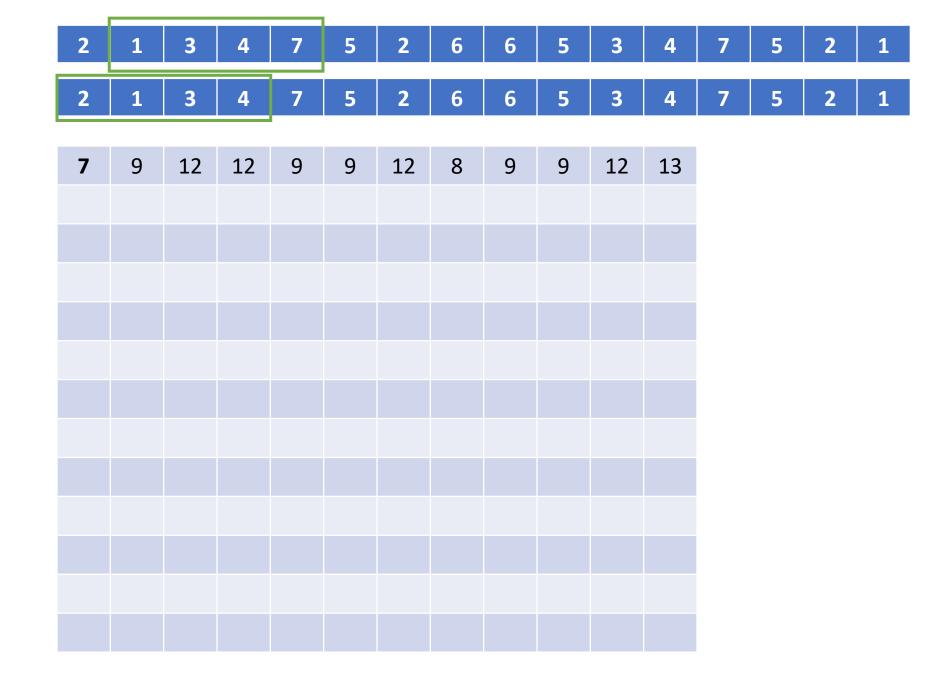




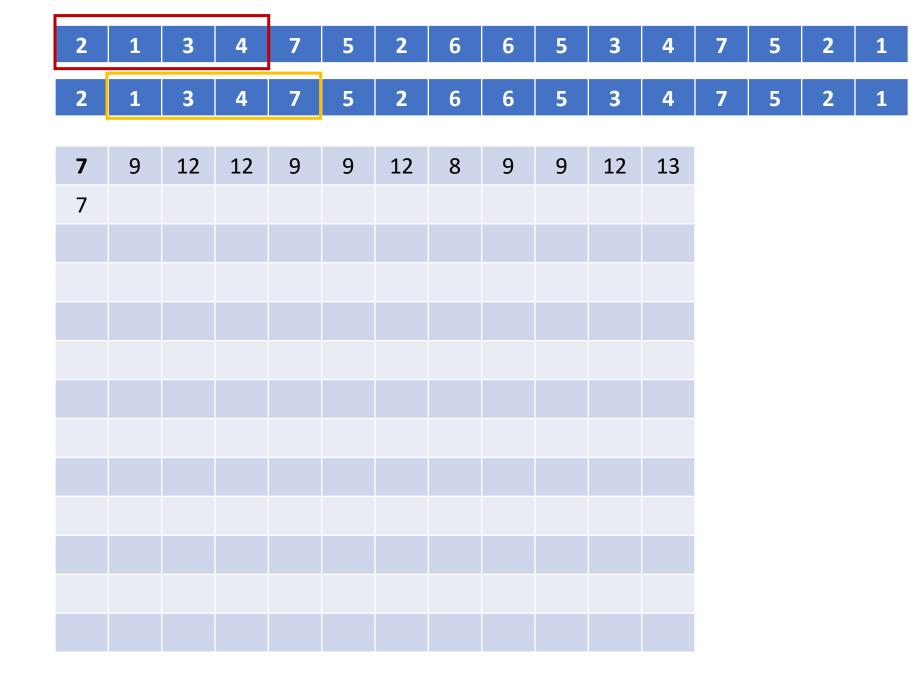


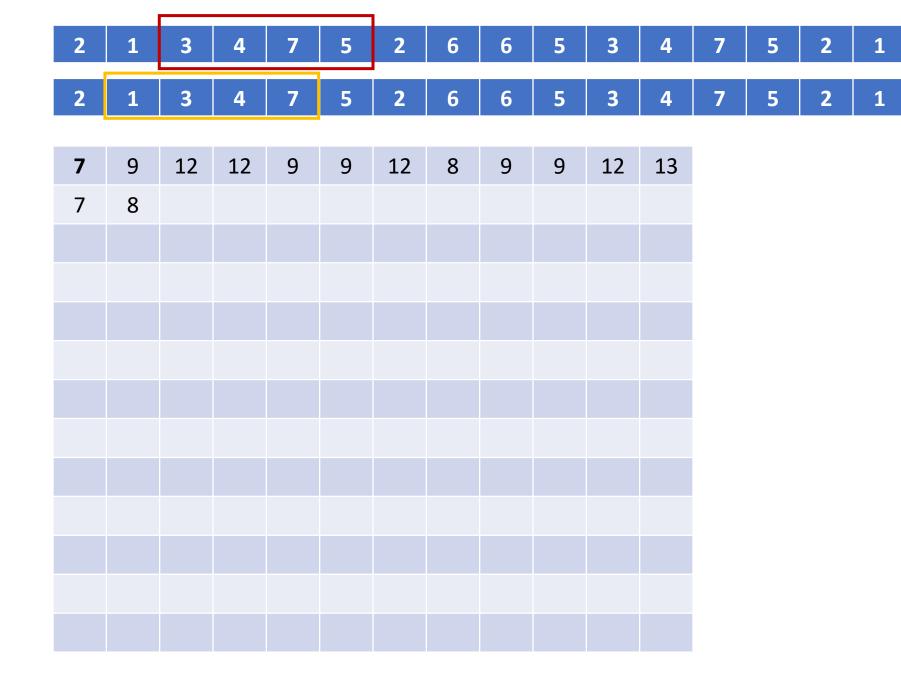
7	9	12	12				

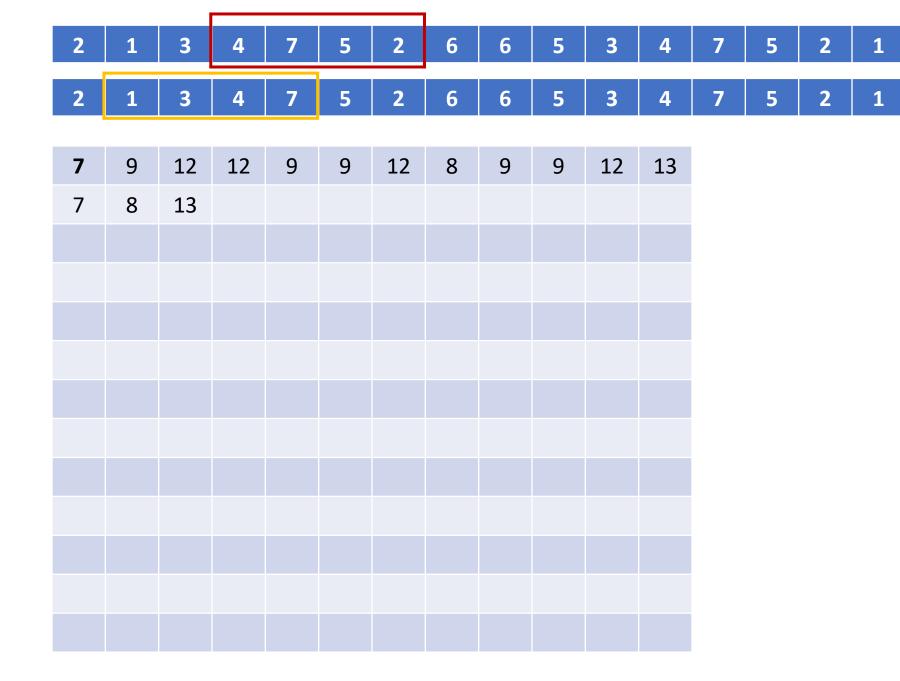


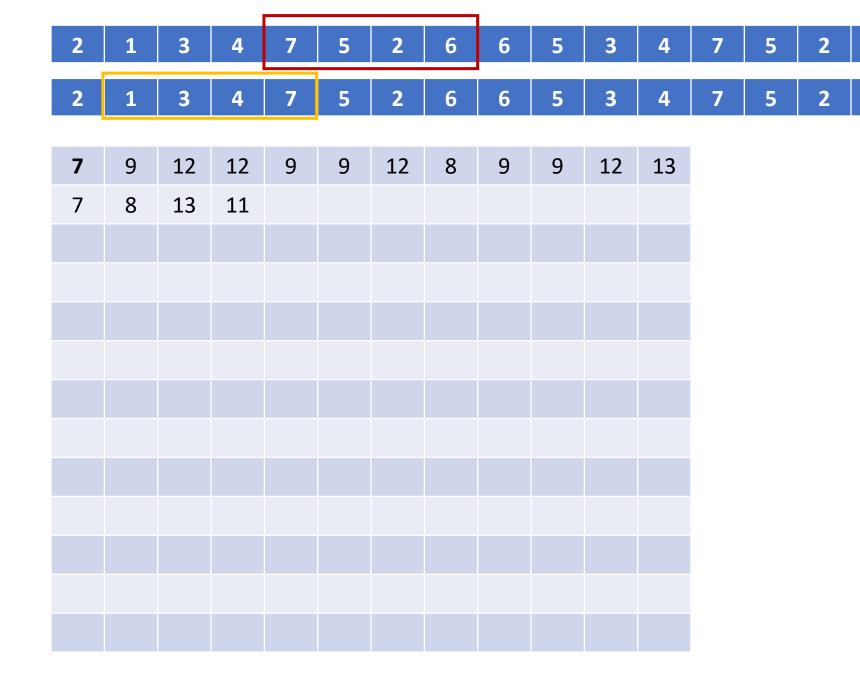


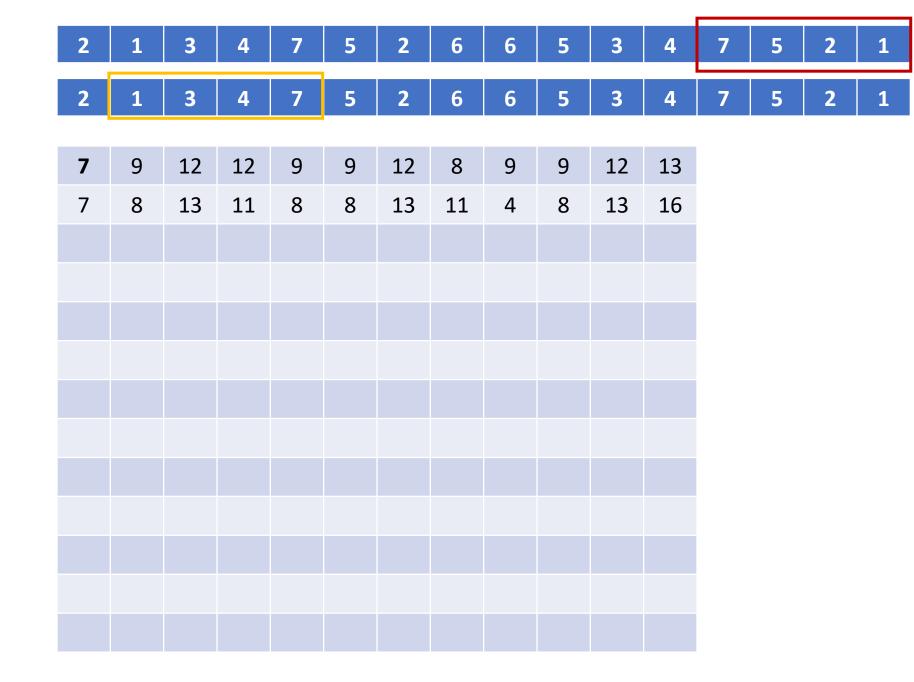
m = 4

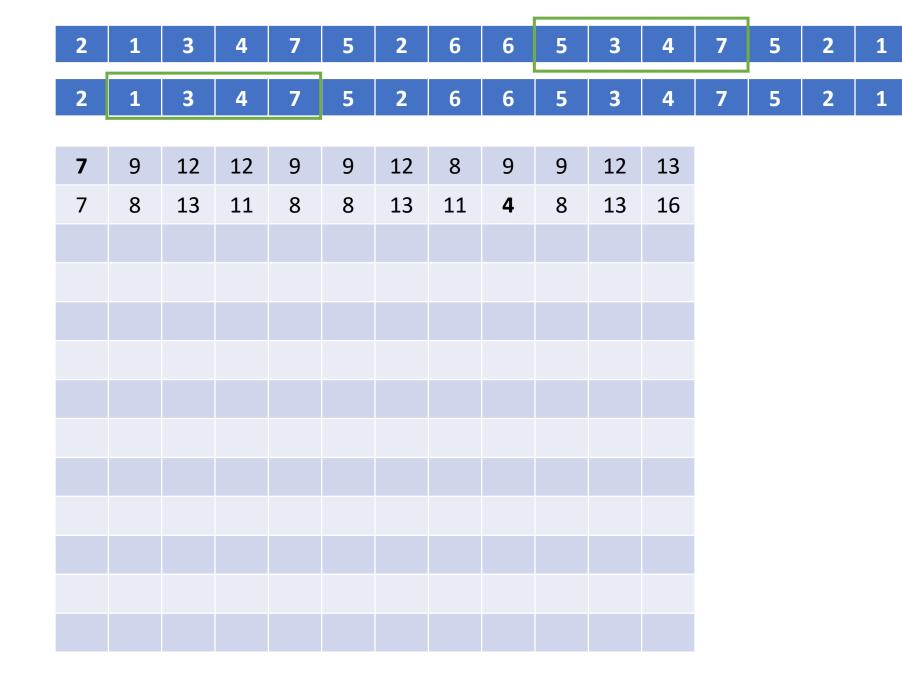










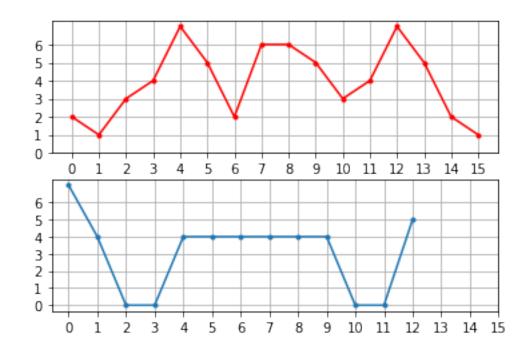


m = 4

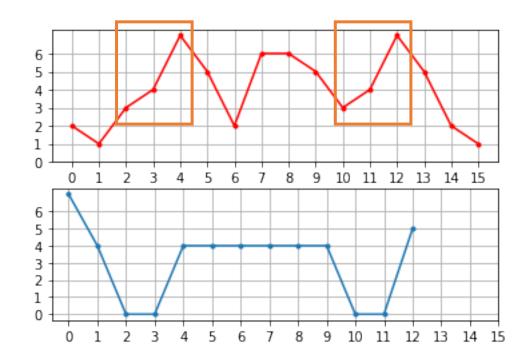
2	1	3	4	7	5	2	6	6	5	3	4	7	5	2	1
2	1	3	4	7	5	2	6	6	5	3	4	7	5	2	1
7	9	12	12	9	9	12	8	9	9	12	13				
7	8	13	11	8	8	13	11	4	8	13	16				
9															

2	1	3	4	7	5	2	6	6	5	3	4	7	5	2	1
2	1	3	4	7	5	2	6	6	5	3	4	7	5	2	1
7	9	12	12	9	9	12	8	9	9	12	13				
7	8	13	11	8	8	13	11	4	8	13	16				
9	8	9	11	6	4	9	9	8	0						

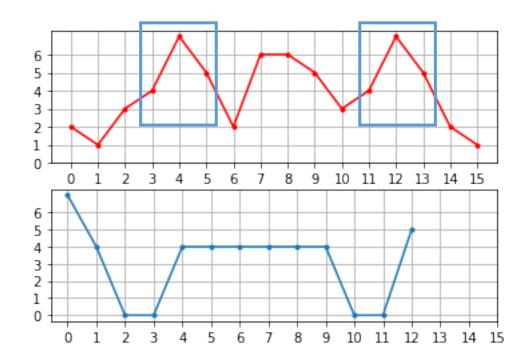
- x = <2, 1, 3, 4, 7, 5, 2, 6, 6, 5, 3, 4, 7, 5, 2, 1>
- mp = < 7, 4, 0, 0, 4, 4, 4, 4, 4, 4, 0, 0, 5 >



- x = <2, 1, 3, 4, 7, 5, 2, 6, 6, 5, 3, 4, 7, 5, 2, 1>
- mp = < 7, 4, 0, 0, 4, 4, 4, 4, 4, 4, 0, 0, 5 >



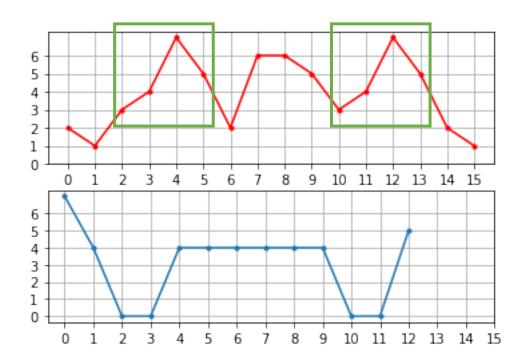
- x = <2, 1, 3, 4, 7, 5, 2, 6, 6, 5, 3, 4, 7, 5, 2, 1>
- mp = < 7, 4, 0, 0, 4, 4, 4, 4, 4, 4, 0, 0, 5 >



• x = <2, 1, 3, 4, 7, 5, 2, 6, 6, 5, 3, 4, 7, 5, 2, 1>

with m = 5

• mp = < 7, 4, 0, 0, 4, 4, 4, 4, 4, 4, 0, 0, 5 >



Given the TS x = <5,5,3,5,5,1> and the

- 1. Build the Matrix Profile for x with m=2 using the Manahttan distance as distance function between subsequences.
- 2. Draw the Matrix Profile
- 3. Identify the motifs with distance equals 0 and length equals to m

